

Algorithms and Data Structures



Who am I

- Ulf Leser
- 1995 Diploma in Computer Science, TU München
- 1996-1997 Database developer at MPI-Molecular Genetics
- 1997-2000 Dissertation in Database Integration, TU Berlin
- 2000-2003 Developer and project manager at PSI AG
- 2003- Prof. Knowledge Management in Bioinformatics
- I do answer emails

- Our topics in research
 - Scientific Databases
 - Text Mining
 - Scientific Data Analysis
- Our topics in teaching
 - Bsc: Grundlagen der Bioinformatik
 - Bsc: Information Retrieval
 - Msc: Algorithmische Bioinformatik
 - Msc: Data Warehousing und Data Mining
 - Msc: Informationsintegration
 - Msc Maschinelle Sprachverarbeitung

- IT company A develops software for insurance company B

 Volume: ~4M Euros
- B not happy with delivered system; doesn't want to pay
- A and B call a referee to decide whether requirements were fulfilled or not

– Volume: ~500K Euros

 Job of referee is to understand requirements (~60 pages) and specification (~300 pages), survey software and manuals, judge whether the contract was fulfilled or not

One Issue

This is hardly testable

Requirement: "Allows for smooth operations in daily routine"

One Issue

- Requirement: "Allows for smooth operations in daily routine"
- Claim from B
 - I search a specific contract
 - I select a region and a contract type
 - I get a list of all contracts sorted by name in a drop-down box
 - This sometimes takes minutes! A simple dropdown box! This performance is inacceptable for our call centre!

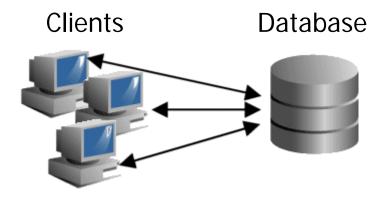


Discussion

- A: We tried and it worked fined
- B: OK, most of the times it works fine, but sometimes it is too slow
- A: We cannot reproduce the error; please be more specific in what you are doing before the problem occurs
- B: Come on, you cannot expect I log all my clicks and take notes on what is happening
- A: Then we conclude that there is no error
- B: Of course there is an error
- A: Please pay as there is no reproducible error

A Closer Look

• System has classical two-tier architecture



- Upon selecting a region and a contract, a query is constructed and send to the database
- Procedure for "query construction" is used a lot
 - All contracts in a region, ... running out this year, ... by first letter of customer, ... sum of all contract revenues per year, ...
 - "Meta" coding: very complex, hard to understand

```
SELECT CU.name, CO.type, CO.start, CO.end, CO.volume, ...
FROM customer CU, contracts CO, c_c CC, region R, ...
WHERE CU.ID=CC.CU_ID AND
CO.ID=CC.CO_ID AND
CU.regionID = R.ID AND
...
CU.ID=4711 AND CO.type="Hausrat"
```

```
SELECT CU.name, CU.street, CU.status, CU.contact, ...
FROM customer CU, contracts CO, c_c CC, region R, ...
WHERE CU.ID=CC.CU_ID AND
CO.ID=CC.CO_ID AND
CU.regionID = R.ID AND
...
R="Berlin"AND CO.type="Leben"
```

Requirement



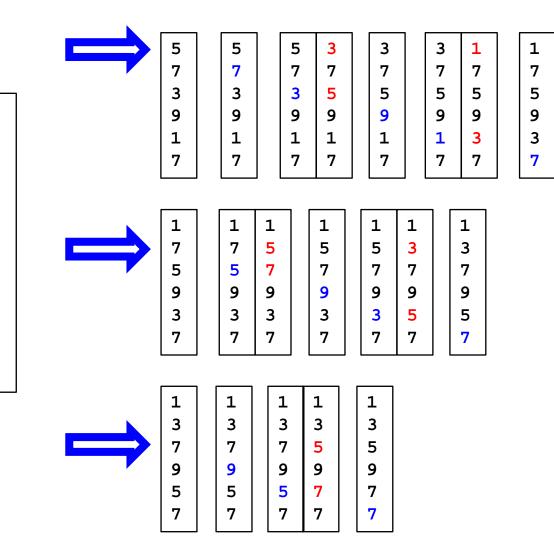
• After retrieving the list of customers, it has to be sorted

```
S: array_of_names;
n := |S|;
for i = 1..n-1 do
  for j = i+1..n do
    if S[i]>S[j] then
      tmp := S[i];
      S[i] := S[j];
      S[j] := tmp;
    end if;
end for;
end for;
```

