



Information Retrieval

Index-Structures for Information Retrieval

Ulf Leser

Content of this Lecture

- Inverted files
- Storage structures
- Phrase and proximity search
- Building and updating the index
- Using a RDBMS

Full-Text Indexing

- Fundamental operation for all BoW approaches: $\text{find}(q, D)$
 - Given a term q , find all docs from D containing q
- Can be implemented using online search
 - Boyer-Moore, Keyword-Trees, etc.
- But
 - We **search for terms** (after tokenization), not arbitrary substrings
 - We assume that **D is stable** compared to q
 - The number of **unique terms** does not grow much with growing D
- Technique: Pre-compute a **term index** over D
 - “Full-text index” or “inverted file” or “inverted index”

Inverted Files (or Inverted Index)

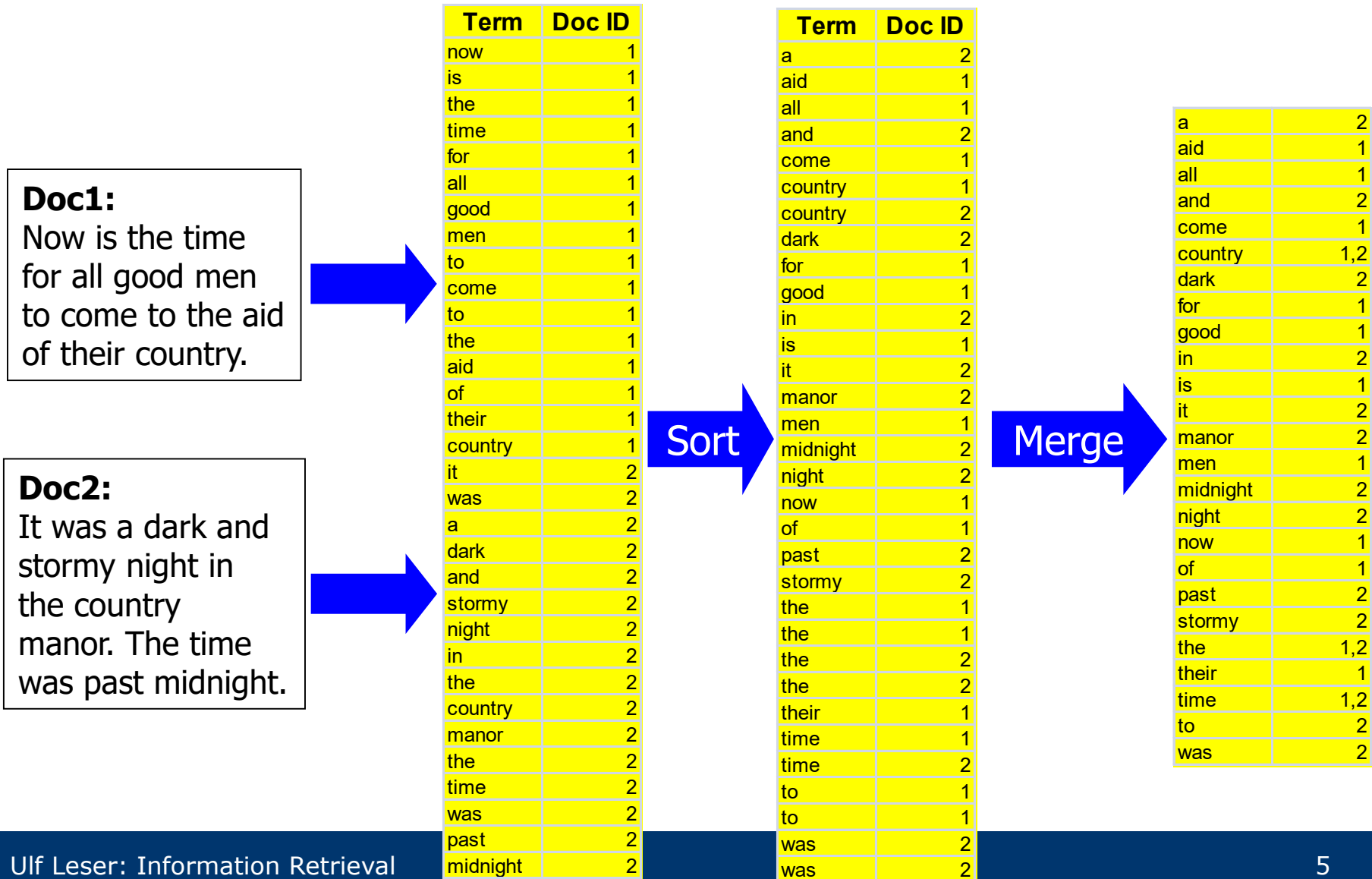
- Simple and effective **index structure** for terms
- Builds on the **Bag of words** approach
 - We give up on order of terms in docs (reappears later)
 - We cannot reconstruct docs based on index only
- Start from “docs containing terms” (~ “docs”) and invert to “**terms appearing in docs**” (~ “inverted docs”)

```
d1: t1, t3
d2: t1
d3: t2, t3
d4: t1
d5: t1, t2, t3
d6: t1, t2
d7: t2
d8: t2
```



```
t1: d1, d2, d4, d5, d6
t2: d3, d5, d6, d7, d8
t3: d1, d3, d5
```

Building an Inverted File [Andreas Nürnberger, IR-2007]



Boolean Retrieval

- For each query term k_i , look-up doc-list D_i containing k_i
- Evaluate query in the usual order

- $k_i \wedge k_j : D_i \cap D_j$

- $k_i \vee k_j : D_i \cup D_j$

- NOT $k_i : D \setminus D_i$

- Example

(time AND past AND the) OR (men)

$$= (D_{\text{time}} \cap D_{\text{past}} \cap D_{\text{the}}) \cup D_{\text{men}}$$

$$= (\{1,2\} \cap \{2\} \cap \{1,2\}) \cup \{1\}$$

$$= \{1,2\}$$

a	2
aid	1
all	1
and	2
come	1
country	1,2
dark	2
for	1
good	1
in	2
is	1
it	2
manor	2
men	1
midnight	2
night	2
now	1
of	1
past	2
stormy	2
the	1,2
their	1
time	1,2
to	2
was	2

