

Can Statistical Language Models be used to improve Spectrum Based Fault Localization Rankings? (Full Spectra – Additional Material)

Anonymous Author(s)

SBFL ranking metric	$\overline{\mathcal{R}}_{\lambda}(\Omega)$					max improv.	$\overline{\mathcal{R}}_{\lambda}^*(\Omega)$					max improv.
	$\lambda = 1$	$\lambda = 0.98$	$\lambda = 0.9$	$\lambda = 0.5$			$\lambda = 1$	$\lambda = 0.98$	$\lambda = 0.9$	$\lambda = 0.5$		
AMPLE	7797.3	7766.3	7900.8	8603.6	0.4%	1094.8	824.0	770.1	822.5	29.7%		
ANDERBERG	10077.4	9632.7	9653.0	9811.7	4.4%	597.0	340.7	345.1	413.4	42.9%		
ARITHMETIC MEAN	14367.6	13597.6	13057.6	11980.3	16.6%	1072.9	811.7	756.5	688.2	35.9%		
COHEN	14236.9	13460.9	12944.1	11926.6	16.2%	986.3	719.5	669.4	649.7	34.1%		
DICE	10077.1	9632.5	9652.6	9811.3	4.4%	597.1	340.8	345.2	413.4	42.9%		
EUCLID	23987.3	21911.0	20115.0	17503.3	27.0%	13655.8	8588.5	6102.9	4253.7	68.9%		
FLEISS	20114.6	18442.8	17101.5	14964.4	25.6%	4762.1	3326.9	2601.0	1842.7	61.3%		
GEOMETRIC MEAN	14736.6	13930.0	13328.6	12107.7	17.8%	1233.8	986.4	901.2	759.7	38.4%		
GOODMAN	10096.3	9644.8	9659.7	9812.6	4.5%	702.0	428.9	354.6	414.3	49.5%		
GP13	10204.9	9761.4	9791.6	10011.9	4.3%	889.2	582.9	561.6	619.9	36.8%		
HAMANN	23987.3	21911.0	20115.0	17503.3	27.0%	13655.8	8588.5	6102.9	4253.7	68.9%		
HAMMING ETC.	23987.3	21911.0	20115.0	17503.3	27.0%	13655.8	8588.5	6102.9	4253.7	68.9%		
HARMONIC MEAN	14892.1	14069.1	13463.0	12177.9	18.2%	1264.1	1012.9	919.2	765.7	39.4%		
JACCARD	10077.2	9632.6	9652.8	9811.4	4.4%	597.0	340.8	345.0	413.4	42.9%		
KULCZYNSKI1	10077.3	9632.6	9652.9	9811.5	4.4%	597.0	340.8	345.2	413.4	42.9%		
KULCZYNSKI2	10181.3	9737.0	9764.8	9971.1	4.4%	746.9	461.2	446.1	513.2	40.3%		
M1	23987.3	21911.0	20115.0	17503.3	27.0%	13655.8	8588.5	6102.9	4253.7	68.9%		
M2	10184.2	9740.4	9768.9	9979.5	4.4%	835.1	534.1	510.0	568.5	38.9%		
OCHIAI	10108.4	9663.4	9685.6	9857.1	4.4%	610.2	353.2	349.8	419.6	42.7%		
OCHIAI2	10200.3	9751.7	9770.8	9918.5	4.4%	789.0	447.7	449.4	521.3	43.3%		
NAISH2 (Op2)	12902.7	12349.8	11976.7	11155.1	13.5%	942.5	709.4	602.4	624.3	36.1%		
OVERLAP	10241.8	9775.4	9828.0	10203.4	4.6%	1067.7	467.7	502.4	821.6	56.2%		
ROGERS & TANIMOTO	23987.3	21911.0	20115.0	17503.3	27.0%	13655.8	8588.5	6102.9	4253.7	68.9%		
ROGOT1	20004.4	18364.9	17058.7	14937.8	25.3%	4719.3	3283.7	2561.3	1805.7	61.7%		
ROGOT2	14881.4	14022.5	13386.9	12096.1	18.7%	1384.1	1074.8	862.6	698.1	49.6%		
RUSSELL & RAO	10284.8	9824.7	9875.8	10230.1	4.5%	1198.0	627.0	646.0	897.1	47.7%		
SCOTT	20004.4	18364.9	17058.7	14937.8	25.3%	4719.3	3283.7	2561.3	1805.7	61.7%		
SIMPLE MATCHING	23987.3	21911.0	20115.0	17503.3	27.0%	13655.8	8588.5	6102.9	4253.7	68.9%		
SOKAL	23987.3	21911.0	20115.0	17503.3	27.0%	13655.8	8588.5	6102.9	4253.7	68.9%		
SØRENSEN-DICE	10077.3	9632.6	9652.8	9811.5	4.4%	597.0	340.8	345.1	413.4	42.9%		
TARANTULA	10064.6	9620.1	9639.1	9796.2	4.4%	585.7	335.4	338.8	405.9	42.7%		
WONG1	10284.8	9824.7	9875.8	10230.1	4.5%	1198.0	627.0	646.0	897.1	47.7%		
WONG3	20455.7	18165.1	17076.5	15799.9	22.8%	10350.5	5056.8	3954.1	3435.9	66.8%		
WONG2	23987.3	21911.0	20115.0	17503.3	27.0%	13655.8	8588.5	6102.9	4253.7	68.9%		
ZOLTAR	11980.9	11213.8	11222.9	11292.0	6.4%	1575.2	606.0	608.9	655.8	61.5%		

TABLE 1: OVERVIEW OF ALL EXAMINED SBFL METRICS WITH $\overline{\mathcal{R}}_{\lambda}(\Omega)$ AND $\overline{\mathcal{R}}_{\lambda}^*(\Omega)$ FOR $\lambda \in \{1.0, 0.98, 0.9, 0.5\}$ AND THE MAXIMUM IMPROVEMENTS FOR THE HIGHEST VALUES WITH REGARD TO $\lambda = 1$. HIGHEST RANKINGS ARE PRINTED WITH A BOLD FONT FOR EACH SET OF VALUES.