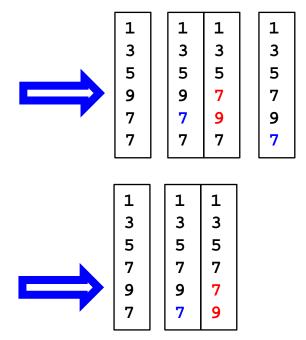
- S: array of Strings, |S|=n
- Sort S alphabetically
 - Take the first string and compare to all others
 - Swap whenever a later string is alphabetically smaller
 - Repeat for 2nd, 3rd, ... string
 - After 1st iteration of outer loop:
 S[1] contains smallest string from S
 - After 2nd iteration of outer loop: S[2] contains 2nd smallest string from S
 - etc.

Example

```
S: array_of_names;
n := |S|;
for i = 1..n-1 do
  for j = i+1..n do
    if S[i]>S[j] then
      tmp := S[i];
      S[i] := S[j];
      S[j] := tmp;
    end if;
    end for;
end for;
```



Example continued



- Seems to work
- This algorithm is called "selection sort"
 - Select smallest element and move to front, select second-smallest and move to 2nd position, ...

Analysis

- How long will it take (depending on n)?
- Which parts of the program take CPU time?
 - 1. Very little, constant time
 - 2. Probably very little, constant time
 - 3. n-1 assignments
 - 4. n-i assignments
 - 5. One comparison
 - 6. One assignment
 - 7. One assignment
 - 8. One assignment
 - 9. No time
 - 10. One increment (j+1); one test

11. One increment (i+1); one test

```
1. S: array_of_names;
2. n := |S|;
3. for i = 1...-1 do
4.
   for j = i+1..n do
5.
       if S[i]>S[j] then
6.
         tmp := S[i];
7.
         S[i] := S[j];
8.
         S[j] := tmp;
9. end if;
     end for;
10.
11. end for;
```

