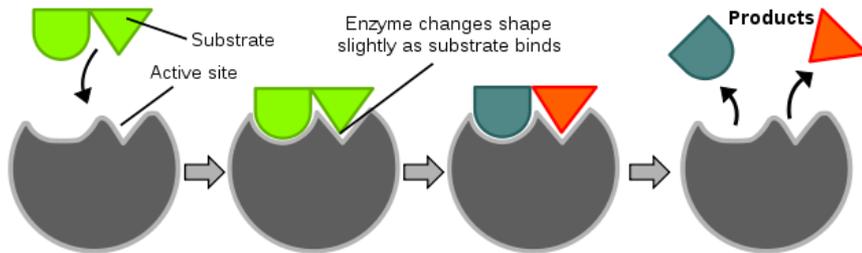


# Protein interaction networks

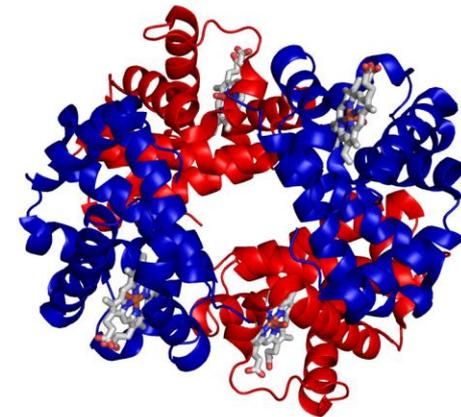
Ulf Leser and Samira Jaeger

# Molecular interactions – Motivation

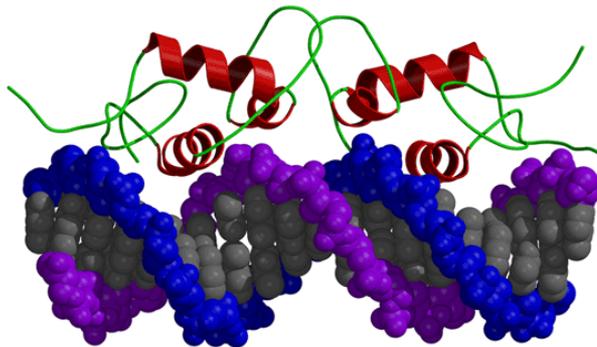
- Proteins mediate their function in complex interplay with other molecules through molecular interactions



Enzymes bind substrates to catalyze biochemical reactions



$\alpha$  and  $\beta$ -hemoglobin chains assemble into hetero-tetramers for transporting oxygen from lungs to tissues



Transcription factors bind the DNA to induce transcription

# Protein-protein interactions – Motivation

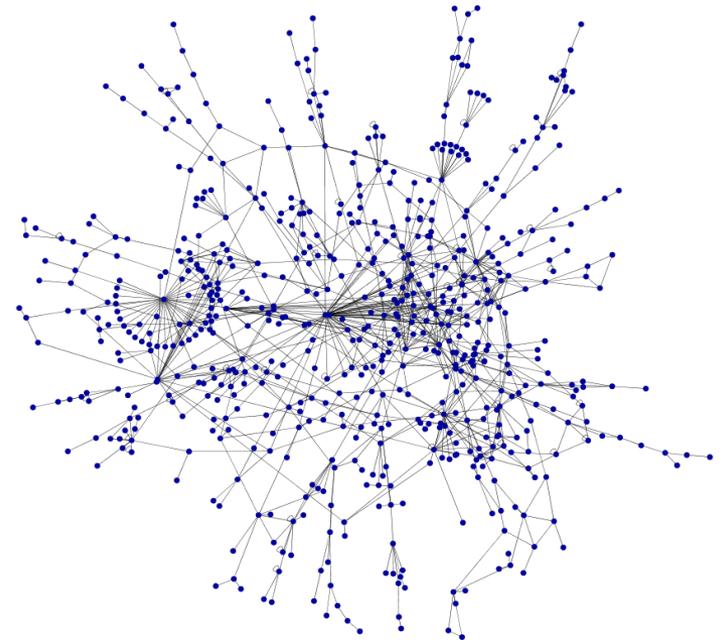
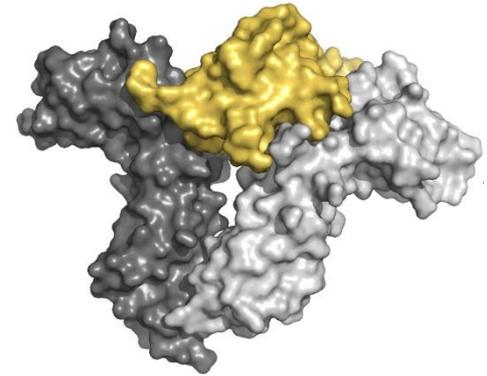
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- Important class of biomolecular interactions are **protein-protein interactions**
- Virtually **all cellular mechanisms rely on the physical binding of two or more proteins** to accomplish a particular task:
  - Critical role in cellular processes, e.g. signal transduction, gene regulation, cell cycle control and metabolism
  - Alterations in protein interactions perturb natural cellular processes and contribute to many diseases, such as cancer and AIDS
- Identifying all physical interactions within an organisms – the **interactome** – essential towards understanding the complex molecular relationships in living systems

# This Lecture

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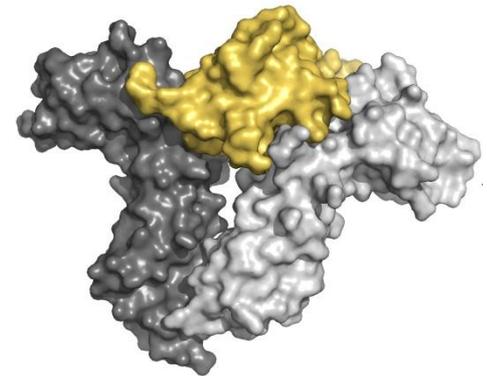
- Protein-protein interactions
  - Characteristics
  - Experimental detection methods
  - Databases
- Protein-protein interaction networks
  - Characteristics
  - Applications
    - Protein function prediction



# Protein-protein interactions – Characteristics

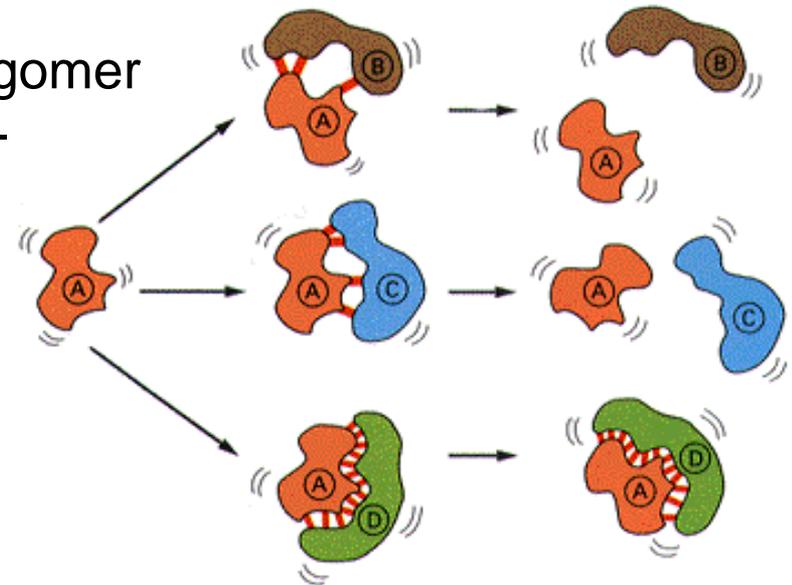
---

- Protein interaction defined as physical contact with molecular docking
  - Non-covalent contacts between side chains driven by hydrophobic effects, hydrogen bonds and electrostatic interactions
- Any two proteins can interact – but on what conditions ?
- Important aspect is the **biological context**:
  - Cell type, cell cycle phase and state
  - Environmental conditions
  - Developmental stage
  - Protein modification
  - Presence of cofactors and other binding partners



# Protein-protein interactions – Characteristics

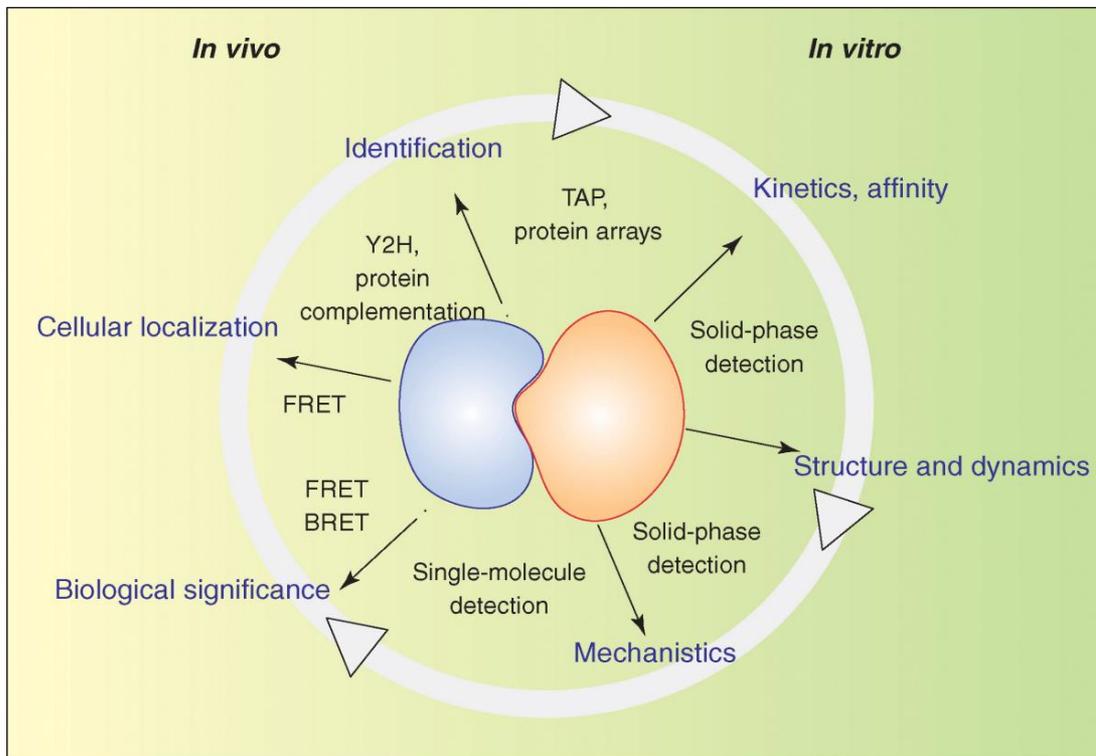
- Protein interactions differ in diverse structural and functional characteristics, e.g. composition, affinity and life time of the association
- **Strength** depicts whether an interaction is permanent or transient
- **Specificity** refers to the selective binding of interaction partners
- **Type of interacting subunits** specifies whether an interaction forms hetero-oligomer with several different subunits or homo-oligomer with only one type of protein subunit