SBFL ranking metric	$\tilde{\mathcal{R}}_\lambda(\Omega)$					max improv.	$\tilde{\mathcal{R}}_\lambda^*(\Omega)$					max improv.
	$\lambda = 1$	$\lambda = 0.98$	$\lambda = 0.9$	$\lambda = 0.5$			$\lambda = 1$	$\lambda = 0.98$	$\lambda = 0.9$	$\lambda = 0.5$		
AMPLE	2843.0	2796.0	2978.0	3874.0	1.7%	42.0	43.0	44.0	75.0	0.0%		
ANDERBERG	5321.0	3428.0	3360.0	4382.0	36.9%	27.0	23.0	26.0	40.0	14.8%		
ARITHMETIC MEAN	11064.0	8591.0	6714.0	5572.0	49.6%	27.0	26.0	28.0	41.0	3.7%		
COHEN	11064.0	8412.0	6702.0	5546.0	49.9%	27.0	26.0	28.0	41.0	3.7%		
DICE	5324.0	3428.0	3360.0	4382.0	36.9%	27.0	23.0	26.0	40.0	14.8%		
EUCLID	24776.0	22947.0	19705.0	15753.0	36.4%	9683.0	1162.0	1049.0	856.0	91.2%		
FLEISS	21118.0	18014.0	15229.0	11293.0	46.5%	40.0	39.0	42.0	68.0	2.5%		
GEOMETRIC MEAN	11081.0	8653.0	6846.0	5590.0	49.6%	29.0	27.0	30.0	46.0	6.9%		
GOODMAN	5324.0	3428.0	3360.0	4382.0	36.9%	27.0	23.0	26.0	40.0	14.8%		
GP13	5286.0	3863.0	4063.0	5167.0	26.9%	33.0	31.0	34.0	55.0	6.1%		
HAMANN	24776.0	22947.0	19705.0	15753.0	36.4%	9683.0	1162.0	1049.0	856.0	91.2%		
HAMMING ETC.	24776.0	22947.0	19705.0	15753.0	36.4%	9683.0	1162.0	1049.0	856.0	91.2%		
HARMONIC MEAN	11426.0	8818.0	7057.0	5590.0	51.1%	27.0	26.0	27.0	45.0	3.7%		
JACCARD	5320.0	3428.0	3360.0	4382.0	36.8%	27.0	23.0	26.0	40.0	14.8%		
KULCZYNSKI1	5325.0	3428.0	3360.0	4382.0	36.9%	27.0	23.0	26.0	40.0	14.8%		
KULCZYNSKI2	5274.0	3900.0	4079.0	4973.0	26.1%	26.0	22.0	23.0	40.0	15.4%		
M1	24776.0	22947.0	19705.0	15753.0	36.4%	9683.0	1162.0	1049.0	856.0	91.2%		
M2	5286.0	3865.0	4062.0	5070.0	26.9%	34.0	32.0	34.0	58.0	5.9%		
OCHIAI	5453.0	3718.0	3690.0	4575.0	32.3%	28.0	26.0	27.0	43.0	7.1%		
OCHIAI2	5922.0	3593.0	3690.0	4482.0	39.3%	29.0	27.0	30.0	45.0	6.9%		
NAISH2(OP2)	5630.0	4484.0	4321.0	5079.0	23.3%	33.0	31.0	34.0	55.0	6.1%		
OVERLAP	5224.0	3697.0	3906.0	5285.0	29.2%	168.0	49.0	79.0	161.0	70.8%		
ROGERS & TANIMOTO	24776.0	22947.0	19705.0	15753.0	36.4%	9683.0	1162.0	1049.0	856.0	91.2%		
ROGOT1	21118.0	17871.0	15195.0	11296.0	46.5%	33.0	31.0	33.0	55.0	6.1%		
ROGOT2	11686.0	8628.0	6707.0	5365.0	54.1%	27.0	25.0	25.0	44.0	7.4%		
RUSSELL & RAO	5307.0	3969.0	4203.0	5434.0	25.2%	203.0	63.0	88.0	189.0	69.0%		
SCOTT	21118.0	17871.0	15195.0	11296.0	46.5%	33.0	31.0	33.0	55.0	6.1%		
SIMPLE MATCHING	24776.0	22947.0	19705.0	15753.0	36.4%	9683.0	1162.0	1049.0	856.0	91.2%		
SOKAL	24776.0	22947.0	19705.0	15753.0	36.4%	9683.0	1162.0	1049.0	856.0	91.2%		
SØRENSEN-DICE	5324.0	3428.0	3360.0	4382.0	36.9%	27.0	23.0	26.0	40.0	14.8%		
TARANTULA	5321.0	3423.0	3352.0	4198.0	37.0%	29.0	25.0	26.0	45.0	13.8%		
WONG1	5307.0	3969.0	4203.0	5434.0	25.2%	203.0	63.0	88.0	189.0	69.0%		
WONG3	20454.0	16794.0	15619.0	13717.0	32.9%	6199.0	549.0	443.0	443.0	92.9%		
WONG2	24776.0	22947.0	19705.0	15753.0	36.4%	9683.0	1162.0	1049.0	856.0	91.2%		
ZOLTAR	18042.0	7397.0	7397.0	7403.0	59.0%	27.0	23.0	24.0	41.0	14.8%		

TABLE 2: OVERVIEW OF ALL EXAMINED SBFL METRICS WITH $\tilde{\mathcal{R}}_\lambda(\Omega)$ AND $\tilde{\mathcal{R}}_\lambda^*(\Omega)$ FOR $\lambda \in \{1.0, 0.98, 0.9, 0.5\}$ AND THE MAXIMUM IMPROVEMENTS FOR THE HIGHEST VALUES WITH REGARD TO $\lambda = 1$. HIGHEST RANKINGS ARE PRINTED WITH A BOLD FONT FOR EACH SET OF VALUES.