Necessary and Obvious Tricks

- How do we **efficiently look-up doc-list D_i** ?
 - Bin-search on **sorted array** with all terms from K : $O(\log(|K|))$
 - How to do this if D and index is very large? (later)
- How do we support union and intersection efficiently?
 - Naïve algorithm requires $O(|D_i| * |D_j|)$
 - Better: Keep **doc-lists sorted**
 - Intersection $D_i \cap D_j$: Sort-Merge in $O(|D_i| + |D_j|)$
 - Union $D_i \cup D_j$: Sort-Merge in $O(|D_i| + |D_j|)$
 - If $|D_i| \ll |D_j|$, **use binsearch** in D_j for all terms in D_i
 - Whenever $|D_i| + |D_j| > |D_i| * \log(|D_j|)$

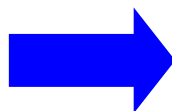
Less Obvious Tricks

- Define **selectivity** $sel(k_i) = df_i / |D|$
- Expected size of result is $|q| = |D| * sel(q) = |D| * \prod_i sel(k_i)$
 - Assuming AND and independence of query terms
- **Intermediate result sizes** vary greatly with different orders
 - These sizes have a large influence on runtime
 - How to keep sizes of intermediate results small?
 - Consider terms in order of **increasing selectivity**
 - Typically creates a few intersections at the beginning, then only look-ups
- General queries: Disjunctions, negations, ...
 - $sel(k_i \cup k_j) = sel(k_i) + sel(k_j) - (sel(k_i) * sel(k_j))$
 - Optimization problem: Find **optimal order of evaluation**

Adding Frequency

- VSM with $TF \cdot IDF$ requires term and document frequencies
- Split up inverted file into **dictionary** (term, df) and **posting list** ($\langle docID, tf \rangle$)

Term	docIDs	DF
a	2	1
aid	1	1
all	1	1
and	2	1
come	1	1
country	1,2	2
dark	2	1
...
of	1	1
past	2	1
stormy	2	1
the	1,2	2
their	1	1
time	1,2	2
to	1	1
was	2	1



Dictionary

Term	DF
a	1
aid	1
all	1
and	1
come	1
country	2
dark	1
...	...
of	1
past	1
stormy	1
the	2
their	1
time	2
to	1
was	1

Postings

Posting
(2,1)
(1,1)
(1,1)
(2,1)
(1,1)
(1,1), (2,1)
(2,1)
...
(1,1)
(2,1)
(2,1)
(1,2), (2,1)
(1,1)
(1,1), (2,1)
(1,2)
(2,2)

Searching in VSM

- Assume we want to retrieve the **top-r docs**
- Algorithm
 - Initialize an empty doc-list S (as hash table or priority queue)
 - Will manage pairs (docID, score)
 - Score is computed incrementally, query term by query term
 - Iterate through query terms k_i
 - Retrieve posting list P
 - For all (docID, TF) \in P
 - If docID \in S: $S[\text{docID}] = + \text{IDF}[k_i] * \text{TF}$
 - else: $S = S.\text{append}(\text{docID}, \text{IDF}[k_i] * \text{TF})$
 - For all pairs in S: Normalize scores
 - Return top-r docs in S
- S contains all and only those docs containing **at least one k_i**

$$\text{sim}(d, q) = \frac{\sum (v_q[i] * v_d[i])}{\sqrt{\sum v_d[i]^2}}$$

Improvement

- Sort **query terms** by decreasing IDF Values – later terms have **smaller IDF values** – less impact on score
- Sort **posting lists** by decreasing TF values – later docs have smaller TF values – less impact on score
- Several **heuristics** for faster approximate VSM
 - H1: Stop adding docs to S in each posting if TF value too small
 - H2: Drop query terms whose IDF value is too small
 - Typically **stop words** with long posting lists – much work, little effect
 - H3: Assume we look at term k_i and are at position TF_j in the posting list. If $s^r - s^{r+1} > IDF_i * TF_j$, stop searching this posting list
 - ...