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# Experimental detection methods

- Protein-protein interactions have been studied extensively by different experimental methods



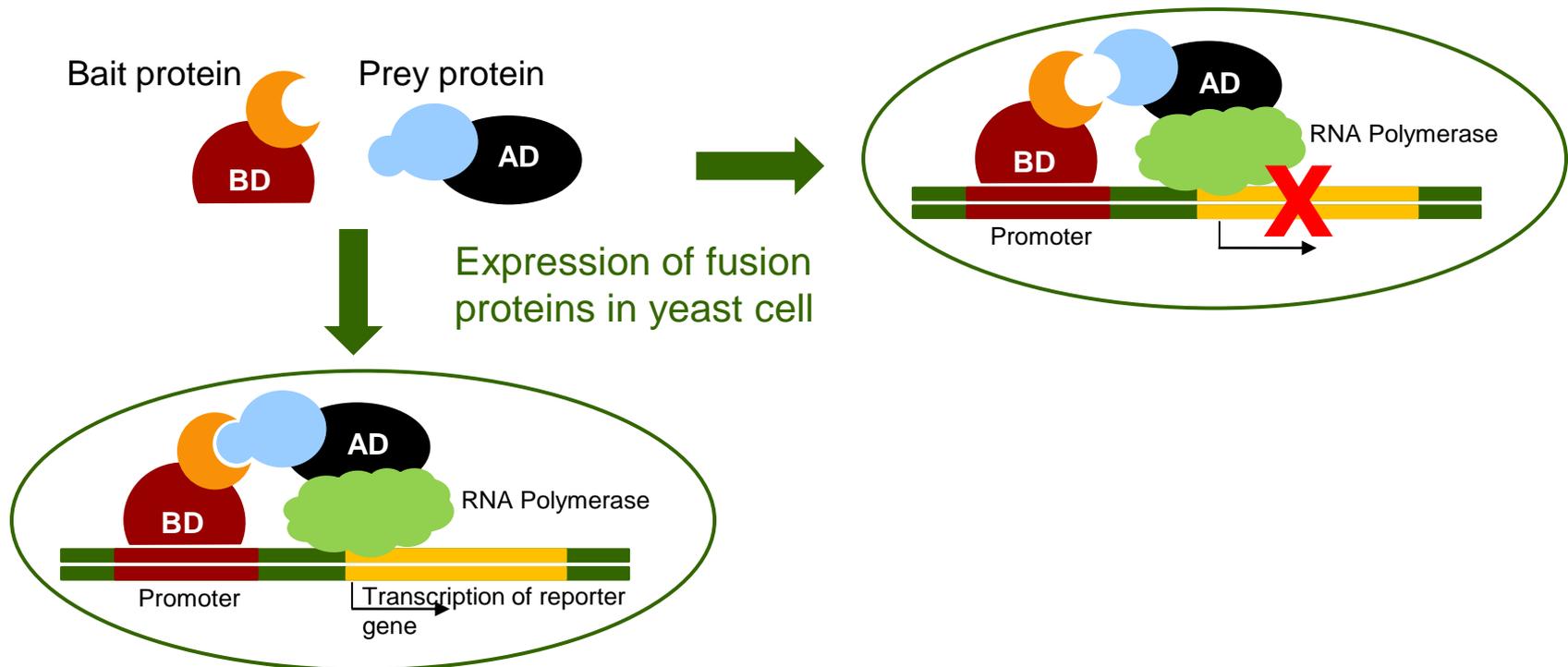
Piehler, 2005

Current Opinion in Structural Biology

- Small-scale techniques
- Large-scale techniques
  - Yeast two-hybrid assays (Y2H)
  - Tandem affinity purification and mass spectrometry (TAP-MS)
- Cell assay
  - *in vivo* vs. *in vitro*
- Type of interaction
  - binary vs. complex
- Type of characterization

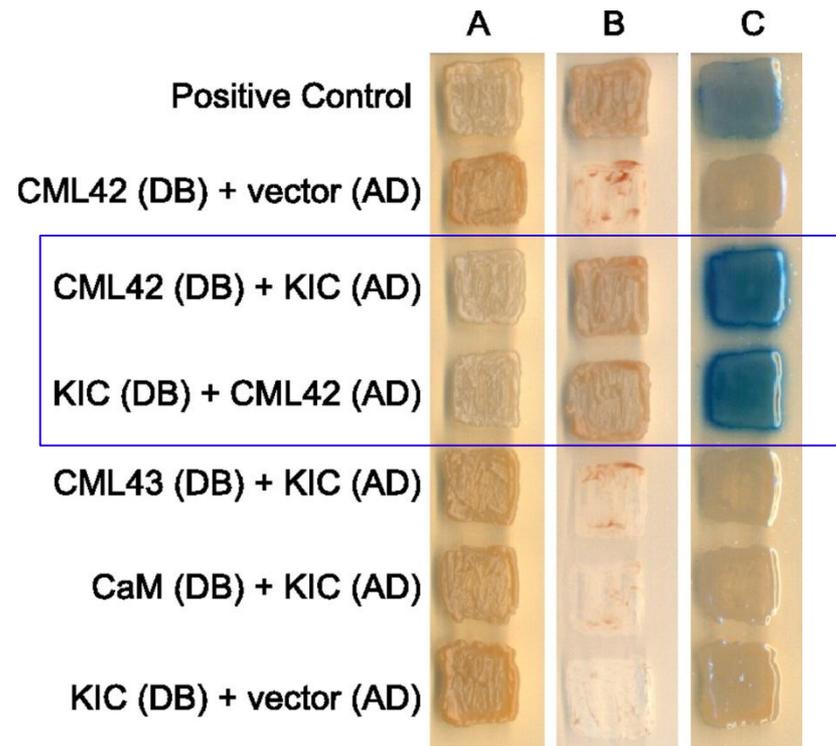
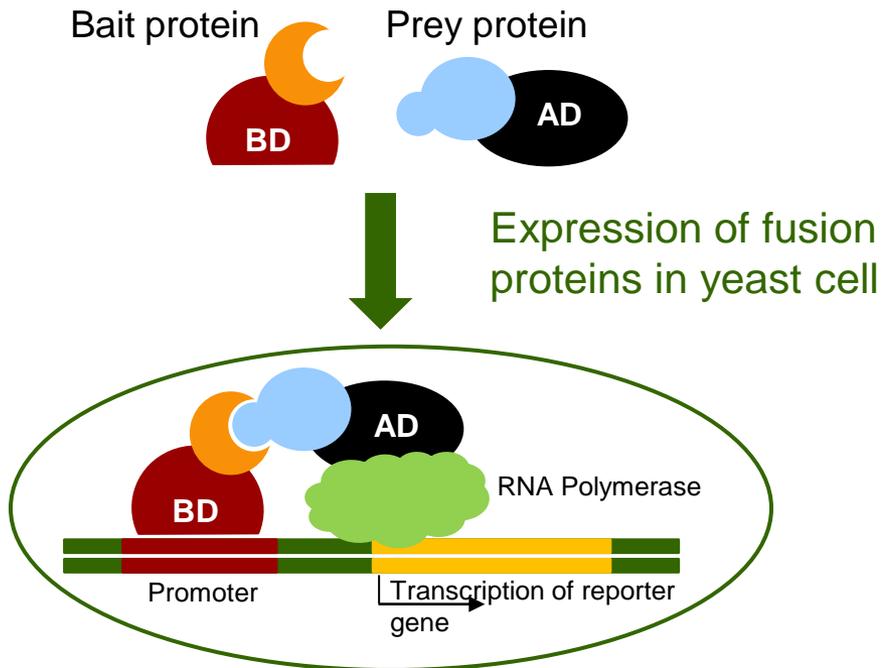
# Yeast two-hybrid screens

- Y2H is a molecular genetic tool, in which an interaction reconstitutes a transcription factor that activates expression of reporter genes
- Transcription factors require two domains: DNA binding domain (BD) and an activation domain (AD)



# Yeast two-hybrid screens

- Y2H is a molecular genetic tool, in which an interaction reconstitutes a transcription factor that activates expression of reporter genes
- Transcription factors require two domains: DNA binding domain (BD) and an activation domain (AD)



Dobney S et al. J. Biol. Chem.