SBFL ranking metric	$\widetilde{\lambda}_p, (\lambda_p), [\min, \max]$	$\widetilde{RI}_{\overline{R}}^{SBFL}, (RI_{\overline{R}}^{SBFL}), [\min, \max]$	$\widetilde{RI}_{\overline{R}}^{LM}, (RI_{\overline{R}}^{LM}), [\min, \max]$
AMPLE	0.98, (0.98), [0.98,0.98]	0.3%, (-0.4%), [-8.8%,4.1%]	58.3%, (56.8%), [34.7%,78.2%]
ANDERBERG	0.98, (0.98), [0.98,0.98]	4.3%, (2.9%), [-10.1%,17.1%]	50.2%, (48.7%), [16.4%,70.4%]
ARITHMETIC MEAN	0.17, (0.18), [0.16,0.22]	18.6%, (18.6%), [3.8%,32.7%]	40.6%, (36.2%), [5.1%,51.5%]
COHEN	0.16, (0.17), [0.16,0.22]	18.3%, (16.5%), [-0.8%,32.7%]	40.4%, (36.3%), [5.1%,51.7%]
DICE	0.98, (0.98), [0.98,0.98]	4.3%, (2.9%), [-10.1%,17.1%]	50.2%, (48.7%), [16.4%,70.4%]
EUCLID	0.02, (0.02), [0.02,0.02]	37.7%, (36.1%), [17.9%,44.5%]	4.2%, (4.4%), [-0.3%,9.7%]
FLEISS	0.06, (0.07), [0.06,0.1]	34.5%, (32.3%), [11.4%,43.1%]	23.6%, (21.0%), [-1.3%,41.1%]
GEOMETRIC MEAN	0.14, (0.16), [0.14,0.2]	20.7%, (20.6%), [7.2%,32.2%]	40.2%, (35.5%), [5.2%,51.1%]
GOODMAN	0.98, (0.98), [0.98,0.98]	4.3%, (3.1%), [-10.1%,17.1%]	50.2%, (48.6%), [16.4%,70.4%]
GP13	0.98, (0.98), [0.98,0.98]	4.1%, (2.8%), [-10.0%,16.3%]	48.7%, (47.5%), [16.5%,70.1%]
HAMANN	0.02, (0.02), [0.02,0.02]	37.7%, (36.1%), [17.9%,44.5%]	4.2%, (4.4%), [-0.3%,9.7%]
HAMMING ETC.	0.02, (0.02), [0.02,0.02]	37.7%, (36.1%), [17.9%,44.5%]	4.2%, (4.4%), [-0.3%,9.7%]
HARMONIC MEAN	0.14, (0.15), [0.14,0.2]	21.0%, (21.1%), [6.8%,32.1%]	40.3%, (35.3%), [4.8%,51.1%]
JACCARD	0.98, (0.98), [0.98,0.98]	4.3%, (2.9%), [-10.1%,17.1%]	50.2%, (48.7%), [16.4%,70.4%]
KULCZYNSKI1	0.98, (0.98), [0.98,0.98]	4.3%, (2.9%), [-10.1%,17.1%]	50.2%, (48.7%), [16.4%,70.4%]
KULCZYNSKI2	0.98, (0.98), [0.98,0.98]	4.2%, (2.8%), [-10.0%,16.4%]	49.0%, (47.8%), [16.5%,70.4%]
M1	0.02, (0.02), [0.02,0.02]	37.7%, (36.1%), [17.9%,44.5%]	4.2%, (4.4%), [-0.3%,9.7%]
M2	0.98, (0.98), [0.98,0.98]	4.2%, (2.8%), [-10.0%,16.4%]	48.8%, (47.7%), [16.5%,70.1%]
OCHIAI	0.98, (0.98), [0.98,0.98]	4.3%, (2.9%), [-10.1%,17.0%]	49.8%, (48.5%), [16.4%,70.4%]
OCHIAI2	0.98, (0.98), [0.98,0.98]	4.0%, (2.9%), [-10.1%,17.1%]	50.2%, (47.6%), [16.0%,68.8%]
NAISH2 (Op2)	0.28, (0.3), [0.22,0.44]	8.7%, (9.0%), [-7.0%,21.2%]	41.2%, (39.1%), [4.2%,59.2%]
OVERLAP	0.98, (0.98), [0.98,0.98]	4.3%, (3.2%), [-9.4%,17.1%]	48.8%, (47.3%), [16.7%,69.8%]
ROGERS & TANIMOTO	0.02, (0.02), [0.02,0.02]	37.7%, (36.1%), [17.9%,44.5%]	4.2%, (4.4%), [-0.3%,9.7%]
ROGOT1	0.06, (0.06), [0.06,0.08]	34.1%, (32.4%), [12.7%,43.5%]	24.3%, (21.6%), [-0.4%,41.8%]
ROGOT2	0.14, (0.15), [0.14,0.2]	23.3%, (22.1%), [7.6%,30.1%]	41.9%, (35.8%), [4.8%,51.1%]
RUSSELL & RAO	0.98, (0.98), [0.98,0.98]	4.3%, (3.0%), [-9.4%,16.7%]	48.3%, (46.9%), [16.6%,69.3%]
SCOTT	0.06, (0.06), [0.06,0.08]	34.1%, (32.4%), [12.7%,43.5%]	24.3%, (21.6%), [-0.4%,41.8%]
SIMPLE MATCHING	0.02, (0.02), [0.02,0.02]	37.7%, (36.1%), [17.9%,44.5%]	4.2%, (4.4%), [-0.3%,9.7%]
SOKAL	0.02, (0.02), [0.02,0.02]	37.7%, (36.1%), [17.9%,44.5%]	4.2%, (4.4%), [-0.3%,9.7%]
SØRENSEN-DICE	0.98, (0.98), [0.98,0.98]	4.3%, (2.9%), [-10.1%,17.1%]	50.2%, (48.7%), [16.4%,70.4%]
TARANTULA	0.98, (0.98), [0.98,0.98]	4.3%, (2.9%), [-10.1%,17.1%]	50.3%, (48.9%), [16.4%,70.5%]
WONG1	0.98, (0.98), [0.98,0.98]	4.3%, (3.0%), [-9.4%,16.7%]	48.3%, (46.9%), [16.6%,69.3%]
WONG3	0.06, (0.06), [0.04,0.08]	28.0%, (25.6%), [11.2%,34.9%]	8.4%, (9.4%), [-1.0%,26.2%]
WONG2	0.02, (0.02), [0.02,0.02]	37.7%, (36.1%), [17.9%,44.5%]	4.2%, (4.4%), [-0.3%,9.7%]
ZOLTAR	0.98, (0.98), [0.98,0.98]	6.3%, (6.2%), [-8.7%,20.4%]	43.7%, (38.8%), [4.8%,61.8%]

TABLE 3: RESULTS OF THE 10-FOLD CROSS VALIDATION OF $\overline{\mathcal{R}}_{\lambda_p}(\Omega)$.