Slightly More Abstract

- Assume one assignment/test costs c, one addition d
- Which parts of the program take time?
 - 1. 0
 - 2. c
 - 3. (n-1)*c
 - 4. (n-i)*c (hmmm ...)
 - 5. c
 - 6. c (hmmm ...) 7. c 8. c 9. 0 10. c+d
 - 11. c+d

```
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2. n := |S|;
3. for i = 1...-1 do
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      if S[i]>S[j] then
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    end for;
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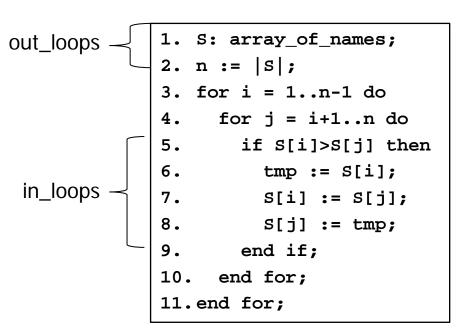
- Assume one assignment/test costs c, one addition d
- Which parts of the program take time?
 - Let's be pessimistic: We always swap
 - How would the list have to look like in first place?
 - C
 - (p=r)*C* (• n-i* (
 - c+d) +
 - c+d)

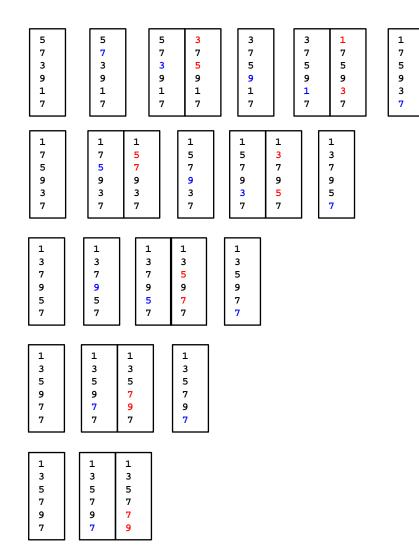
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       end if;
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```

This is not yet clear

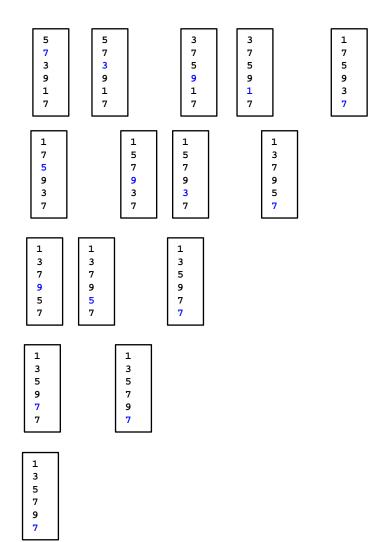
Even More Compact

- Assume one assignment/test costs c, one addition d
- Which parts of the program take time?
 - We have some cost outside the loops (out_loops)
 - And some cost inside the loops (in_loops)
 - How often do we need to perform in_loops?
 - Total: c+(n-1)*c* ((n-i)*...)= out_loops+(n-1)*c*?*in_loops

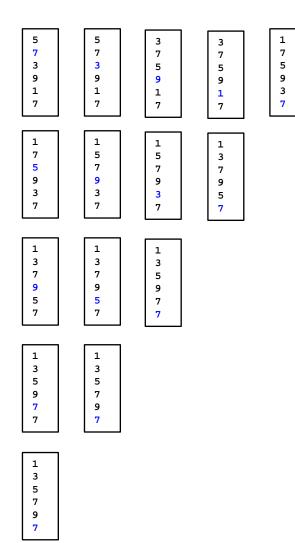




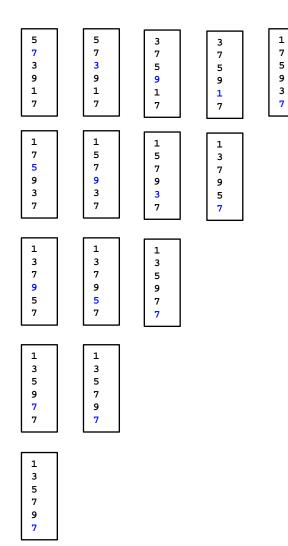
- The number of comparisons is independent of the number of swaps
 - We always compare, but we do not always swap



- The number of comparisons is independent of the number of swaps
 - We always compare, but we do not always swap
- How many comparisons do we perform in total?



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 - We always compare, but we do not always swap
- How many comparisons do we perform in total?



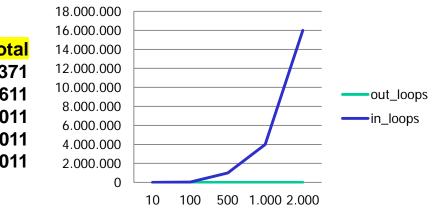
- First string is compared to n-1 other strings
 - First row
- Second is compared to n-2
 - Second row
- Third is compared to n-3

• ...

• n-1'th is compared to 1

$$(n-1) + (n-2) + (n-3) + \ldots + 1 = \sum_{i=1}^{n-1} i = \frac{n(n-1)}{2} = \frac{n^2}{2} - \frac{n}{2}$$

- This leads to the following estimation for the total cost out_loops+(n²-n)*in_loops/2
- Let's assume c=d=1



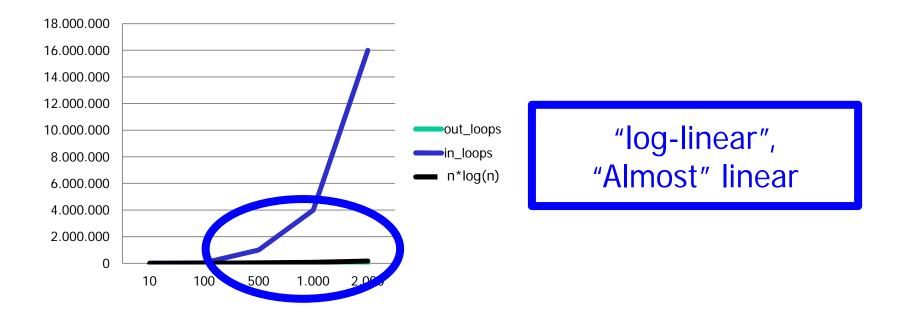
$n+1+(n^2-n)*8/2$

	out_loops	in_loops	total
10	11	360	371
100	11	39.600	39.611
500	11	998.000	998.011
1.000	11	3.996.000	3.996.011
2.000	11	15.992.000	15.992.011

- Most combinations (region, contract type) select only a handful of contracts
- A few combinations select many contracts (2000-5000)
- Time it takes to fill the drop-down list is not proportional to the number of contracts (n), but proportional to n²/2
 - Required time is "quadratic in n"
 - Assume one operation takes 10 nanoseconds (0.000001 sec)
 - A handful of contracts (~10): ~500 operations => 0,0005 sec
 - Many contracts (~5000) => ~125M operations => 125 sec
 - Humans always expect linear time ...
- Question: Could they have done it better?

Of course

- Efficient sorting algorithms need ~n*log(n)*x operations
 - Quick sort, merge sort, ... see later
 - For comparability, let's assume x=8



So there is an End to Research in Sorting?

- We didn't consider how long it takes to compare 2 strings