# Yeast two-hybrid screens

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## Benefits

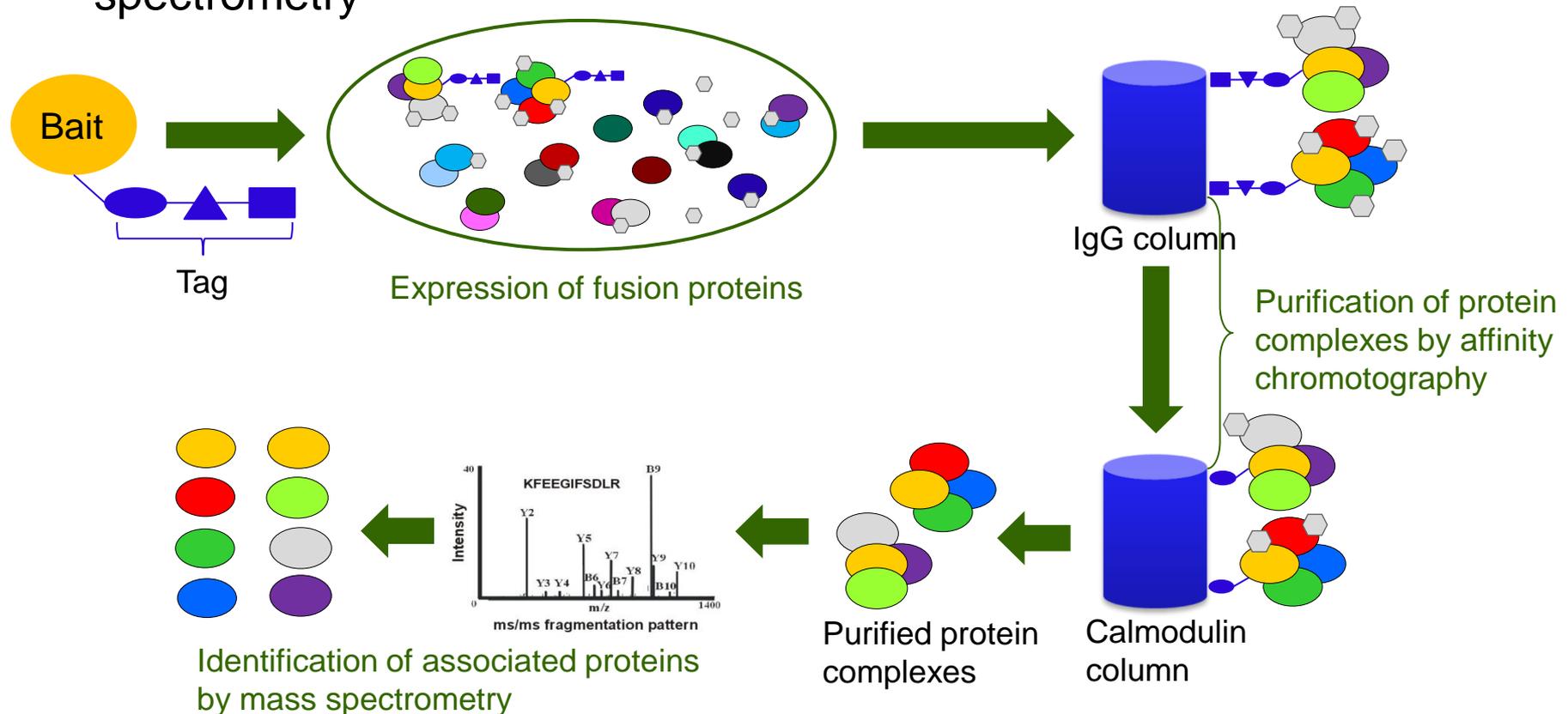
- Large-scale analysis
- Sensitive *in vivo* technique
- Identification of direct, transient and unstable interactions
- Genetic code of any fusion protein may be introduced into yeast cells

## Drawbacks

- Poor reliability
  - High false positive rate up to 50% (!)
  - High false negative rate
- Analysis of proteins in nucleus rather than in their native compartment
- Stable expression of fusion protein might be a problem
- Essential post-translational modification of non-yeast proteins may not be carried out

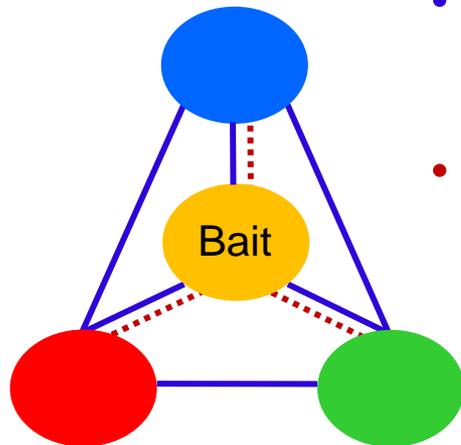
# Tandem affinity purification and mass spectrometry

- TAP-MS involves biochemical isolation of protein complexes and subsequent identification of their constituting proteins using mass spectrometry



# Matrix and spoke model

- Direct interactions can not be distinguished from interactions mediated by other proteins in a complex
- How many interactions are detected from a TAP-MS purification ?



- **Matrix model**: infers interactions between all proteins of a purified complex  $\rightarrow (N*N - 1)/2$
- **Spokes model**: infers only interactions between the bait and the co-purified proteins  $\rightarrow N - 1$

# Proteins	Matrix	Spoke
4	6	3
10	45	9
80	3540	79

# Tandem affinity purification and mass spectrometry

---

## Benefits

- Large-scale analysis
- Detection of protein complexes/interactions in correct cellular environment and detect several members of a complex

## Drawbacks

- No direct translation into binary interactions
- Protein complexes not present under given conditions are missed
- Loosely associated proteins of a complex might be washed off during purification
- Protein targeting might interfere with complex formation

# Protein-protein interaction databases

Database	Species	Proteins	Interactions
IntAct	No restriction	53.276	271.764
BioGrid	No restriction	30.712	131.638
DIP	No restriction (372)	23.201	71.276
MINT	No restriction	31.797	90.505
HPRD	Human only	30.047	39.194
MMPPPI	Mammals		
⋮			
STRING	No restriction (630)	2.590.259	
UniHI	Human only	22.307	200.473
OPID	Human only		
⋮			

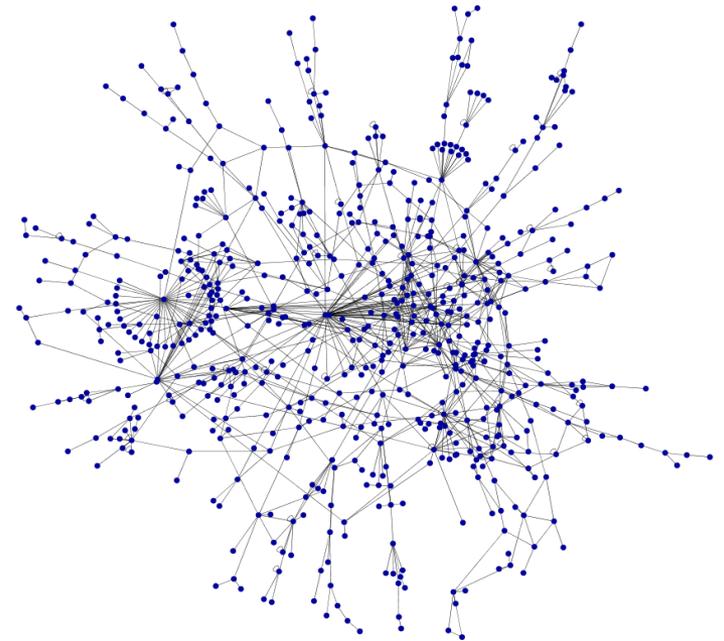
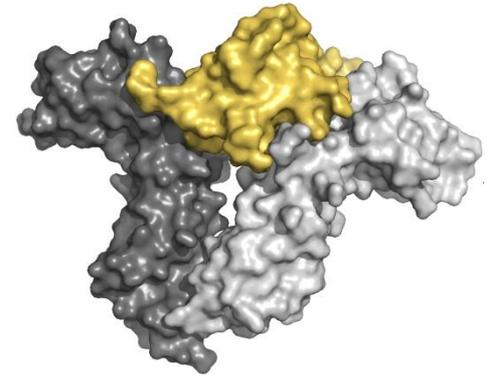
Experimentally  
verified protein  
interactions

Experimentally  
verified and  
predicted protein  
interactions

# This Lecture

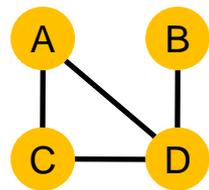
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- Protein-protein interactions
  - Characteristics
  - Experimental detection methods
  - Databases
- Protein-protein interaction networks
  - Characteristics
  - Applications
    - Protein function prediction



# Protein-protein interaction networks

- Binary interaction data can be assembled to protein-protein interaction networks
- Networks are represented as graphs
- Definition of a graph:  $G = (V, E)$ 
  - $V$  is the set of nodes (proteins)
  - $E$  is the set of edges (interactions)
- Computational representation of graphs:



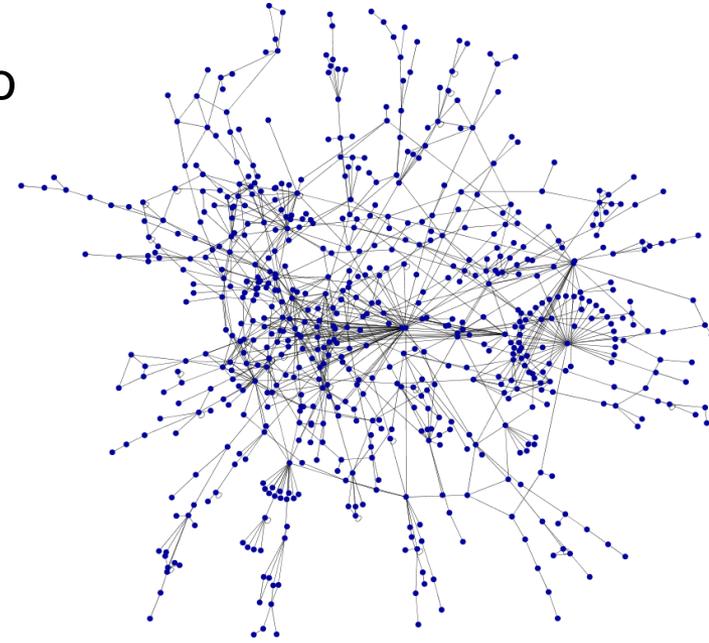
Adjacency lists:

(ordered) pairs of nodes

$\{ (A,C), (A,D), (B,D), (C,A), (C,D), (D,B), (D,C), (D,A) \}$

Adjacency matrix

	A	B	C	D
A	0	0	1	1
B	0	0	0	1
C	1	0	0	1
D	1	1	1	0



# Graph-theoretic concepts

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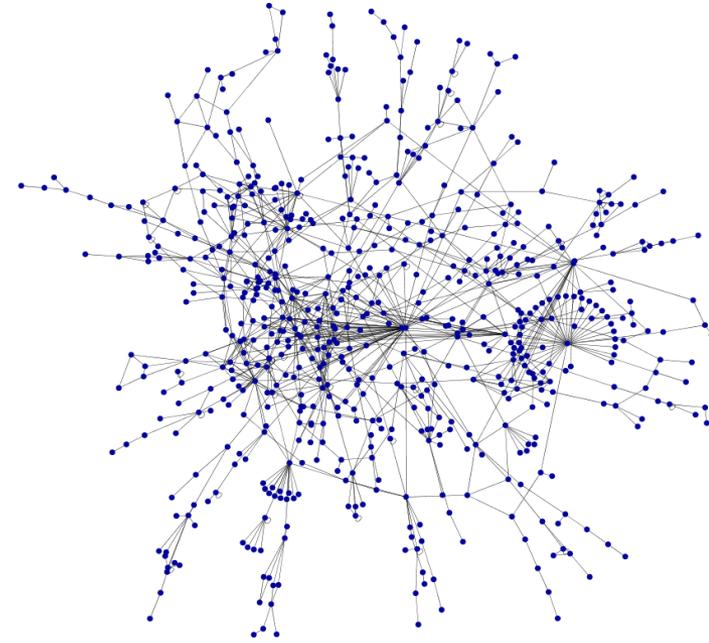
- A **graph** is defined by  $G = (V, E)$ , where  $V$  is the set of nodes and  $E$  is the set of edges connecting pairs of nodes
- The **distance** between two nodes is the number of edges on the shortest path between them
  - **Diameter** is the maximum distance between any two node
- The **neighborhood** of node is the set of nodes connected to it
  - **$n$ -neighborhood** of a node is the set of nodes with distance  $n$
- A **clique** is a fully connected subgraph, a subgraph in which every two nodes are connected by an edge
  - **$k$ -core** is a subgraph where each node has at least  $k$  interactions
- The **density** is the fraction of edges a graph has given all possible pairs of nodes

$$D_G = \frac{2|E|}{|V|(|V|-1)}$$

# Protein-protein interaction networks

---

- Why study protein interaction networks ?
  - Elucidate the relationship between network structure and biological function
  - Discover novel protein function
  - Identify functional modules and conserved interaction patterns
  - Associate proteins with phenotypes or disease
  - Study pharmacological drug-target relationships



# Topological network properties

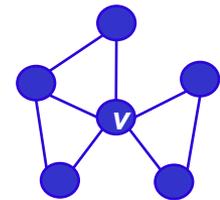
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- Topology of a network reveals its organization on different levels
  - Local and global characteristics provide insights in network evolution, stability and dynamics
- Common properties of biological networks
  - Small world property
  - Clustering coefficient
  - Degree distribution
  - Network centrality
- Modular network organization

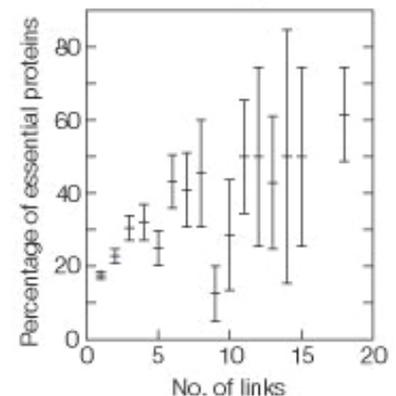
# Network centrality

- Network centrality analysis identifies interesting elements/proteins within a network
- Quantitative measure to determine a proteins relative position in a network
- Example – Degree centrality:
  - Degree of a node = number of edges to other nodes

$$C_D(v) = \frac{\text{deg}(v)}{|V| - 1}$$



- High centrality in interaction networks correlates with:
  - Gene essentiality
  - Evolutionary importance
  - Conservation rate
  - Likelihood to cause human disease



# Degree distribution

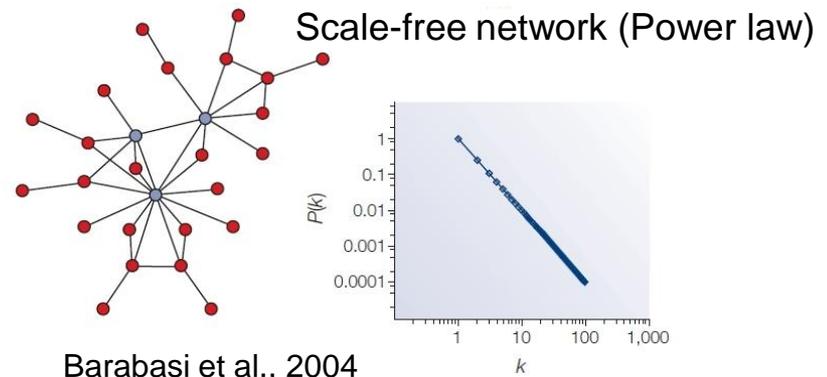
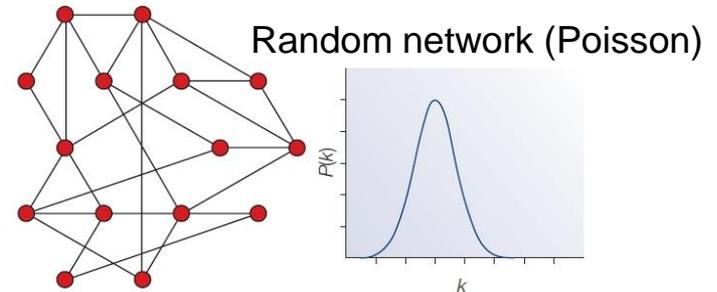
- Degree distribution  $P(k)$ : probability that a node has exactly  $k$  links
  - Count the number of nodes  $N(k)$  with  $k = 1, 2, \dots$  links and divide by  $N$
- Allows to distinguish between different network classes

- Common network distributions

- Poisson: 
$$P(k) = \frac{e^{-d} d^k}{k!}$$

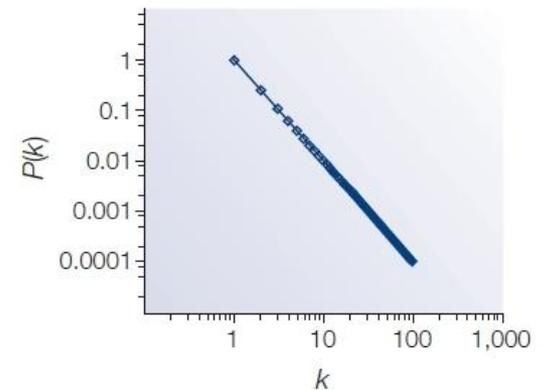
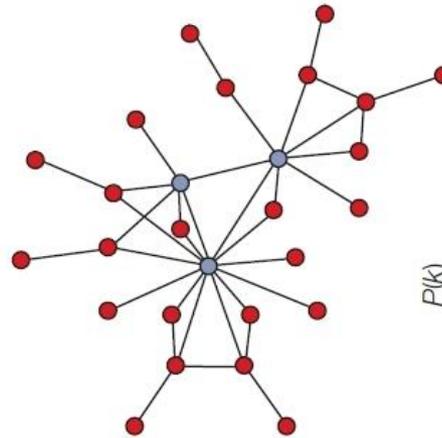
- Exponential: 
$$P(k) \sim e^{-k/d}$$

- Power-law: 
$$P(k) \sim k^{-\gamma}$$



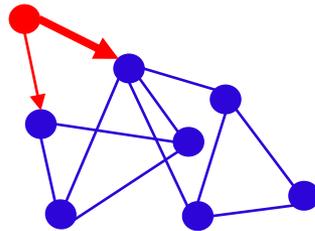
# Scale-free networks

- **Scale-free networks**, e.g. protein interaction networks, follow a power law distribution:  $P(k) \sim k^{-\gamma}$ , with degree exponents  $2 < \gamma < 3$ 
  - Characterized by a small number of highly connected nodes known as **hubs**
- Scale-free topology typical feature of interaction networks
  - Most proteins participate in few interactions and few proteins in dozens
- Resistant to random failure, but prone to vulnerable attacks especially against hubs

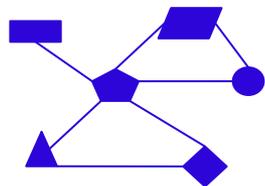


# Scale-free networks

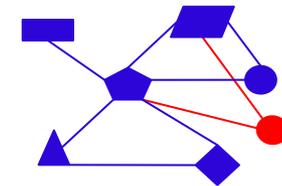
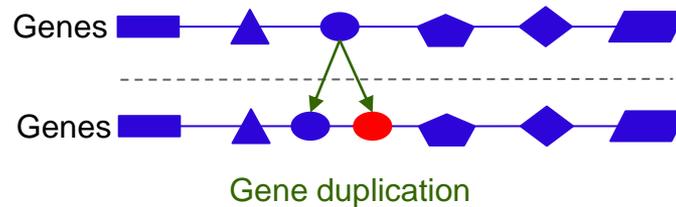
- **Evolutionary origin** of scale free networks
  - Growth: networks emerge through addition of new nodes
  - Preferential attachment: new nodes prefer to link to more connected nodes



- In interaction networks: scale-free property is thought to originate from gene duplications