SBFL ranking metric	$\widetilde{\lambda}_p, (\lambda_p)$, [min, max]	$\widetilde{RI}_{\overline{R}^*}^{SBFL}, (RI_{\overline{R}^*}^{SBFL})$, [min, max]	$\widetilde{RI}_{\overline{R}^*}^{LM}, (RI_{\overline{R}^*}^{LM})$, [min, max]
AMPLE	0.76, (0.8), [0.76,0.9]	24.2%, (25.9%), [0.1%,50.5%]	85.2%, (83.8%), [63.4%,95.7%]
ANDERBERG	0.98, (0.97), [0.88,0.98]	31.6%, (31.0%), [1.8%,57.4%]	93.2%, (92.8%), [88.0%,97.2%]
ARITHMETIC MEAN	0.58, (0.58), [0.52,0.62]	36.9%, (29.7%), [-51.5%,65.5%]	88.2%, (85.6%), [64.4%,94.1%]
COHEN	0.58, (0.62), [0.58,0.76]	33.0%, (23.6%), [-51.9%,65.4%]	87.8%, (86.2%), [67.4%,94.1%]
DICE	0.98, (0.97), [0.88,0.98]	31.6%, (31.0%), [1.8%,57.4%]	93.2%, (92.8%), [88.0%,97.2%]
EUCLID	0.06, (0.07), [0.06,0.08]	70.4%, (71.4%), [58.0%,81.7%]	21.1%, (19.7%), [1.4%,34.4%]
FLEISS	0.24, (0.24), [0.22,0.26]	68.2%, (63.0%), [20.2%,82.9%]	68.1%, (65.4%), [27.8%,82.7%]
GEOMETRIC MEAN	0.42, (0.43), [0.42,0.48]	39.9%, (31.3%), [-71.8%,64.0%]	87.2%, (84.1%), [53.3%,93.3%]
GOODMAN	0.88, (0.88), [0.86,0.92]	42.3%, (32.3%), [-9.6%,69.5%]	93.2%, (92.4%), [86.0%,96.9%]
GP13	0.78, (0.79), [0.78,0.86]	41.0%, (32.9%), [5.1%,51.7%]	88.5%, (88.2%), [81.4%,93.7%]
HAMANN	0.06, (0.07), [0.06,0.08]	70.4%, (71.4%), [58.0%,81.7%]	21.1%, (19.7%), [1.4%,34.4%]
HAMMING ETC.	0.06, (0.07), [0.06,0.08]	70.4%, (71.4%), [58.0%,81.7%]	21.1%, (19.7%), [1.4%,34.4%]
HARMONIC MEAN	0.44, (0.44), [0.44,0.48]	41.1%, (34.6%), [-51.0%,66.2%]	87.7%, (84.2%), [51.5%,94.0%]
JACCARD	0.98, (0.97), [0.88,0.98]	31.6%, (31.0%), [1.8%,57.4%]	93.2%, (92.8%), [88.0%,97.2%]
KULCZYNSKI1	0.98, (0.97), [0.88,0.98]	31.6%, (31.0%), [1.8%,57.4%]	93.2%, (92.8%), [88.0%,97.2%]
KULCZYNSKI2	0.88, (0.87), [0.8,0.9]	44.7%, (34.1%), [-16.6%,56.6%]	90.5%, (90.6%), [83.4%,96.7%]
M1	0.06, (0.07), [0.06,0.08]	70.4%, (71.4%), [58.0%,81.7%]	21.1%, (19.7%), [1.4%,34.4%]
M2	0.81, (0.82), [0.78,0.88]	42.2%, (34.3%), [2.6%,53.5%]	89.6%, (89.3%), [81.2%,94.6%]
OCHIAI	0.88, (0.9), [0.88,0.98]	30.3%, (28.3%), [-7.8%,56.7%]	92.7%, (92.4%), [87.2%,97.5%]
OCHIAI2	0.98, (0.97), [0.88,0.98]	39.1%, (33.8%), [0.8%,59.9%]	91.8%, (90.7%), [81.9%,96.3%]
NAISH2 (Op2)	0.78, (0.78), [0.76,0.8]	32.0%, (33.6%), [4.2%,66.7%]	88.8%, (88.1%), [81.1%,93.6%]
OVERLAP	0.98, (0.98), [0.98,0.98]	56.8%, (56.7%), [45.5%,69.2%]	91.1%, (90.3%), [85.0%,94.3%]
ROGERS & TANIMOTO	0.06, (0.07), [0.06,0.08]	70.4%, (71.4%), [58.0%,81.7%]	21.1%, (19.7%), [1.4%,34.4%]
ROGOT1	0.18, (0.19), [0.18,0.24]	67.8%, (63.2%), [21.3%,83.0%]	68.5%, (66.0%), [32.0%,83.2%]
ROGOT2	0.44, (0.44), [0.44,0.48]	49.2%, (43.0%), [-51.0%,75.3%]	88.3%, (85.4%), [51.4%,93.9%]
RUSSELL & RAO	0.98, (0.98), [0.98,0.98]	45.2%, (46.6%), [36.7%,55.8%]	86.4%, (86.8%), [84.0%,90.6%]
SCOTT	0.18, (0.19), [0.18,0.24]	67.8%, (63.2%), [21.3%,83.0%]	68.5%, (66.0%), [32.0%,83.2%]
SIMPLE MATCHING	0.06, (0.07), [0.06,0.08]	70.4%, (71.4%), [58.0%,81.7%]	21.1%, (19.7%), [1.4%,34.4%]
SOKAL	0.06, (0.07), [0.06,0.08]	70.4%, (71.4%), [58.0%,81.7%]	21.1%, (19.7%), [1.4%,34.4%]
SØRENSEN-DICE	0.98, (0.97), [0.88,0.98]	31.6%, (31.0%), [1.8%,57.4%]	93.2%, (92.8%), [88.0%,97.2%]
TARANTULA	0.98, (0.97), [0.88,0.98]	31.6%, (31.0%), [3.5%,59.0%]	93.3%, (92.9%), [87.8%,97.2%]
WONG1	0.98, (0.98), [0.98,0.98]	45.2%, (46.6%), [36.7%,55.8%]	86.4%, (86.8%), [84.0%,90.6%]
WONG3	0.4, (0.38), [0.26,0.4]	64.5%, (66.7%), [51.2%,80.2%]	27.7%, (27.9%), [-1.4%,50.4%]
WONG2	0.06, (0.07), [0.06,0.08]	70.4%, (71.4%), [58.0%,81.7%]	21.1%, (19.7%), [1.4%,34.4%]
ZOLTAR	0.94, (0.95), [0.94,0.98]	60.7%, (57.3%), [23.7%,84.1%]	89.0%, (87.7%), [66.9%,97.2%]

TABLE 4: RESULTS OF THE 10-FOLD CROSS VALIDATION OF $\overline{R}_{\lambda_p}^*$ (Ω).