 - We used c=d=1, but we need to compare strings char-by-char
 - Time of every comparison is proportional to the length of the shorter string
- We want algorithms requiring less operations per inner loop (smaller x)
- We want algorithms that are fast even if we want to sort 1.000.000.000 strings
 - Which might not fit into main memory
- We made a pessimistic estimate what is a realistic estimate (how often do we swap in the inner loop?)?

Terasort Benchmark

- 2009: 100 TB in 173 minutes
 - Amounts to 0.578 TB/min
 - 3452 nodes x (2 Quadcore, 8 GB memory)
 - Owen O'Malley and Arun Murthy, Yahoo Inc.
- 2010: 1,000,000,000,000 records in 10,318 seconds
 - Amounts to 0.582 TB/min
 - 47 nodes x (2 Quadcore, 24 GB memory), Nexus 5020 switch
 - Rasmussen, Mysore, Madhyastha, Conley, Porter, Vahdat, Pucher
- Other goals
 - PennySort: Amount of data sorted for a penny's worth of system time
 - JouleSort: Minimize amount of energy required during sorting

- This lecture
- Algorithms and ...
- Data Structures
- Concluding Remarks

- Slides are English
- Vorlesung wird auf Deutsch gehalten
- Lecture: 4 SWS; exercises 2 SWS
- Contact
 - Ulf Leser,
 - Raum IV.401
 - Tel: 2093 3902
 - eMail: leser (..) informatik . hu...berlin . de

- Lectures: Monday 11-13, Wednesday 11-13, EZ 0115
- Exercises: See webpages / AGNES

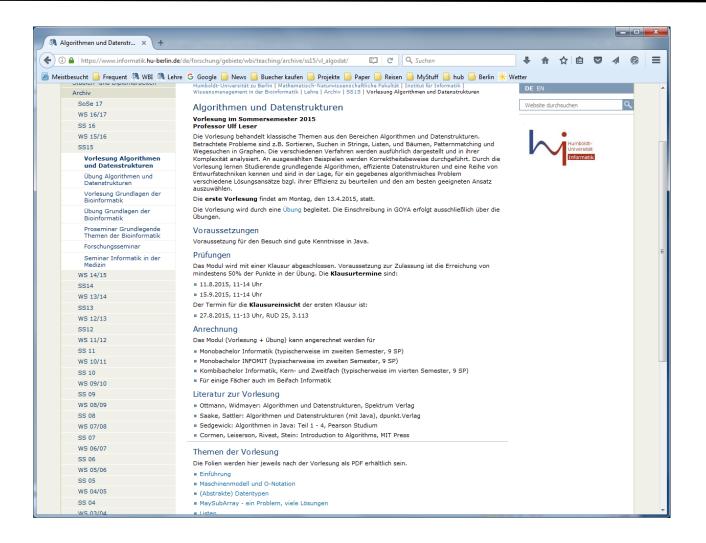
Exercises

- Start only next week
- You will build teams of two students
- There will be an assignment about every two weeks
- You need to work on every assignment
- Each assignment gives 40 points max
- Only groups having >50% of the maximal number of points over the entire semester are admitted to the exam
- For every assignment and slot, 2-3 students are selected at random and must present their solution
- Failing to do so more than two times implies exclusion from exercise

Literature

- Ottmann, Widmayer: Algorithmen und Datenstrukturen, Spektrum Verlag, 2002-2012
 - 20 copies in library
- Other
 - Saake / Sattler: Algorithmen und Datenstrukturen (mit Java), dpunkt.Verlag, 2006
 - Sedgewick: Algorithmen in Java: Teil 1 4, Pearson Studium, 2003
 - 20 copies in library
 - Güting, Dieker: Datenstrukturen und Algorithmen, Teubner, 2004
 - Cormen, Leiserson, Rivest, Stein: Introduction to Algorithms, MIT Press, 2003
 - 10 copies in library

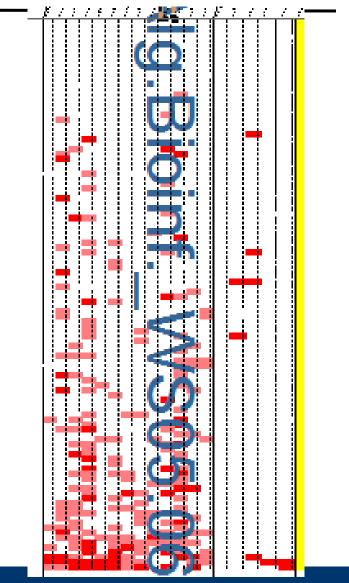
Web



- You need to program exercises in Java
- I will use informal pseudo code
 - Much more concise than Java
 - Goal: You should understand what I mean
 - Syntax is not important; don't try to execute programs from slides
- Translation into Java should be simple

•	Machine models and complexity (~2)	April
•	Abstract data types (~2)	Артп
•	Lists (~3)	
•	Sorting (~5)	Mai
•	Selection (~3)	
•	Hashing (~3)	June
•	Trees (~4)	
•	Graphs (~4)	July

- Very good scores
- Materials could (always) be better
- Discerning BA, KB, INFOMIT impossible
- Many liked it a lot, a few strongly disliked it



Freitexthinweise

Gut·gefallen¤	Nicht·gefallen¤	Zu·wenig¤	Zu·viel¤	Sonstiges¤
 → 21·Beispiele·(Praxis)¶ 	• → 4·Zu·langsam¶	• → 4·Formaler·machen¶	• → 11·Hochschulpolitik¶	• → Mikro·leiser¶
• → 15·Stil¶	 → 11·Englische·Folien¶ 	 → Englisch·vortragen¶ 	• → 4·Bioinformatik¶	● → Mehr·Praxis¶