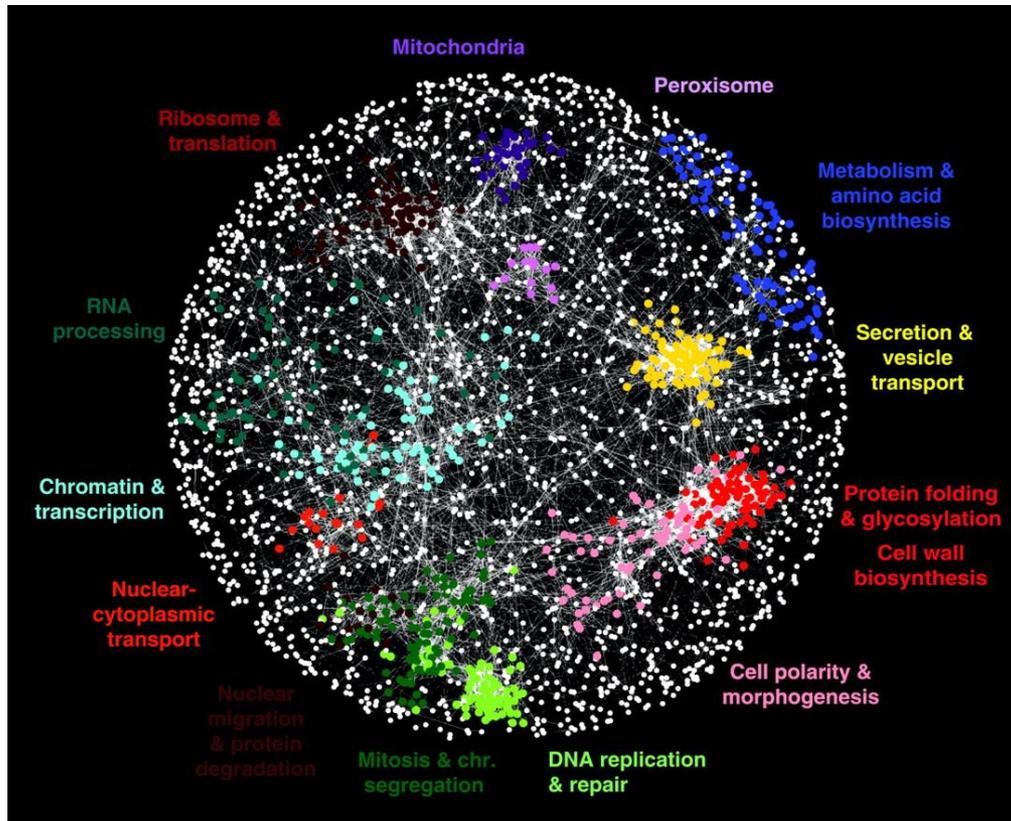
Network before duplication



Network after duplication

# Modular network organization

- Complex cellular function is carried out in a highly modular manner
- Modular organization is reflected in a modular network structure



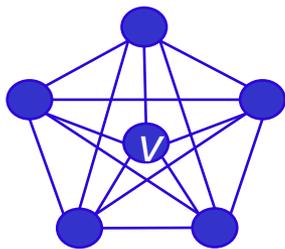
Costanzo et al., Nature, 2010

# Clustering coefficient

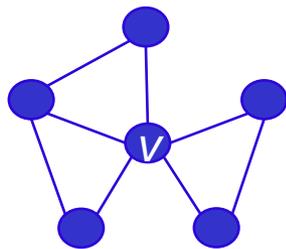
- Modules (or cluster) are densely connected groups of nodes
- Cluster coefficient  $C$  reflects a network's potential modularity and characterizes the tendency of nodes to cluster ('triangle density')

$$C_v = \frac{2E_v}{d_v(d_v - 1)} \longrightarrow \langle C \rangle = \frac{1}{|V|} \sum_{v \in V} C_v$$

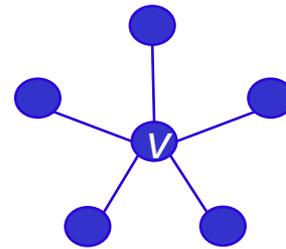
- $E_v$  = number of edges between neighbors of  $v$
- $d_v$  = number of neighbors of  $v$
- $\frac{d_v(d_v - 1)}{2}$  = maximum number of edges between neighbors  $d_v$
- Example:



$$C_v = 10/10 = 1$$



$$C_v = 3/10 = 0.3$$



$$C_v = 0/10 = 0$$

# Functional modules

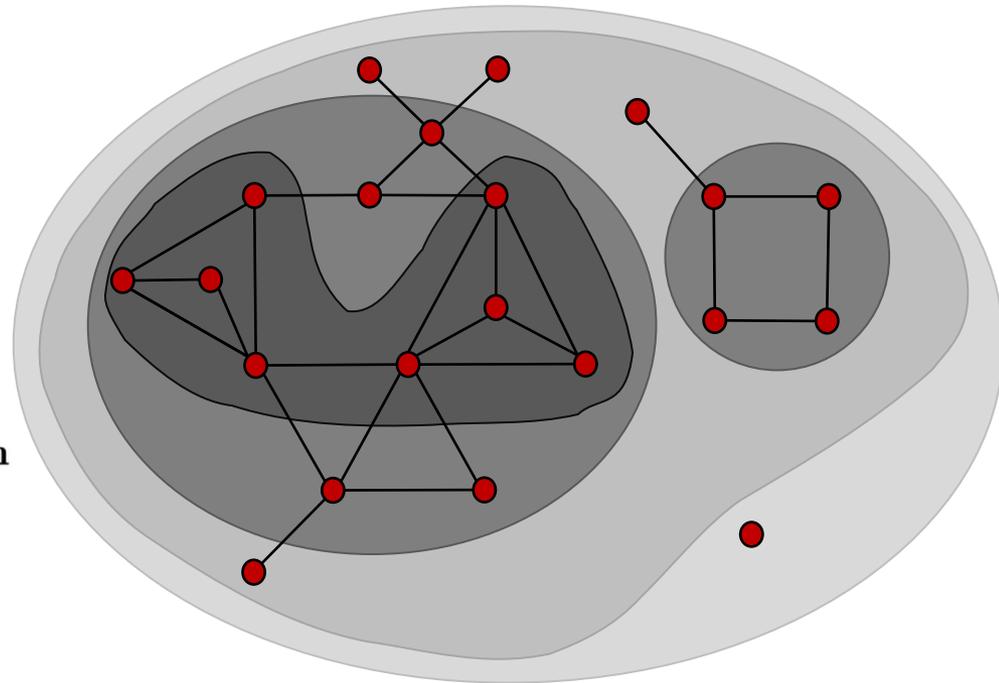
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- Two types of modules are distinguished in interaction networks
  - Protein complexes: proteins that interact with each other at the same time and place
  - Functional modules: proteins that participate in the same process but interacting at different times and places
- Finding functional modules → find densely connected subgraphs:
  - Cliques / **k-cores**
  - Network clustering
  - **Network alignment**
  - Decompose networks into subnetworks according to particular topological properties

# K-cores

- Identifying cliques in graphs is NP complete
- Approximation:  $k$ -cores
- A  $k$ -core of a graph  $G$  is defined as maximally connected subgraph of  $G$  in which all vertices have degree at least  $k$

```
while modify_kcore == true do
  modify_kcore = false
  for all  $v \in V$  do
    consider  $\text{deg}(v)$  and the degree of  $N(v)$ 
    if  $\text{deg}(v) < k$  then
      prune  $v$ 
      modify_kcore = true
    else
      if  $v$  has  $n$  neighbors with degree  $< k$  then
         $\text{deg}(v) = \text{deg}(v) - n$ 
        if  $\text{deg}(v) < k$  then
          prune  $v$ 
          modify_kcore = true
```



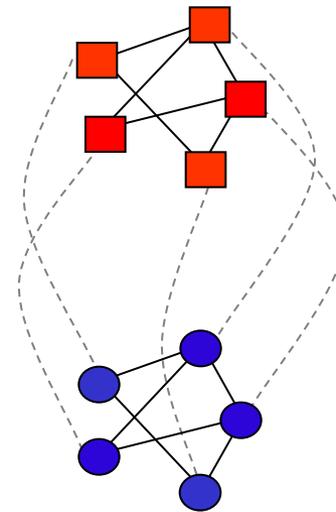
# Network Alignment

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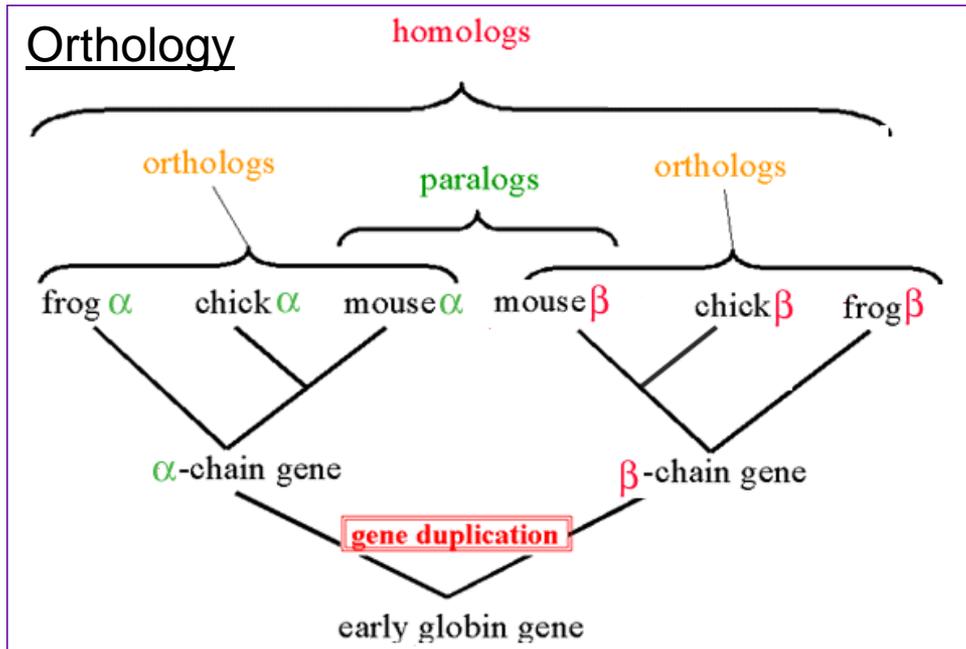
- 1) Detection of orthologous proteins
- 2) Identification of interologs & assembly to conserved and connected subgraphs (CCS)

ACGGT\_AGATA

\_CGGTCAGAT\_



# Network Alignment

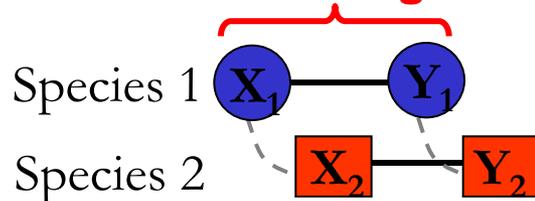


In-paralogs (,recent' paralogs)