Illustration H1

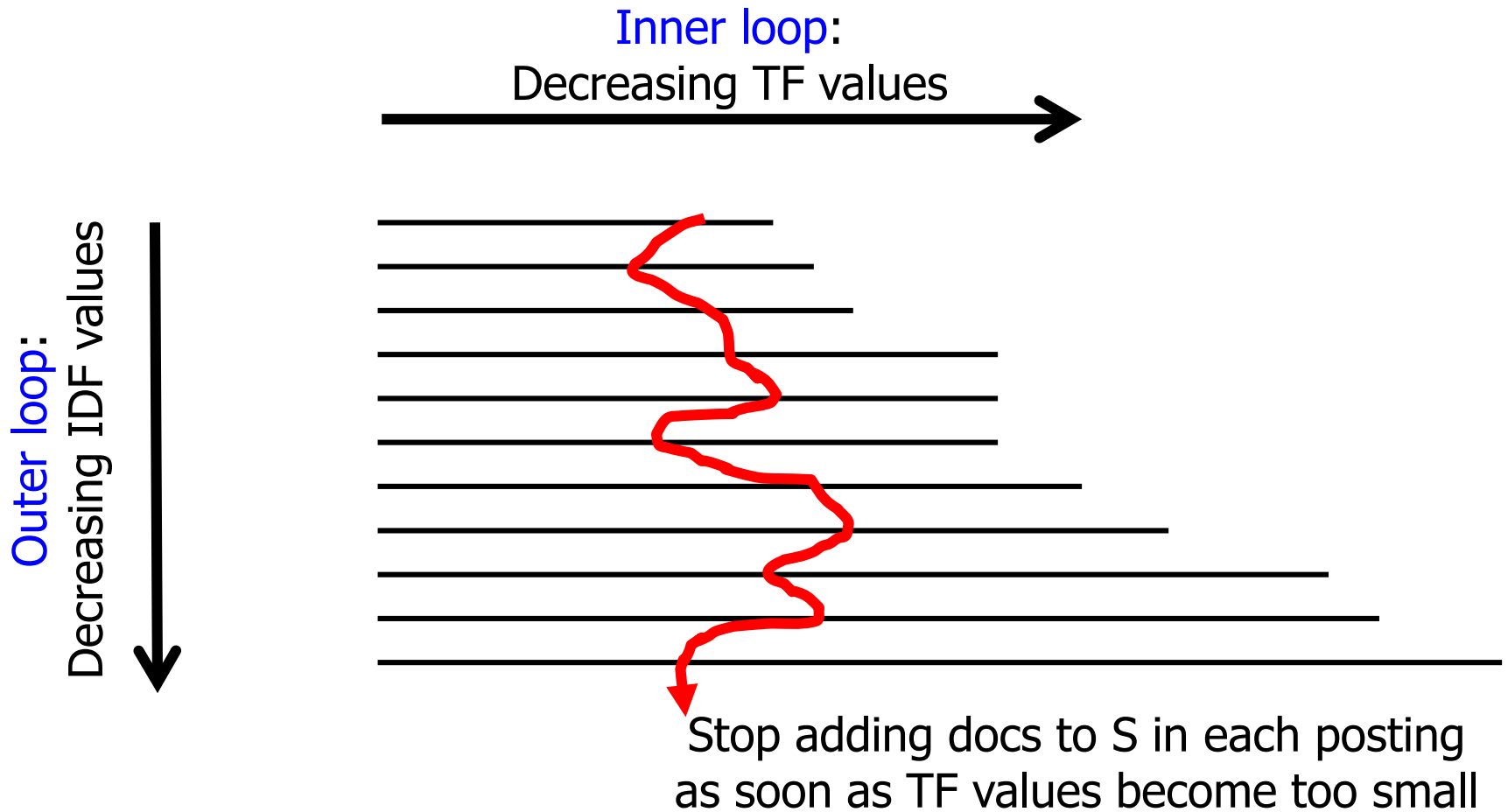


Illustration H2

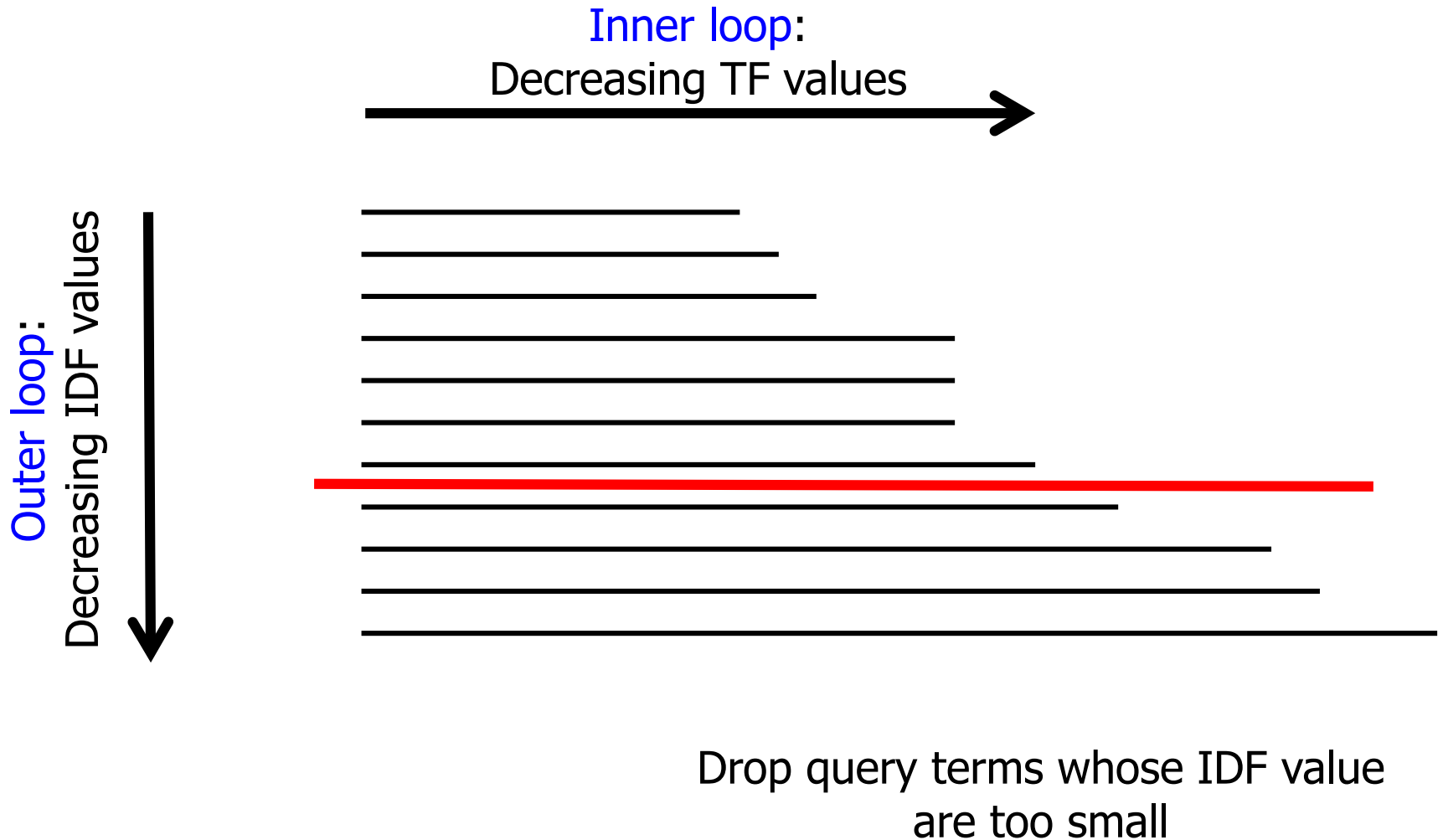
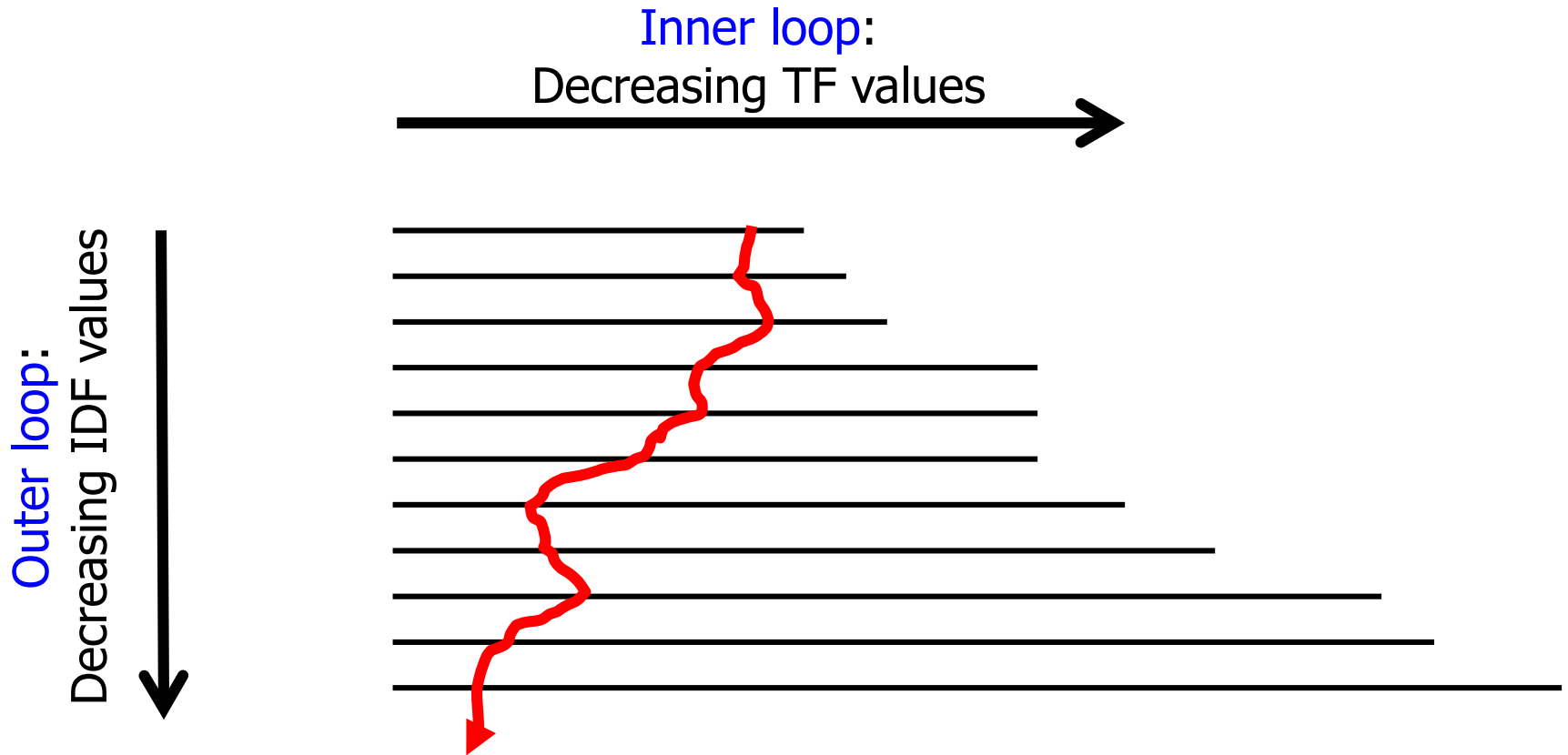


Illustration H3



If $s^r - s^{r+1} > IDF_i * TF_j$, stop searching this posting list

Space Usage

- Size of dictionary: $|K|$
 - Zipf's law: If D is large, adding docs to D adds only few terms to K
 - But there are always new terms, no matter how large D
 - Example: 1GB text (TREC-2) generates only 5MB dictionary
 - Herdan–Heaps law: $|K| = a \cdot \text{terms}(D)^b$
 - With $a \sim 50$ and $b \sim 0,5$ (for English)
 - Typically: $|K| < 1$ Million
 - Not true in multi-lingual corpora, web corpora, etc.
- Size of posting list
 - Theoretic worst case: $O(|K| \cdot |D|)$
 - Average case analysis is difficult, but certainly still large (in $|D|$)
- Implementation
 - Dictionary is small; should always fit into **main memory**
 - Posting lists is large; **keep on disk**

Content of this Lecture

- General approach
- Storage structures
 - The dictionary
 - The posting lists
- Phrase and proximity search
- Building and updating the index
- Using a RDBMS

Storing the Dictionary

- Dictionary are always kept in main memory
- Suitable **data structures**?