 → 15·Sehr·gut·erklärt¶ 	• → Struktur•manchmal•	 → 7·Alg·der·Woche¶ 	 → Verschiedene · Fak· 	• → Alg·der·Woche·erfordern·zu·viel·
• → 5·Gute·Struktur¶	unklar¶	• → 2·Programmierung¶	beim∙Verfolgen∙der∙	Vorwissen¶
 → Möglichkeit·für·Fragen¶ 	• → Manche·Themen·zu·	• → 4·Beweise¶	VL·(?)¶	 → Licht·für·Tafel¶
 → Abstimmung·VL····UE¶ 	kurz¶	 → Hochschulpolitik¶ 	 → Zu·viel·*·in·UE¶ 	 → Schwierige-Themen-einfacher-
 → 3·Engagement·für· 	• → 3·Husten·und·räuspern¶	● → Lambda-Notation zu	 → Zu-wenig-echtes- 	darstellen¶
Verständnis¶	• → Hinweis·auf·"nur·	schnell¶	Interesse an Bildung¶	 → 3·Folien·verbessern·(überladen)¶
 → 12·Alg·der·Woche¶ 	Grundlagen"¶	 → Interaktion·und·Tafel¶ 	• → 2·Übungen¶	 → Team·der·Übungen·super¶
 → 11·Hochschulpolitik¶ 	 → Terminkollision¶ 	 → Zusatzliteratur¶ 	• → Sehr·zeitaufwändig¶	• → Quiz·in·letzten·10m¶
• → 3·Tempo¶	• → Mathematische·	• → Motivierende	 → AlgdWoche 	• → Schlechte·Luft¶
 → 2·Zweiwöchige·Übung ¶ 	Wüsten¶	Erklärungen¶	weglassen¶	 → Folien·nicht·doppelt·zeigen¶
• → 2·Folien¶	 → Grüner-Laserpointer¶ 	• → 2·Beispiele¶	• → 2·Fehler·in·Folien¶	• → Gesellschaftlich·relevante·Dinge·
 → 2·Englische·Folien¶ 	• → Langsamer·sprechen¶	• → Mehr·Tafel·benutzen¤	 → Sehr·lange·Beispiele¶ 	besprechen, nicht nur Uni-
• → Übung¶	• → Zu·viel·Text¶		 → Komplexitätsanalysen¤ 	Politik¶
 → Themenvielfalt¶ 	• → Amortisierte Analyse			 → Mehr·Ersatzbatterien¶
• → 3·Einleitende·Wdhs¶	raus¶			 → Variablen·in·Pseudo-Code· bei·
• → Verbindungen·zu·anderen·	• → 2·Folien·kein·Script¶			<u>Wdh</u> •unklar¶
Themen¶	• → Uni-Politik•zu•			 → 2·Niemand-schläft-ein¶
• → 2·Pünktlichkeit¶	reißerisch·und·			 → Pseudo-Code· besser·erklären¶
• → Wenig·Vertretung¶	einseitig¶			 → Mehr·Zeit·bei·komplexen·
 → Sehr·nützliche·Inhalte¶ 	• → 3·Mikro-Einstellung¶			Themen¶
• → 2·Es·wurde·diskutiert¶	• → VL-Zeit·nicht·voll·			 → Mute-Knopf·benutzen¶
• → Schnelle·Korrekturen·der·	ausgenutzt¶			• → Lieber wöchentliche Übungen¶
Folien¶	● → Manchmal·			 → Folien vorab online stellen¶
	-tolat 2.6- one-l@			

- Danke f
 ür MERGESORT, half beim Sortieren von Blument
 öpfen in der G
 ärtnerei meiner Oma
- Prof. Leser ist vertrauenswürdig. Wenn er sagt, dass etwas stimmt, glaube ich es auch ohne Beweis. Beweise weglassen und Zeit sinnvoller nutzen

- Hochschulpolitik: 12 gut, 11 schlecht
- Alg der Woche: 19 gut, 1 schlecht
- Englische Folien: 2 gut, 11 schlecht
- Tempo: 3 gut, 4 zu langsam, 6 zu schnell
- Formale Beweise: 8 bitte formaler, 7 bitte weniger formal

Questions?



- Diplominformatiker?
- Bachelor?
- Semester?
- Kombibachelor?
- INFOMIT? Biophysics? Beifach?
- Who heard this course before?
- No Nebenhörer ☺

- This lecture
- Algorithms and ...
- Data Structures
- Concluding Remarks

- An algorithm is a recipe for doing something
 - Washing a car, sorting a set of strings, preparing a pancake, employing a student, ...
- The recipe is given in a (formal, clearly defined) language
- The recipe consists of atomic steps
 - Someone (the machine) must know what to do
- The recipe must be precise
 - After every step, it is unambiguously decidable what to do next
 - Does not imply that every run has the same sequence of steps
 - There can be randomized steps
- The recipe must not be infinitely long

- Definition (general) An algorithm is a precise and finite description of a process consisting of elementary steps.