SBFL ranking metric	$\widetilde{\lambda}_p, (\lambda_p), [\min, \max]$	$\widetilde{RI}_{\widetilde{R}}^{SBFL}, (\overline{RI}_{\widetilde{R}}^{SBFL}), [\min, \max]$	$\widetilde{RI}_{\widetilde{R}}^{LM}, (\overline{RI}_{\widetilde{R}}^{LM}), [\min, \max]$
AMPLE	0.97, (0.97), [0.94,1.0]	-0.1%, (0.9%), [-11.3%,23.2%]	85.7%, (78.9%), [47.4%,97.6%]
ANDERBERG	0.98, (0.97), [0.94,0.98]	3.7%, (10.5%), [-4.6%,35.1%]	92.1%, (77.9%), [29.3%,98.0%]
ARITHMETIC MEAN	0.43, (0.54), [0.42,0.92]	-33.9%, (-36.3%), [-139.4%,59.8%]	83.9%, (66.3%), [-5.5%,96.1%]
COHEN	0.46, (0.56), [0.42,0.92]	-37.7%, (-34.6%), [-139.6%,60.9%]	83.6%, (66.1%), [-5.5%,96.1%]
DICE	0.98, (0.97), [0.94,0.98]	3.7%, (10.5%), [-4.6%,35.1%]	92.1%, (77.9%), [29.3%,98.0%]
EUCLID	0.04, (0.07), [0.02,0.18]	52.4%, (48.0%), [30.2%,62.4%]	8.1%, (6.6%), [-1.6%,15.4%]
FLEISS	0.2, (0.21), [0.1,0.3]	56.3%, (54.7%), [29.4%,75.6%]	39.5%, (40.8%), [-4.6%,83.2%]
GEOMETRIC MEAN	0.43, (0.52), [0.4,0.9]	-28.2%, (-33.2%), [-134.6%,60.9%]	84.3%, (66.1%), [-5.6%,95.6%]
GOODMAN	0.98, (0.97), [0.94,0.98]	3.7%, (10.5%), [-4.6%,35.1%]	92.1%, (77.9%), [29.3%,98.0%]
GP13	0.98, (0.97), [0.94,0.98]	0.0%, (8.4%), [-8.1%,35.1%]	81.3%, (72.3%), [29.3%,97.7%]
HAMANN	0.04, (0.07), [0.02,0.18]	52.4%, (48.0%), [30.2%,62.4%]	8.1%, (6.6%), [-1.6%,15.4%]
HAMMING ETC.	0.04, (0.07), [0.02,0.18]	52.4%, (48.0%), [30.2%,62.4%]	8.1%, (6.6%), [-1.6%,15.4%]
HARMONIC MEAN	0.42, (0.52), [0.38,0.9]	-37.0%, (-30.6%), [-138.8%,60.3%]	83.7%, (64.7%), [-9.4%,95.9%]
JACCARD	0.98, (0.97), [0.94,0.98]	3.7%, (10.5%), [-4.6%,35.1%]	92.1%, (77.9%), [29.3%,98.0%]
KULCZYNSKI1	0.98, (0.97), [0.94,0.98]	3.7%, (10.5%), [-4.6%,35.1%]	92.1%, (77.9%), [29.3%,98.0%]
KULCZYNSKI2	0.98, (0.97), [0.94,0.98]	1.3%, (8.6%), [-6.3%,35.1%]	81.7%, (73.4%), [29.3%,97.8%]
M1	0.04, (0.07), [0.02,0.18]	52.4%, (48.0%), [30.2%,62.4%]	8.1%, (6.6%), [-1.6%,15.4%]
M2	0.98, (0.98), [0.98,0.98]	2.2%, (9.4%), [-5.4%,35.1%]	81.3%, (73.0%), [29.3%,97.8%]
OCHIAI	0.98, (0.97), [0.94,0.98]	1.7%, (9.6%), [-5.0%,35.1%]	91.7%, (76.7%), [29.3%,97.9%]
OCHIAI2	0.98, (0.97), [0.86,0.98]	4.1%, (10.1%), [0.7%,34.9%]	92.0%, (77.1%), [28.2%,97.9%]
NAISH2 (Op2)	0.8, (0.82), [0.66,0.94]	-6.4%, (-12.9%), [-54.5%,14.6%]	80.2%, (63.3%), [-5.7%,97.2%]
OVERLAP	0.98, (0.98), [0.94,0.98]	9.9%, (15.2%), [-0.4%,35.1%]	84.4%, (72.6%), [29.3%,92.7%]
ROGERS & TANIMOTO	0.04, (0.07), [0.02,0.18]	52.4%, (48.0%), [30.2%,62.4%]	8.1%, (6.6%), [-1.6%,15.4%]
ROGOT1	0.2, (0.21), [0.1,0.3]	60.5%, (56.8%), [29.6%,75.3%]	42.3%, (42.4%), [-4.5%,87.6%]
ROGOT2	0.42, (0.52), [0.4,0.94]	-57.0%, (-48.6%), [-138.8%,62.0%]	84.4%, (64.3%), [-12.4%,94.9%]
RUSSELL & RAO	0.98, (0.98), [0.94,0.98]	12.3%, (11.5%), [-24.0%,35.1%]	79.8%, (70.7%), [29.3%,92.2%]
SCOTT	0.2, (0.21), [0.1,0.3]	60.5%, (56.8%), [29.6%,75.3%]	42.3%, (42.4%), [-4.5%,87.6%]
SIMPLE MATCHING	0.04, (0.07), [0.02,0.18]	52.4%, (48.0%), [30.2%,62.4%]	8.1%, (6.6%), [-1.6%,15.4%]
SOKAL	0.04, (0.07), [0.02,0.18]	52.4%, (48.0%), [30.2%,62.4%]	8.1%, (6.6%), [-1.6%,15.4%]
SØRENSEN-DICE	0.98, (0.97), [0.94,0.98]	3.7%, (10.5%), [-4.6%,35.1%]	92.1%, (77.9%), [29.3%,98.0%]
TARANTULA	0.97, (0.97), [0.94,0.98]	1.9%, (11.7%), [-2.7%,35.1%]	91.5%, (78.5%), [29.3%,98.3%]
WONG1	0.98, (0.98), [0.94,0.98]	12.3%, (11.5%), [-24.0%,35.1%]	79.8%, (70.7%), [29.3%,92.2%]
WONG3	0.2, (0.2), [0.16,0.22]	40.1%, (42.4%), [22.3%,65.0%]	15.6%, (17.4%), [-0.2%,53.1%]
WONG2	0.04, (0.07), [0.02,0.18]	52.4%, (48.0%), [30.2%,62.4%]	8.1%, (6.6%), [-1.6%,15.4%]
ZOLTAR	0.48, (0.58), [0.32,0.98]	3.2%, (-22.7%), [-203.3%,55.5%]	79.4%, (67.6%), [10.0%,96.3%]

TABLE 5: RESULTS OF THE 10-FOLD CROSS VALIDATION OF $\widetilde{R}_{\lambda_p}(\Omega)$.