Storing the Dictionary

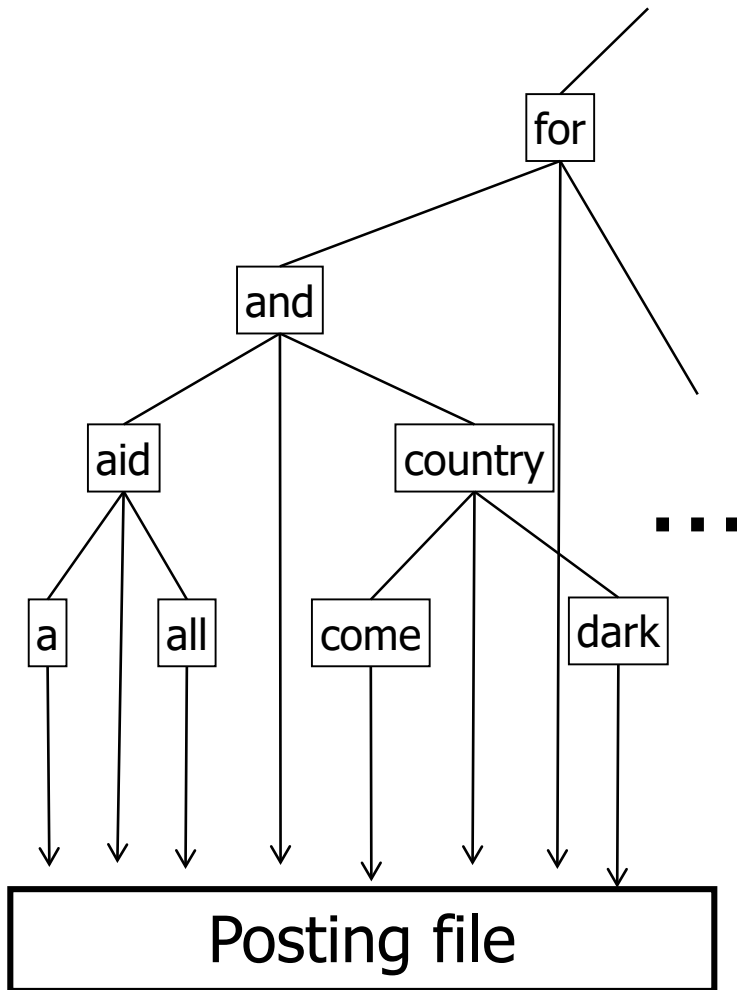
- Dictionary are always kept in main memory
- Suitable **data structures**?
 - Sorted term array: Small and fast (binsearch), static
 - Balanced binary (AVL) tree: Larger and fast, dynamic
 - Hashing: Either small and slow or large and very fast
 - (Compressed) Prefix-tree: **Much larger and very fast**
- In the following
 - Assume $|ptr|=|DF|=4$; $|K|=1M$
 - Let $|q|$ be total length of query in characters
 - Usually small; used as upper bound on the number of char comparisons
 - Let $n=8*|K|=8M$ be the sum of lengths of all terms in dictionary
 - Assuming average word length = 8

Dictionary as Sorted Array

- Elements: $\langle \text{term}, \text{DF}, \text{ptr} \rangle$
- Since terms have different lengths:
Implementation will be $(\text{ptr1}, \text{DF}, \text{ptr2})$
 - ptr1: To string (the keyword)
 - ptr2: To posting list
- Search: Compute $\log(|K|)$ memory addresses, follow ptr1, compare strings:
 $O(\log(|K|) * |q|)$
- Construction: $O(|K| * \log(|K|))$
 - Sorting K
- Space: $(4+4+4) * 1M + n \sim 20M$ bytes
- But: Adding new terms is painful

Term	DF	
a	1	ptr
aid	1	ptr
all	1	ptr
and	1	ptr
come	1	ptr
country	2	ptr
dark	1	ptr
for	1	ptr
good	1	ptr
in	1	ptr
is	1	ptr
it	1	ptr
manor	1	ptr
men	1	ptr
midnight	1	ptr
night	1	ptr
now	1	ptr

Dictionary as AVL Tree



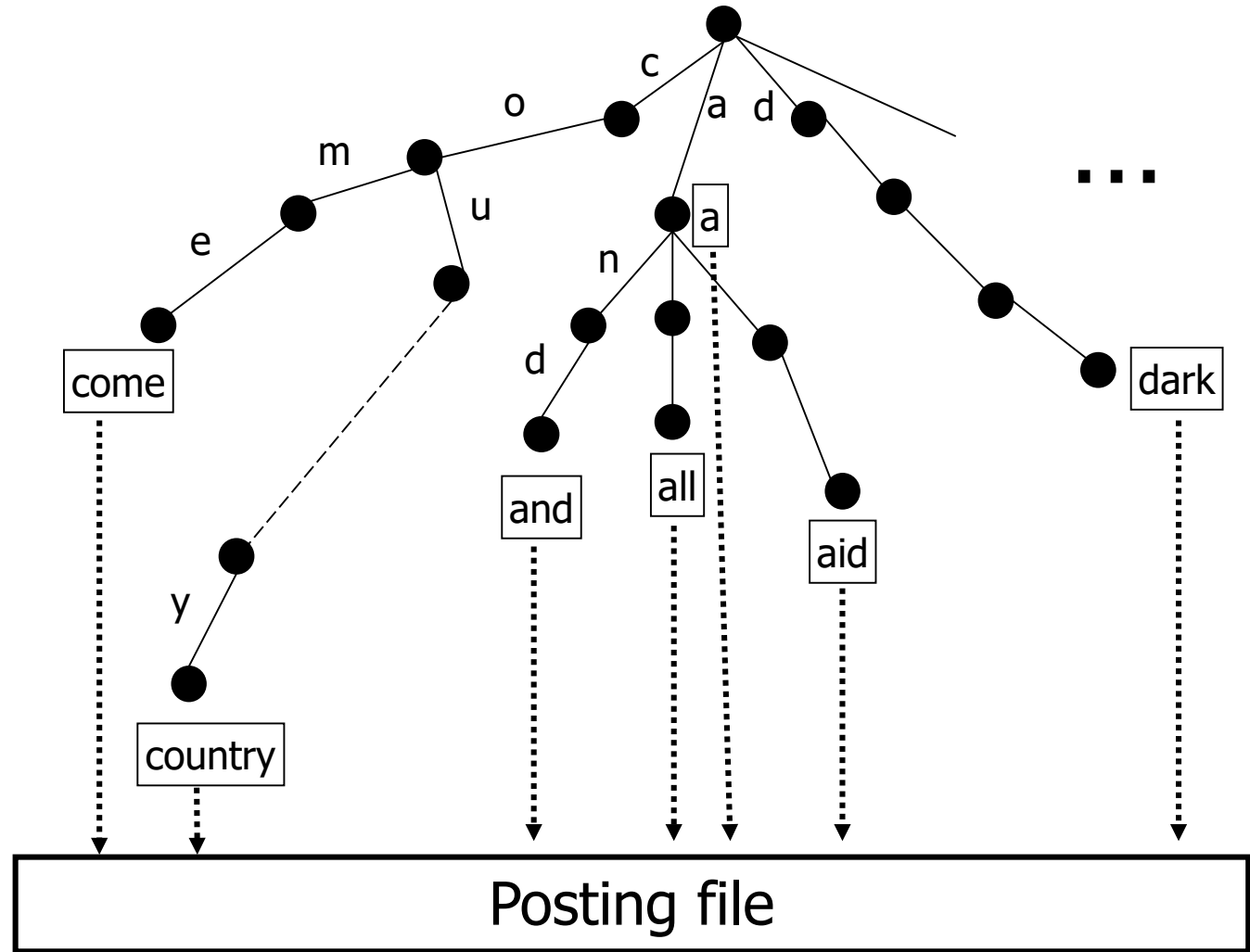
- Internal node:
(ptr1, ptr2, ptr3, ptr4, DF)
 - String, posting, child1, child2
- Leaf: (ptr1, ptr2, DF)
- Search: Follow pointer, compare strings: $O(\log(|K|) * |q|)$
- Construction: $O(|K| * \log(|K|))$
- Space
 - Internal: $0.5M * (4+4+4+4+4)$
 - Leaves: $0.5M * (4+4+4)$
 - Together: $16M+n \sim 24MB$
- Adding terms is simple