- Definition (Computer Science) An algorithm is a precise and finite description of a process that is (a) given in a formal language and (b) consists of elementary and machine-executable steps.
- Usually we also want: "and (c) solves a given problem"
 - But algorithms can be wrong ...

- Rezept
- Ausführungsvorschrift
- Prozessbeschreibung
- Verwaltungsanweisung
- Regelwerk
- Bedienungsanleitung
 - Well ...
- ...

- Word presumably dates back to "Muhammed ibn Musa abu Djafar alChoresmi",
 - Published a book on calculating in the 8th century in Persia
 - See Wikipedia for details
- Given the general meaning of the term, there have been algorithms since ever
 - "To hunt a mammoth, you should ..."
- One of the first prominent one in math: Euclidian algorithm for finding the greatest common divisor (gcd) of two ints
 - Assume $a,b\geq 0$; define gcd(a,0)=a

- Recipe: Given two integers a, b. As long as neither a nor b is 0, take the smaller of both and subtract it from the greater. If this yields 0, return the other number
- Example: (28, 92)
 - (28, 64)
 - (28, 36)
 - (28, 8)
 - (20, 8)
 - (12, 8)
 - -(4, 8)-(4, 4) -(4, 0)

- 1. a,b: integer; 2. if a=0 return b; 3. while b≠0 4. if a>b 5. a := a-b; 6. else 7. b := b-a; 8. end if; 9. end while; 10.return a;
- Will this always work?

Proof (sketch) that an Algorithm is Correct

1.	<pre>func euclid(a,b: int)</pre>		
2.	if a=0 return b;		
3.	while b≠0		
4.	if a>b		
5.	a := a-b;		
6.	else		
7.	b := b-a;		
8.	end if;		
9.	end while;		
10.	. return a;		
11.end func;			
L			

- Assume our function "euclid" returns x
- We write "b|a" if (a mod b)=0
 - We say: "b teilt a"
 - Note: if c|a and c|b and $a > b \Rightarrow c|(a-b)$
 - 1st step: We prove that x is a common divisor of a and b
 - Last step: b=0 and x=a!=0 \Rightarrow x|a, x|b
 - Pre-last: It must hold: $a=b \Rightarrow x|a, x|b$
 - Previous: Either a=2x or $b=2x \Rightarrow x|a, x|b$
 - Previous: Either (a,b)=(3x,x) or (a,b)=(2x,3x) or $... \Rightarrow x|a, x|b$

- func euclid(a,b: int) 1. 2. if a=0 return b; 3. while b≠0 if a>b 4. 5. a := a-b; 6. else b := b-a;7. end if; 8. end while; 9. 10. return a; 11. end func;
- 2nd step: We prove that x is the greatest common divisor
 - Assume any y with y|a and y|b
 - It follows that y (a-b) (or y (b-a))
 - It follows that y|((a-b)-b) (or y|((b-a)-b) ...)
 - It follows that y|x
 - Thus, y≤x

. . .

• Definition

An algorithm is called terminating if it stops after a finite number of steps for every input

Definition

An algorithm is called deterministic if it always performs the same series of steps given the same input

- We only study terminating and mostly deterministic algs
 - Operating systems are "algorithms" that do not terminate
 - Algs which at some point randomly decide about the next step are not deterministic

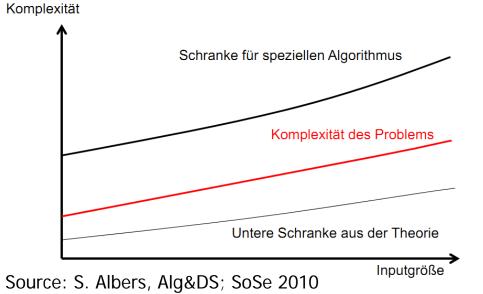
- Usually, one seeks efficient (read for now: fast) algorithms
- We will analyze the efficiency of an algorithm as a function of the size of its input; this is called its (time-)complexity
 - Selection-sort has time-complexity "O(n²)"
- The real runtime of an algorithm on a real machine depends on many additional factors we gracefully ignore
 - Clock rate, processor, programming language, representation of primitive data types, available main memory, cache lines, ...