Out-paralogs (,ancient' paralogs)

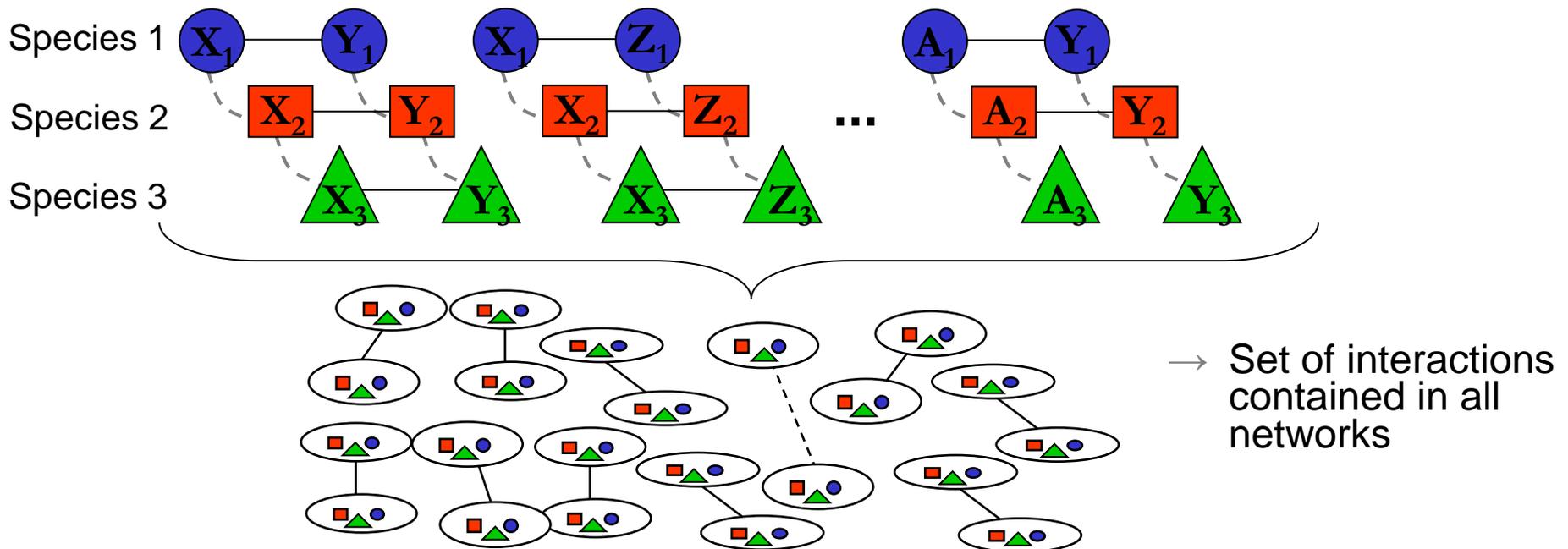
## Interologs

**Interolog** = orthologous interaction



# Network Alignment

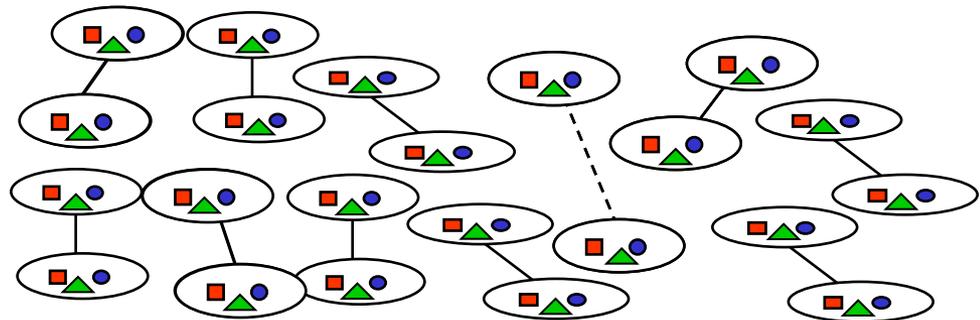
- (1) Identification of interologs and (2) assembly to subgraphs
- Modification of algorithm for frequent subgraph discovery



# Network Alignment

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(2) Assembly of conserved PPIs to maximally connected subgraphs



→ Maximally connected and conserved subgraph → CCS

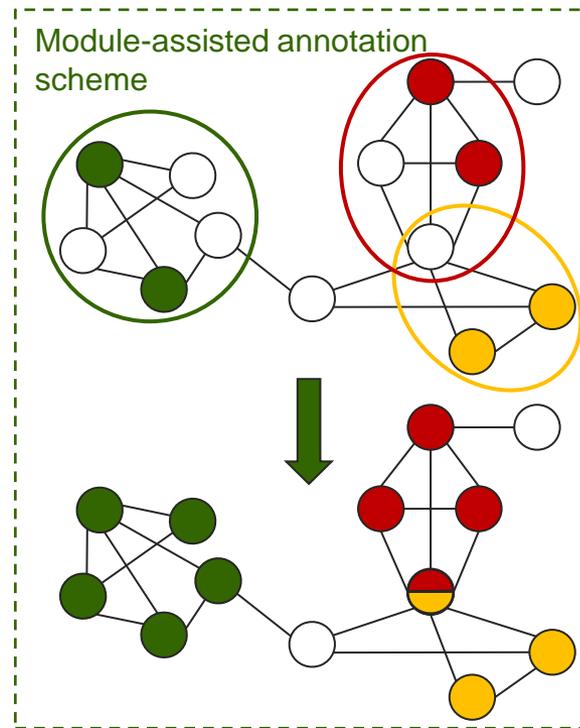
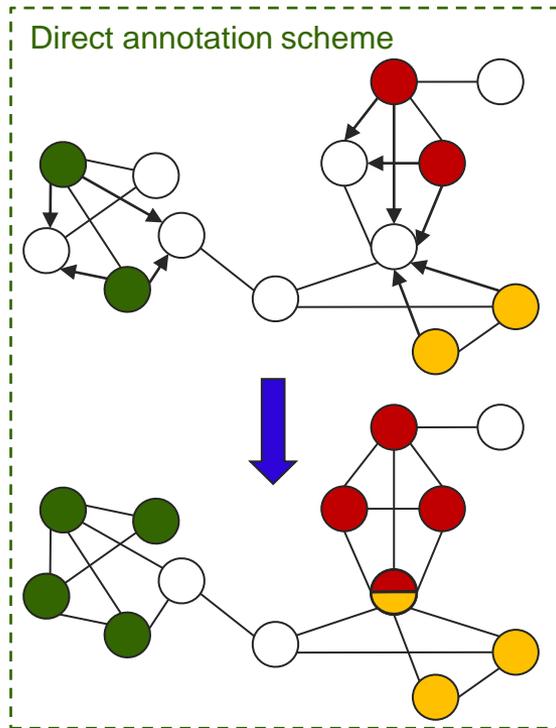
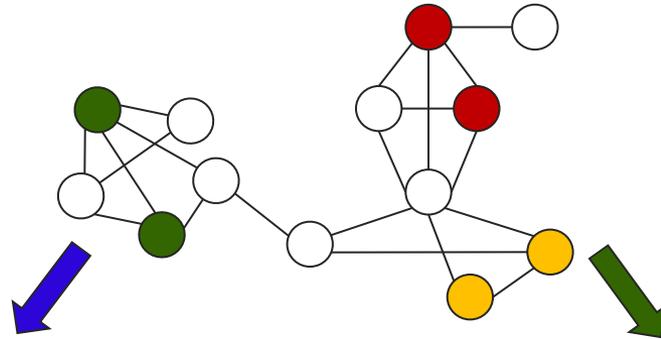


# Network-based protein function prediction

---

- Knowing a protein's function is essential for understanding biological processes, cellular mechanisms, evolutionary changes and the onset of diseases
- Protein interactions reflect the **biological role of proteins** within the cells
- Neighboring proteins in a network are likely to share function (guilt-by-association)
- Function might be inferred:
  1. **By transferring known functions from directly or indirectly interacting proteins.**
  2. **Based on the protein complexes a protein belongs to.**

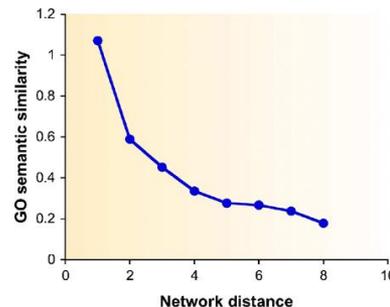
# Network-based protein function prediction



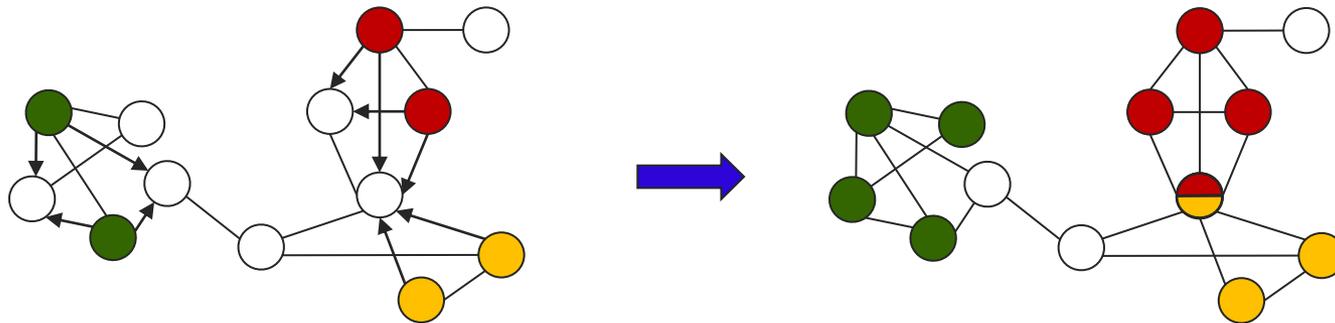
- Study the set of neighbors
- Consider position of the protein within its neighborhood,
- Consider position of the protein in the entire interaction network