Dictionary as Hash Table

- Idea: Hash keywords into a hash table T (with overflow)
 - Value is $\langle \text{ptr-to-posting-list}, \text{DF} \rangle$
- In principle, $O(1)$ access is possible ...
 - Construction: $O(|K|)$
 - Search time: $O(|q|)$
 - $O(1)$ key comparisons, typical STRING hash functions look at all chars
 - Space: Difficult
 - Depends on $\text{size of hash table}$ and implementation of overflow chains
- Only if $\text{collision are rare}$ is used
 - Which requires that T is much larger than $|K|$
- Adding terms is simple (if collisions are rare)

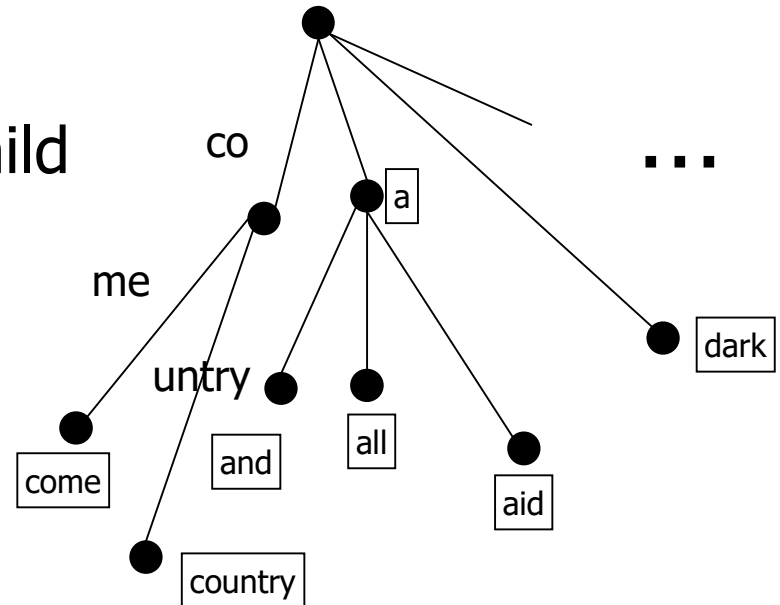
Dictionary as Prefix Tree (TRIE: Information ReTRIEval)

Term	IDF
a	1
aid	1
all	1
and	1
come	1
country	2
dark	1
for	1
good	1
in	1
is	1
it	1
manor	1
men	1
midnight	1
night	1
now	1



Compressed Tries (Patricia Trees)

- Remove nodes with only one child
- Label **edges with substrings**, not single characters
- Saves space and pointers
- **Search: $O(|q|)$**
 - Maximally $|q|$ char-comps + max $|q|$ ptr to follow
 - Assumes **$O(1)$ for decision on child-pointer** within each node
- Construction: $O(n)$
- Adding terms: Simple (search and insert new nodes)
- Space ...



Space of a Trie

- Space: **Difficult to estimate**
- Assume 4 full levels, then each last inner node having two different suffixes (1M leaves, alphabet size 26)
 - 26 nodes in 1st, $26^2 \sim 700$ in 2nd, $26^3 \sim 17.000$ in 3rd, $26^4 \sim 450K$ in 4th
 - Assume each incoming edge stores only 1 character
 - Nodes in first 3 levels store 26 pointer, nodes in 4th **only two**
 - Beware: **No $O(|q|)$ search** any more
- Inner: $(26+700+17K) \cdot (26 \cdot \text{ptr} + 1) + 450K \cdot (2 \cdot \text{ptr} + 1) \sim 6M$
- Leaves: $|K| \cdot (\text{string-ptr, posting-ptr, DF}) + (n - |K| \cdot 4) \sim 16M$
 - We only need to store a suffix of each term, prefix is in tree
- Together: **$\sim 22M$**
 - But assumptions are optimistic (Four full levels, equal-length terms)
 - Prefix trees are typically **very space-consuming**

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Storing the Posting File

- Posting file is usually kept on disk
- Suggestions?

Storing the Posting File

- Posting file kept on disk
- Static
 - Store posting lists **one after the** other in large file
 - Posting-ptr is offset in this file
- Less static: Prepare for inserts
 - Reserve **additional space per posting**
 - Good idea: Large initial posting lists get some extra space
 - Many inserts can be handled internally
 - Upon **overflow**, append entire posting list at the end of the file
 - Place **pointer at old position** – at most two access per posting list
 - Or update pointer in dictionary – better if only one copy around
 - Generates unused space (holes) – regular **reorganization**
 - Reorganization requires updating all pointers in the dictionary

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Positional Information

- What if we **search for phrases**: "Bill Clinton", "Ulf Leser"
 - ~10% of web searches are phrase queries
- What if we search by proximity "car AND rent/5"
 - "We rent cars", "cars for rent", "special care rent", "if you want to rent a car, click here", "Cars and motorcycles for rent", ...
- We need **positional information**

Doc1:
Now is the time
for all good men
to come to the aid
of their country.