- But: Complexity in some sense correlates with runtime
 - It should correlate well in most cases, but there may be exceptions
 - Precise definition follows

Algorithms, Complexity and Problems

- An (correct) algorithm solves a given problem
- An algorithm has a certain complexity
 - Which is a statement about the amount of work it will take to finish as a function on the size of its input
- Also problems have complexities
 - The provably minimal amount of work necessary for solving it
 - The complexity of a problem is a lower bound on the complexity of any algorithm that solves it
 - If an algorithm has the same complexity as the problem it solves, it is optimal no algorithm can solve this problem faster
- Proving the complexity of a problem usually is much harder than proving the complexity of an algorithm
 - Needs to make a statement on any algorithm for this problem

Relationships

- There are problems for which we know their complexity, but no optimal algorithm is known
- There are problems for which we do not know the complexity yet more and more efficient algorithms are discovered over time
- There are problems for which we only know lower bounds on their complexity, but not the precise complexity
- There are problems of which we know that no algorithm exists
 - Undecidable problems
 - Example: "Halteproblem"
 - Implies that we cannot check in general if an algorithm is terminating



- 1. Time consumption how long will it take?
 - Time complexity
 - Worst-case, average-case, best-case
- 2. Space consumption how much memory will it need?
 - Space complexity 🧲
 - Worst-case, average-case, best-case
 - Can be decisive for large inputs

Often, one can trade space for time – look at both

3. Correctness – does the algorithm solve the problem?

Formal Analysis versus Empirical Analysis

- We will usually perform a formal complexity analysis of the algorithms we study
 - Goal: Derive a simple formula which helps to compare the principal runtime behavior of different algorithms
 - Should correlate with the true runtime on any machine
 - In some yet-to-be-defined sense
 - However, this doesn't help to decide which of 10 sorting algorithms with complexity O(n*log(n)) are actually the fastest for your setting
 - Machine, nature and amount of data to be sorted, ...
- Alternative: Implement carefully and run on reference machine using reference data set
 - Done a lot in practical algorithm engineering
 - Not so much in this introductory course

- We will mostly focus on worst-case time complexity
 - Best-case is not very interesting
 - Average-case often is hard to determine
 - What is an "average string list"?
 - What is average number of twisted sorts in an arbitrary string list?
 - What is the average length of an arbitrary string?
 - May depend in the semantic of the input (person names, DNA sequences, job descriptions, book titles, language, ...)
- Keep in mind: Worst-case often is overly pessimistic

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- Algorithms and ...
- Data Structures
- Concluding Remarks

- Algorithms work on input data, generate intermediate data, and finally produce result data
- A data structure is a way how data is represented inside the machine
 - In memory or on disc (see Database course)