SBFL ranking metric	$\widetilde{\lambda}_p, (\lambda_p)$, [min, max]	$\widetilde{RI}_{\widetilde{R}^*}^{SBFL}, (RI_{\widetilde{R}^*}^{SBFL})$, [min, max]	$\widetilde{RI}_{\widetilde{R}^*}^{LM}, (RI_{\widetilde{R}^*}^{LM})$, [min, max]
AMPLE	0.99, (0.96), [0.9,1.0]	0.0%, (-2.8%), [-21.9%,18.5%]	97.9%, (97.1%), [94.1%,98.7%]
ANDERBERG	0.98, (0.97), [0.94,0.98]	10.2%, (10.5%), [-42.5%,41.7%]	98.6%, (98.3%), [95.3%,99.6%]
ARITHMETIC MEAN	0.98, (0.98), [0.98,0.98]	10.2%, (15.8%), [-6.5%,50.0%]	98.7%, (98.2%), [94.3%,99.6%]
COHEN	0.98, (0.97), [0.94,0.98]	10.2%, (15.7%), [-6.5%,50.0%]	98.7%, (98.2%), [94.3%,99.6%]
DICE	0.98, (0.97), [0.94,0.98]	10.2%, (10.5%), [-42.5%,41.7%]	98.6%, (98.3%), [95.3%,99.6%]
EUCLID	0.38, (0.43), [0.34,0.9]	91.1%, (90.6%), [81.1%,97.2%]	51.7%, (49.9%), [-4.9%,92.9%]
FLEISS	0.98, (0.99), [0.98,1.0]	1.7%, (3.5%), [-12.2%,23.3%]	97.5%, (97.5%), [94.7%,99.5%]
GEOMETRIC MEAN	0.98, (0.98), [0.98,0.98]	10.5%, (16.9%), [-2.9%,56.3%]	98.7%, (98.1%), [94.3%,99.6%]
GOODMAN	0.98, (0.97), [0.94,0.98]	10.2%, (10.5%), [-42.5%,41.7%]	98.6%, (98.3%), [95.3%,99.6%]
GP13	0.98, (0.98), [0.94,0.98]	13.2%, (12.2%), [-30.5%,60.6%]	98.7%, (98.3%), [96.7%,99.5%]
HAMANN	0.38, (0.43), [0.34,0.9]	91.1%, (90.6%), [81.1%,97.2%]	51.7%, (49.9%), [-4.9%,92.9%]
HAMMING ETC.	0.38, (0.43), [0.34,0.9]	91.1%, (90.6%), [81.1%,97.2%]	51.7%, (49.9%), [-4.9%,92.9%]
HARMONIC MEAN	0.98, (0.97), [0.9,1.0]	0.0%, (4.2%), [-32.5%,35.7%]	98.7%, (98.3%), [95.7%,99.6%]
JACCARD	0.98, (0.97), [0.94,0.98]	10.2%, (10.5%), [-42.5%,41.7%]	98.6%, (98.3%), [95.3%,99.6%]
KULCZYNSKI1	0.98, (0.97), [0.94,0.98]	10.2%, (10.5%), [-42.5%,41.7%]	98.6%, (98.3%), [95.3%,99.6%]
KULCZYNSKI2	0.98, (0.97), [0.9,0.98]	12.9%, (14.7%), [-7.4%,50.0%]	98.6%, (98.6%), [97.3%,99.7%]
M1	0.38, (0.43), [0.34,0.9]	91.1%, (90.6%), [81.1%,97.2%]	51.7%, (49.9%), [-4.9%,92.9%]
M2	0.98, (0.98), [0.98,0.98]	9.4%, (11.5%), [-11.4%,53.6%]	98.6%, (98.4%), [97.2%,99.5%]
OCHIAI	0.98, (0.96), [0.92,0.98]	4.9%, (10.8%), [-42.5%,56.3%]	98.4%, (98.2%), [95.3%,99.7%]
OCHIAI2	0.98, (0.97), [0.92,0.98]	9.5%, (15.8%), [-3.5%,56.3%]	98.7%, (98.1%), [93.7%,99.6%]
NAISH2 (Op2)	0.98, (0.98), [0.94,0.98]	13.2%, (12.2%), [-30.5%,60.6%]	98.7%, (98.3%), [96.7%,99.5%]
OVERLAP	0.98, (0.98), [0.98,0.98]	67.1%, (66.7%), [43.2%,84.1%]	96.9%, (96.8%), [94.2%,99.4%]
ROGERS & TANIMOTO	0.38, (0.43), [0.34,0.9]	91.1%, (90.6%), [81.1%,97.2%]	51.7%, (49.9%), [-4.9%,92.9%]
ROGOT1	0.98, (0.97), [0.94,0.98]	8.3%, (8.8%), [-19.4%,28.6%]	97.9%, (97.8%), [94.2%,99.6%]
ROGOT2	0.98, (0.97), [0.9,1.0]	0.0%, (8.0%), [-5.4%,35.7%]	98.7%, (98.4%), [96.8%,99.6%]
RUSSELL & RAO	0.98, (0.98), [0.98,0.98]	75.9%, (73.8%), [48.6%,84.1%]	96.1%, (96.1%), [93.0%,99.2%]
SCOTT	0.98, (0.97), [0.94,0.98]	8.3%, (8.8%), [-19.4%,28.6%]	97.9%, (97.8%), [94.2%,99.6%]
SIMPLE MATCHING	0.38, (0.43), [0.34,0.9]	91.1%, (90.6%), [81.1%,97.2%]	51.7%, (49.9%), [-4.9%,92.9%]
SOKAL	0.38, (0.43), [0.34,0.9]	91.1%, (90.6%), [81.1%,97.2%]	51.7%, (49.9%), [-4.9%,92.9%]
SØRENSEN-DICE	0.98, (0.97), [0.94,0.98]	10.2%, (10.5%), [-42.5%,41.7%]	98.6%, (98.3%), [95.3%,99.6%]
TARANTULA	0.98, (0.96), [0.9,0.98]	15.3%, (17.8%), [-6.2%,50.0%]	98.6%, (98.4%), [96.6%,99.7%]
WONG1	0.98, (0.98), [0.98,0.98]	75.9%, (73.8%), [48.6%,84.1%]	96.1%, (96.1%), [93.0%,99.2%]
WONG3	0.69, (0.69), [0.58,0.78]	90.4%, (88.5%), [71.1%,96.6%]	66.8%, (64.8%), [31.3%,92.0%]
WONG2	0.38, (0.43), [0.34,0.9]	91.1%, (90.6%), [81.1%,97.2%]	51.7%, (49.9%), [-4.9%,92.9%]
ZOLTAR	0.98, (0.96), [0.9,0.98]	8.5%, (12.7%), [-15.9%,50.0%]	98.6%, (98.6%), [97.3%,99.7%]