... a dark and
stormy night in
the country
manor. The time
was past midnight.

Term	Doc #	Doc #	TF	Pos
		2	1	6
a	1	1	1	1
aid	1	1	1	14
all	1	2	1	15
and	1	1	1	6
come	1	1	1	16
country	2	2	1	10
...	...	1	1	15
the	2	1
their	1	1	2	3,12
time	2	2	2	9,12
...

Answering Phrase Queries

- Search posting lists of all query terms
- Boolean: During intersection, also **positions must fit**
 - If $q = "k_1 k_2"$ and $(d, tf_1, \langle P_1 \rangle) \in \text{post}(k_1)$ and $(d, tf_2, \langle P_2 \rangle) \in \text{post}(k_2)$
 - I.e.: d contains k_1 in positions $\langle P_1 \rangle$ and k_2 in positions $\langle P_2 \rangle$
 - Find all pairs p_1, p_2 with $p_1 \in P_1$ and $p_2 \in P_2$ and $p_1 + 1 = p_2$
 - For longer phrases, e.g. $q = "k_1 k_2 k_3 \dots"$, maintain a list P with all positions that are the end of a prefix of q
- VSM: More complicated (details skipped)

Effects

- Dictionary is not affected
- Posting lists get **much larger**
 - Store (docID, TF, <pos>) instead of (docID,TF)
 - Positional index typically **30-50% larger** than the corpus itself
 - Especially **frequent words** create excessively long positing lists
- One trick: **Compression** of docIDs (delta encoding)
 - In large corpora, docID is a large integer
 - Trick: Store **length of gaps** instead of docID
 - t1: 17654,3,17655,12,17862,8,17880,4,17884,9, ...
 - t1: 17654,3,1,12,207,8,18,4,4,9, ...
 - In contrast, positions are small ints – no compression

Encoding

- Only pays off if we need **few bits for small numbers** but still have many bits for large numbers
- **Variable-byte encoding**
 - Always use at least 1 byte
 - Reserve first bit as “continuation bit” (cb) and 7 bit as payload
 - If cb=1, also use payload of next byte
 - t1: 17654, 3, 1, ..., 12, 207, ..., 8, ...
 - t1: 17654, 3, 00000001, 12, 11001111 | 00000001, 8, ...
 - **Simple**, small numbers not encoded optimally
- γ (gamma) codes (details skipped)
 - Always use **minimal number** of bits for value
 - Encode length in unary encoding

Bi-Gram Index

- Alternative for phrase queries: **Index over bi-grams**
 - „The fat cat ate a rat“ – „the fat“, „fat cat“, „cat ate“, ...
- Phrase query with $|q|$ keywords gets translated into $|q|-1$ lookups
- Done?

Bi-Gram Index

- Alternative for phrase queries: Index over bi-grams
 - „The fat cat ate a rat“ – „the fat“, „fat cat“, „cat ate“, ...
- Phrase query with $|q|$ keywords gets translated into $|q|-1$ lookups
- Done?
 - Bi-gram need not appear sequentially in the doc
 - Need to **confirm match** after loading the doc
- Advantage
 - **Very high selectivity** of each bi-grams query leads to few confirmations
- Disadvantage: **Very large dictionary**

Proximity Search

- Phrase search = **proximity search** with distance one
- Proximity search
 - Search doc-lists with positional information for each term
 - Boolean: Upon intersection, check all pairs of positions
 - Can get quite involved for multi-term queries
 - “car AND rent/5 AND cheap/2 AND toyota/20” – “cheap” between 1 and 7 words from “car”, “toyota” between 1 and 22 words from rent ...
 - **All conditions** must be satisfied

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Building an Inverted File

- Assume a very large corpus: Billions of documents
 - We still assume that dictionary fits in memory
- How can we efficiently build the index?

Blocked, Sort-Based Indexing

- Partition corpus in **blocks fitting into memory**
- Algorithm
 - Keep dictionary always in memory
 - For each block: Load, create postings, **flash to disk**
 - **Merge** all posting lists
 - Open all at once
 - Skip through all posting lists **term-by-term** in sort-order
 - Merge doc-lists of equal keywords and flash to disk
 - If doc-lists are very large, we need special means here
- Requires **2 reads and 2 writes** of all data
 - If there are enough file handles to open all posting lists at once

Updating an index: INSERT d_{new}

- What has to be done?
 - Foreach $k_i \in d_{\text{new}}$
 - Search k_i in dictionary
 - If present
 - Follow [pointer to posting file](#)
 - Add d_{new} to posting list of k_i
 - If list [overflows](#), move posting list to end of file and place pointer
 - If not present
 - Insert k_i into dictionary
 - Add new posting list $\{d_{\text{new}}\}$ at end of posting file
- Disadvantage
 - Degradation: Many pointers in file, many terms [require 2 IO](#)
 - Especially the frequent ones
 - [Index partly locked](#) during updates