- Data structures determine what algs may do at what cost
 More precisely: ... what a specific step of an algorithm costs
- Complexity of algs is tightly bound to the data structures they use
 - So tightly that one often subsumes both concepts under the term "algorithm"

Example: Selection Sort (again)

- We assumed that S is
 - a list of strings (abstract), represented
 - as an array (concrete data structure)
- Arrays allow us to access the i'th element with a cost that is independent of i (and |S|)
 - Constant cost, "O(1)"

- 1. S: array of names; 2. n := |S|;3. for i = 1...-1 do 4. for j = i+1..n do 5. if S[i]>S[j] then 6. tmp := S[i];7. S[i] := S[j];8. S[j] := tmp;9. end if; 10. end for; 11. end for;
- Let's use a linked list for storing S
 - Create a class C holding a string and a pointer to an object of C
 - Put first s∈S into first object and point to second object, put second s into second object and point to third object, …
 - Keep a pointer p_0 to the first object

Selection Sort with Linked Lists

- 1. i := p0; 2. repeat 3. i := i.next; 4. repeat 5. if i.val > j.val then 6. tmp := i.val; i.val := j.val; 7. 8. j.val := tmp; 9. end if; j = j.next; 10. 11. unil j.next = null; i := i.next; 12. 13.until i.next.next = null;
- How much do the algorithm's steps cost now?
 - Assume following a pointer costs c
 - 1. One assignment
 - 2. Nothing
 - 3. One assignment, n-1 times
 - 4. Nothing
 - 5. One comparison, ... times

6. ...

- Apparently no change in complexity
 - Why? Only sequential access

- 1. i := p0; 2. repeat 3. i := i.next; 4. repeat 5. if i.val > j.val then 6. tmp := i.val; 7. i.val := j.val; 8. j.val := tmp; 9. end if; 10. j = j.next; 11. unil j.next = null; 12. i := i.next; 13.until i.next.next = null;
- No change in complexity, but
 - Previously, we accessed array elements, performed additions of integers and comparisons of strings, and assigned values to integers
 - Now, we assign pointers, follow pointers, compare strings and follow pointers again
- These differences are not reflected in our "cost model", but may have a big impact in practice

- This lecture
- Algorithms and Data Structures
- Concluding Remarks

- You will learn things you will need a lot through all of your professional life
- Searching, sorting, hashing cannot Java do this for us?
 - Java libraries contain efficient implementations for most of the (basic) problems we will discuss
 - But: Choose the right algorithm / data structure for your problem
 - TreeMap? HashMap? Set? Map? Array? ...
 - "Right" means: Most efficient (space and time) for the expected operations: Many inserts? Many searches? Biased searches? ...
- Few of you will design new algorithms, but all of you often will need to decide which algorithm to use when
- To prevent problems like the ones we have seen earlier

- Give a definition of the concept "algorithm"
- What different types of complexity exist?
- Given the following algorithm ..., analyze its worst-case time complexity
- The following algorithm ... uses a double-linked list as basic set data structure. Replace this with an array
- When do we say an algorithm is optimal for a given problem?
- How does the complexity of an algorithm depend on (a) the data structures it uses and (b) the complexity of the problem it solves?