TABLE 6: RESULTS OF THE 10-FOLD CROSS VALIDATION OF $\widetilde{R}_{\lambda_p}^*$ (Ω).

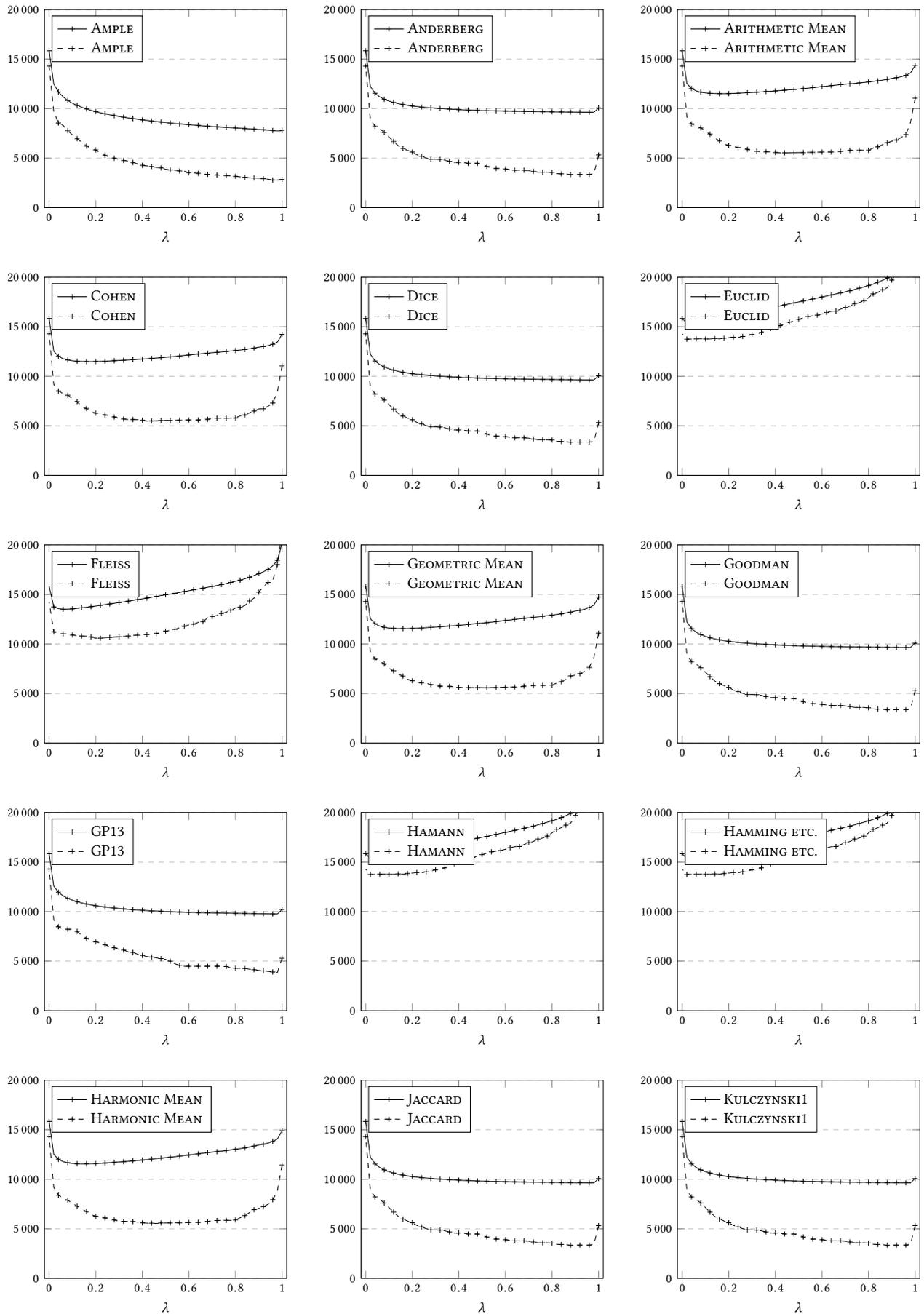


FIGURE 1: PLOTS OF $\bar{\mathcal{R}}_\lambda(\Omega)$ (SOLID) AND $\bar{\mathcal{R}}_\lambda(\Omega)$ (DASHED) FOR DIFFERENT SBFL RANKING METRICS.