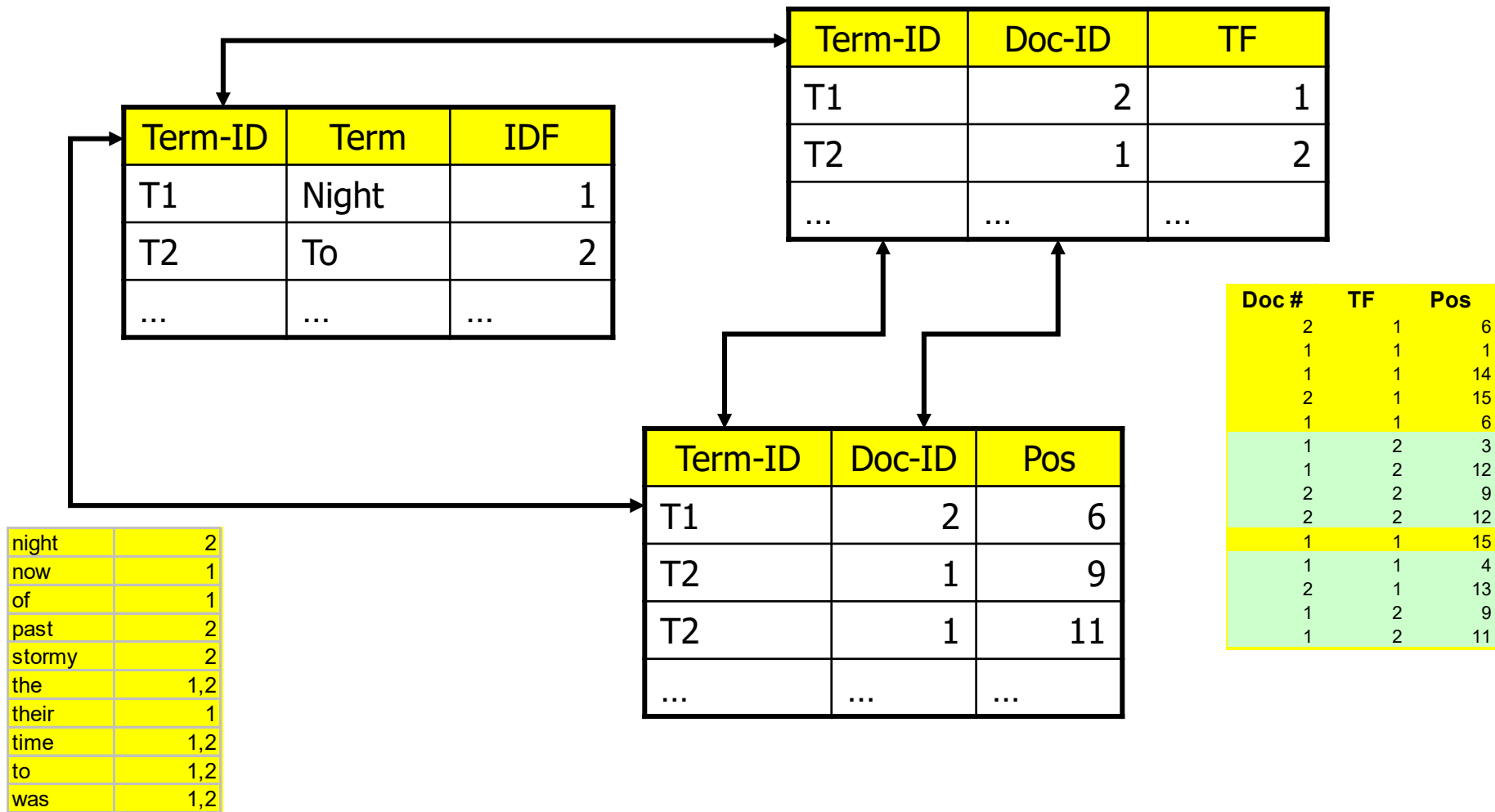
Using Auxiliary Indexes

- All inserts are performed on a **second, auxiliary index**
 - Keep it small: Always in memory
- Searches need to search **real and auxiliary** index
- When aux index grows too large, merge into real index
 - Try to append in-file: Same problem with degradation
 - Or read both indexes and write a **new “fresh” index**
 - In both cases, the index is locked
 - Solution: Work on a copy, then switch file pointers
- Alternative: Ignore new docs during search and periodically rebuild index on all docs

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Implementing an Inverted File using a RDBMS



Example Query 1

- Boolean: All docs containing terms "night" and "to"

```
- SELECT D1.docid
   FROM terms T1, terms T2, termdoc D1, termdoc D2
   WHERE T1.term='night' AND T2.term='to' AND
         D1.termid=T1.termid AND
         D2.termid=T2.termid AND
         D1.docid = D2.docid;
```

terms		
Term-ID	Term	IDF
T1	Night	1
T2	To	2

pos		
Term-ID	Doc-ID	Pos
T1	2	6
T2	1	9
T2	1	11

termdoc		
Term-ID	Doc-ID	TF
T1	2	1
T2	1	2
...

Example Query 2

- VSM queries
 - We need to compute the inner product of two vectors
 - We ignore normalization
 - We assume TF-values of query terms are 1, others are 0
 - It suffices to **aggregate TF values of matching terms** per doc
- Example: Compute score for “night rider” (two terms)

```
- SELECT did, sum(tf)
  FROM (   SELECT D.docid did, T.term term, tf
           FROM terms T, termdoc D
           WHERE T.term='night' AND D.termid=T.termid)
        UNION
        SELECT D.docid did, T.term term, tf
           FROM terms T, termdoc D
           WHERE T.term='rider' AND D.termid=T.termid) docs
 GROUP BY did;
```

Access Methods in a RDBMS

- Use B*-Indices on ID columns
- Searching a term
 - Requires $O(\log(|K|))$ random-access IO
 - Mind the base of the logarithm: Block size
 - For <100M terms, this usually means <3 IO (cache!)
 - Accessing the posting list: $O(\log(n))$ quasi-random-access IO
 - Where n is the number of term occurrences in D
 - Access is a lookup with term-ID, then seq. scan along the B*-leaves
 - Compared to IR: Dictionary in memory, posting is accessed by direct link, then only sequential IO
- Advantages: Simple, easy to build
- Disadvantages: **Much slower**
 - More IO, general RDBMS overhead, space overhead for keys, ...

Self Assessment

- Explain idea and structure of inverted files?
- What are possible data structures for the dictionary?
Advantages / disadvantages?
- How can posting lists be managed?
- How much bigger is an inverted file with positions than without?
- How can one efficiently build a large inverted file from scratch?