# Direct annotation scheme

- **Correlation between network and functional distance:** the closer two proteins are in the network, the more similar are their functional annotation

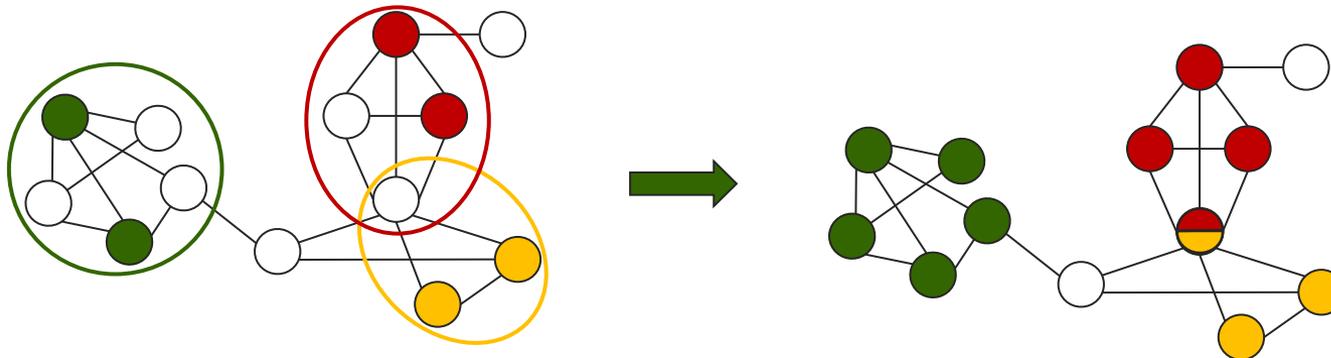


- **Majority-rule** based on most common function(s) annotated to the direct interaction partners of a protein – proteins are associated with the most frequent functions of its direct neighbors



# Module-assisted annotation scheme

- Based on hypothesis: cellular function is organized in a highly modular manner
- Module-based function assignment:
  1. First compute clusters (or modules) within the protein network.
  2. Proteins in a cluster are associated with annotations that are enriched within the module
    - Common functional annotations shared by the majority of the module's proteins
    - Over-represented function that are enriched in a cluster according to the hypergeometric distribution



# Direct vs. Module-based methods

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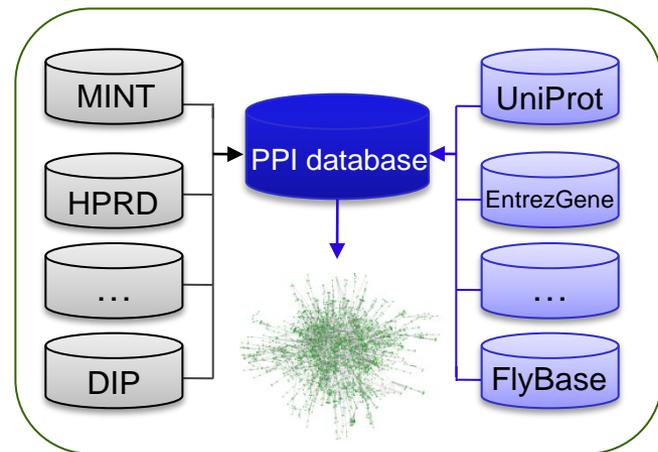
- Direct methods
  - + Accurate predictions
  - + Provide high coverage
  - More sensitive to high level of false positives
- Module-based methods
  - + More robust to missing or false interactions
  - + Performance improves in networks with less functional coverage
  - Predict function only in dense network regions → reduced coverage
  - Less accurate than simple direct methods
- Both methods work within a species, which disregards functional information available in evolutionary related other species



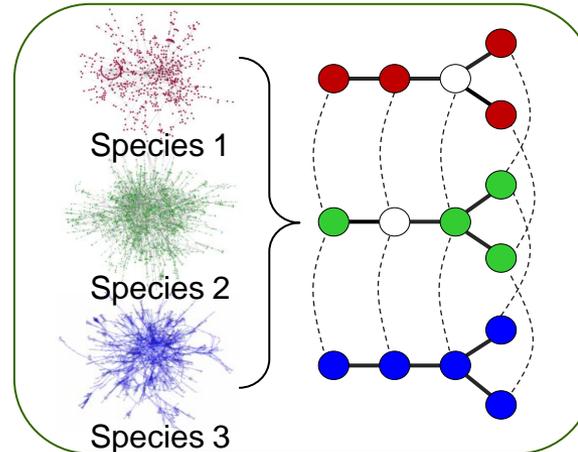
Combining modularity, conservation, and direct interactions in one method

# Combine modularity, conservation, and direct interactions

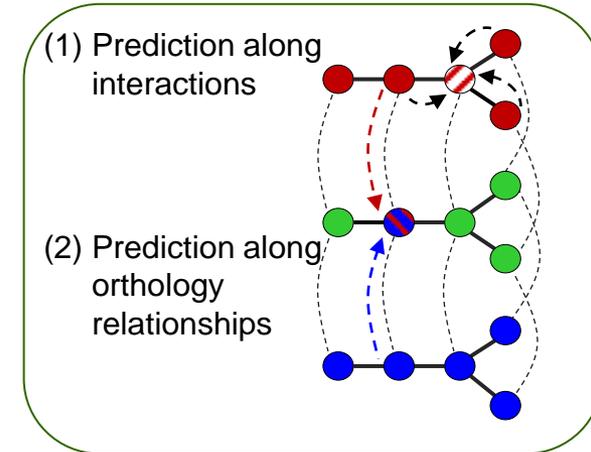
- Assumption: structural conservation in networks correlates with functional conservation in networks which can be exploited for predicting protein functions



a) Data Integration

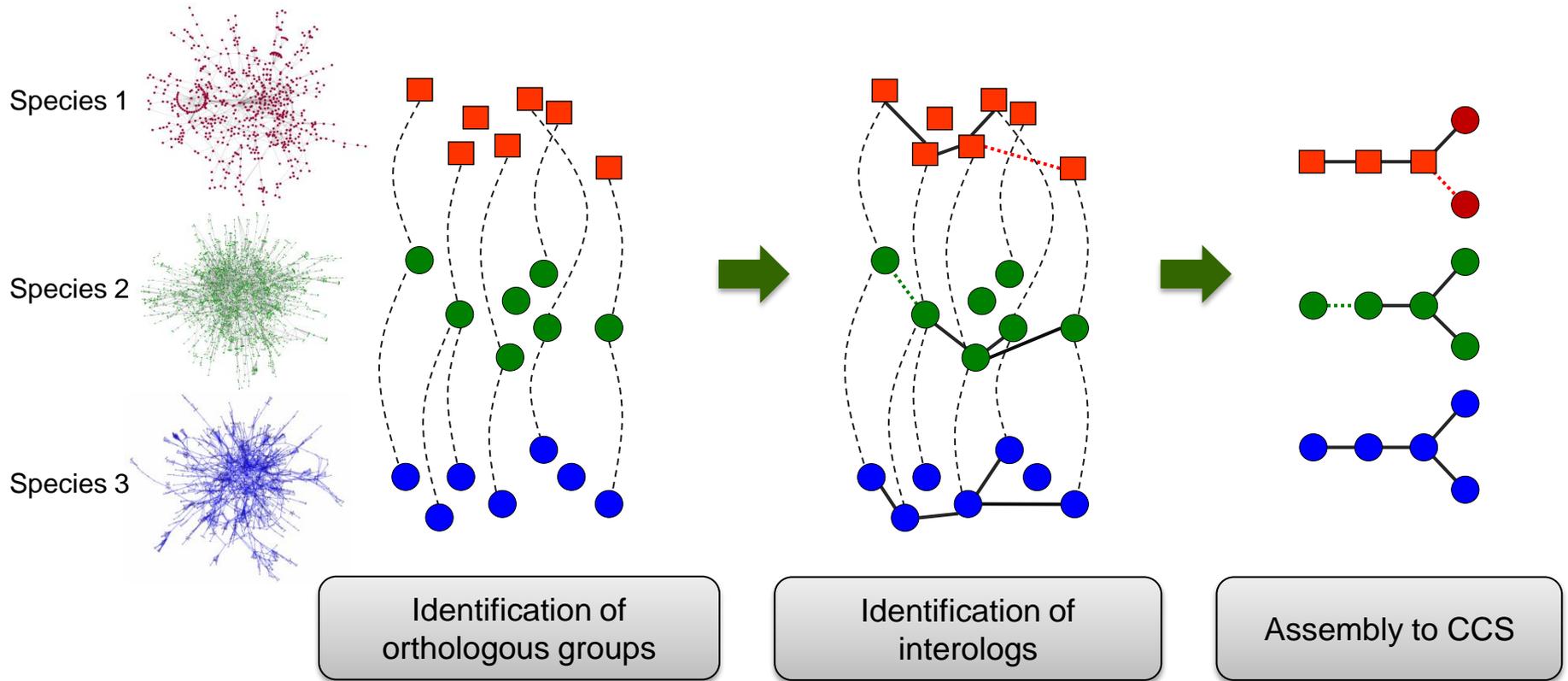


b) Network Comparison



c) Protein Function Prediction

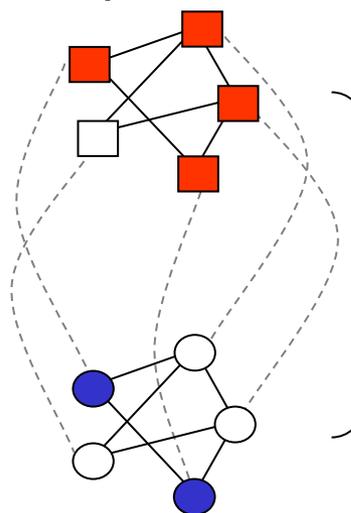
# Network Comparison



# CCS-based function prediction

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- Analyze proteins within CCS that are defined by evolutionary conserved processes

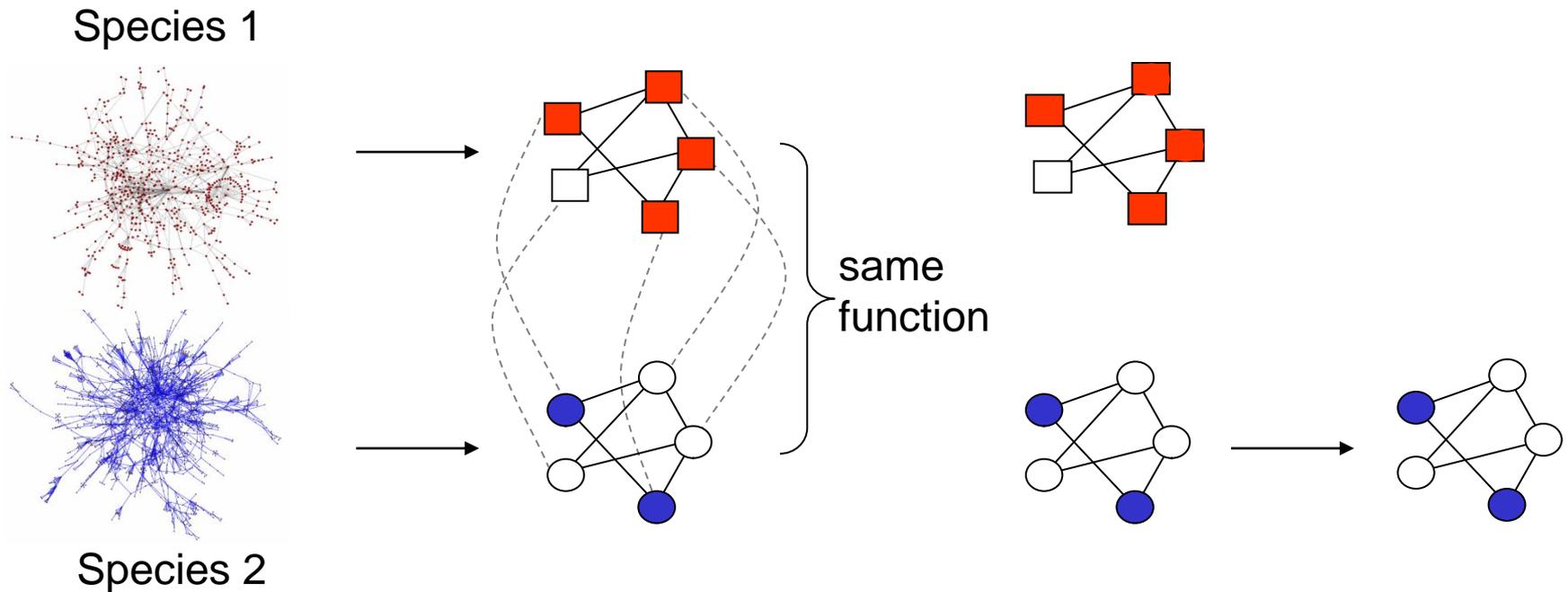


Evolutionary conserved CCS = Functionally coherent?

- Combine comparative cross-species genomics and functional linkage within species-specific networks, predict function from
  - Orthology relationships
  - Direct interaction partners

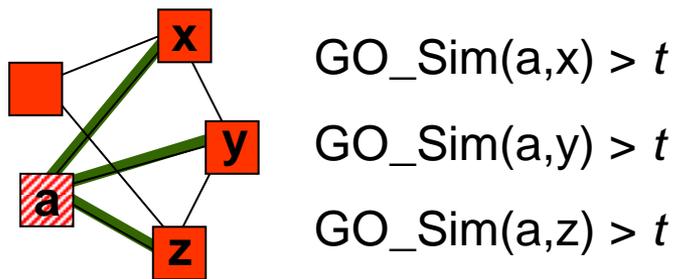
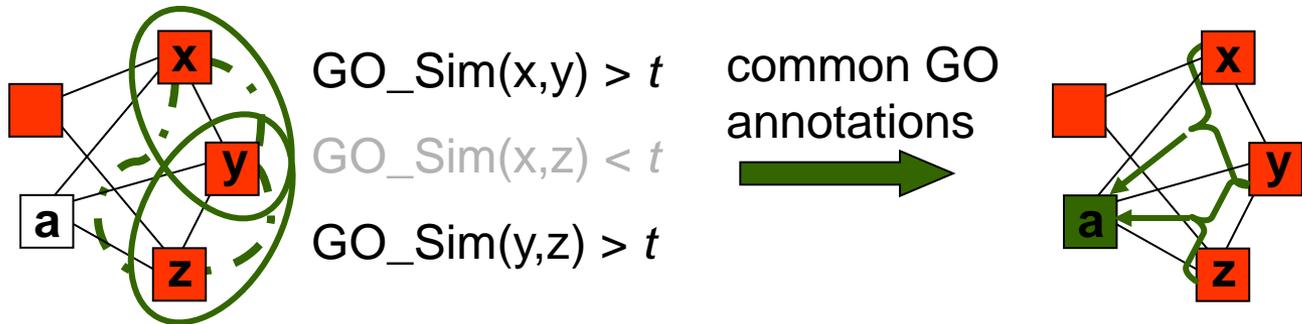
# CCS-based function prediction

## 1) Exploiting Orthology Relationships across multiple species



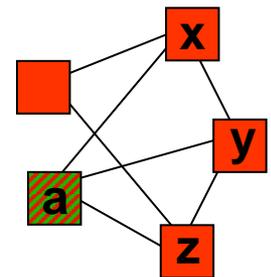
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## 2) Exploiting Protein Neighbours – Based on functional similarity between proteins



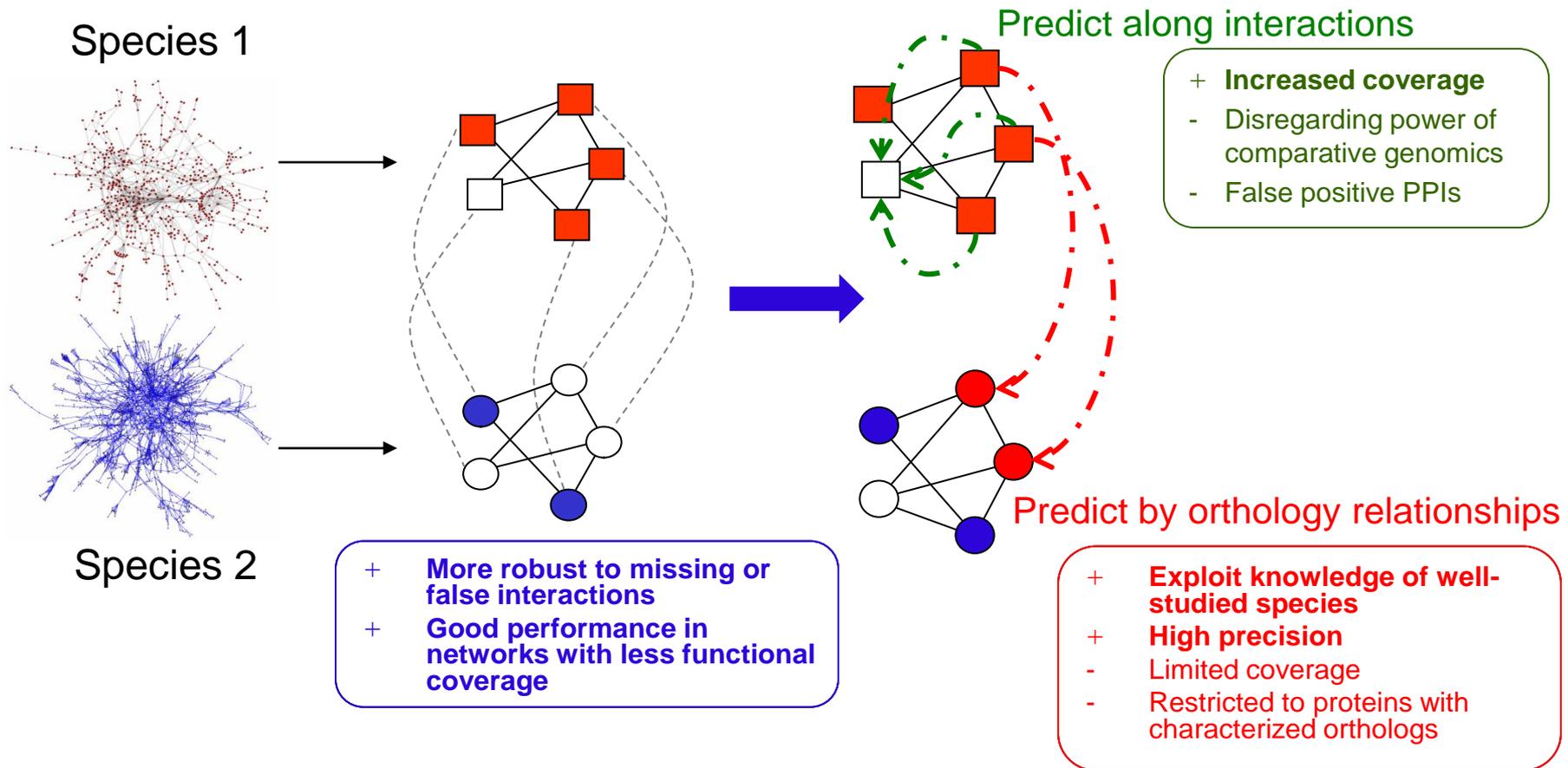
Candidate GO terms =  $\{GO_1, GO_2, \dots, GO_n\}$

	protein	GO Sim	$GO_i$
candidate	a	-	? ✓
training	x	0.7	✓
	y	0.75	-
	z	0.71	✓



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## Combining modularity, conservation and interaction



# Summary

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- Analysis of protein interaction data and protein interaction network facilitates the understanding of cellular organization, function and processes
- Public databases provide large repositories of interaction data of varying quality and quantity
- Successfully used to infer novel function and disease associations from interaction partners