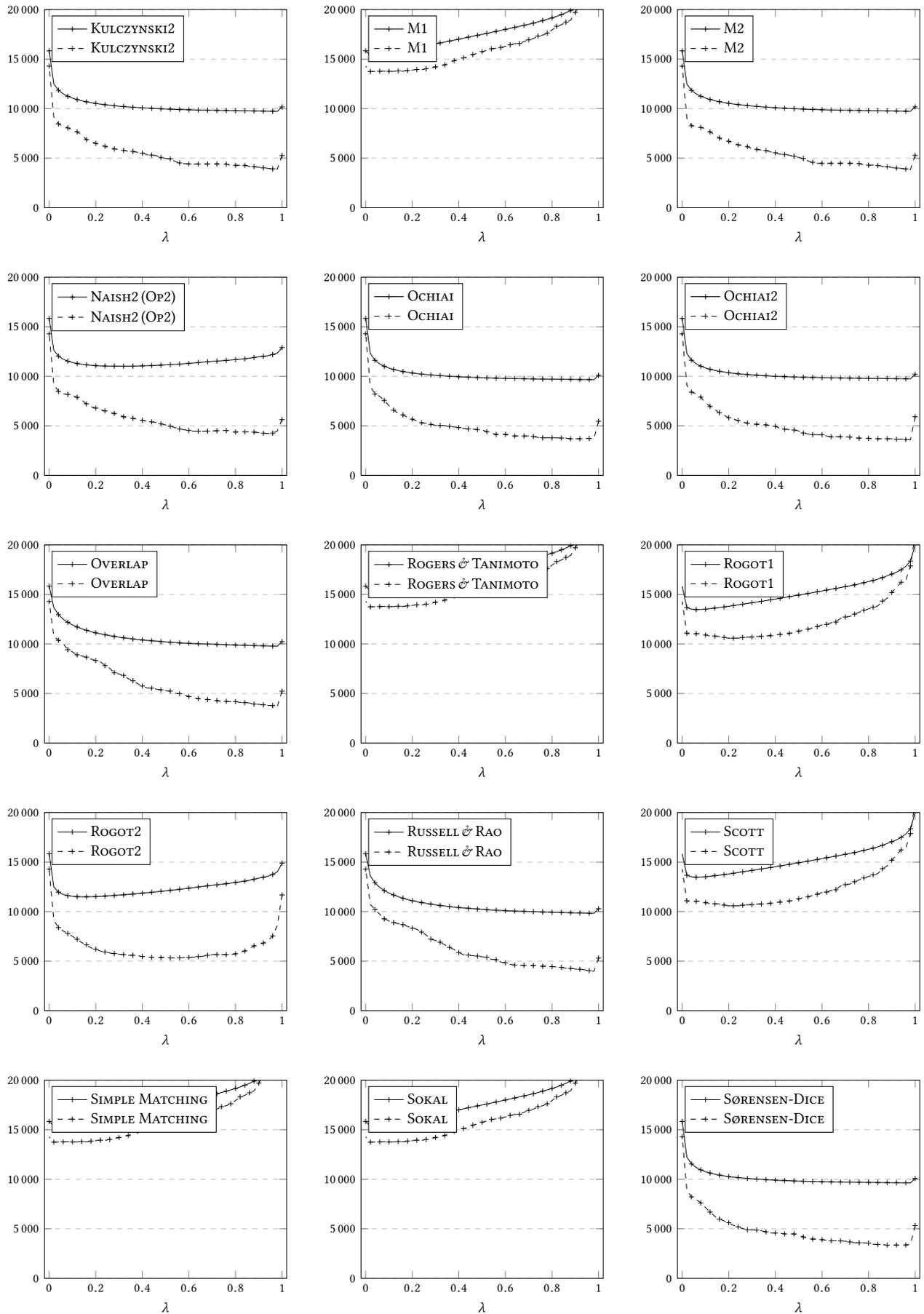


FIGURE 2: PLOTS OF $\bar{\mathcal{R}}_\lambda(\Omega)$ (SOLID) AND $\bar{\mathcal{R}}_\lambda(\Omega)$ (DASHED) FOR DIFFERENT SBFL RANKING METRICS.

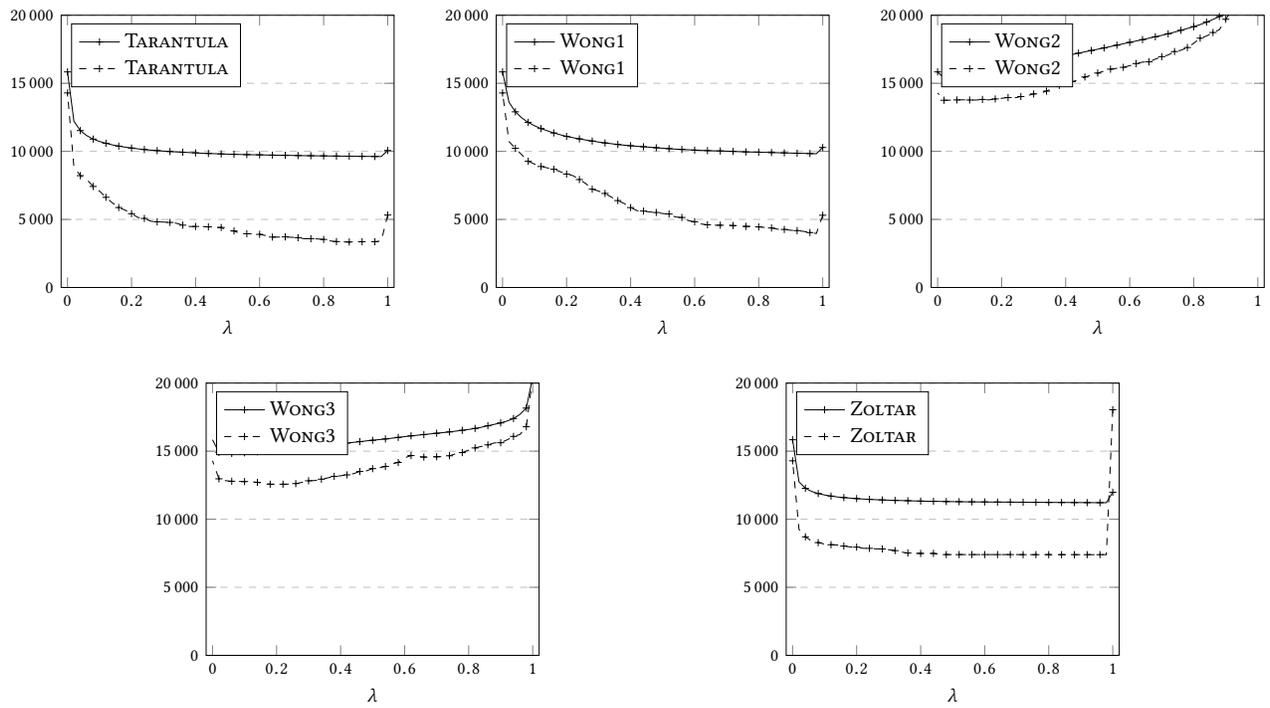


FIGURE 3: PLOTS OF $\bar{\mathcal{R}}_\lambda(\Omega)$ (SOLID) AND $\tilde{\mathcal{R}}_\lambda(\Omega)$ (DASHED) FOR DIFFERENT SBFL RANKING METRICS.

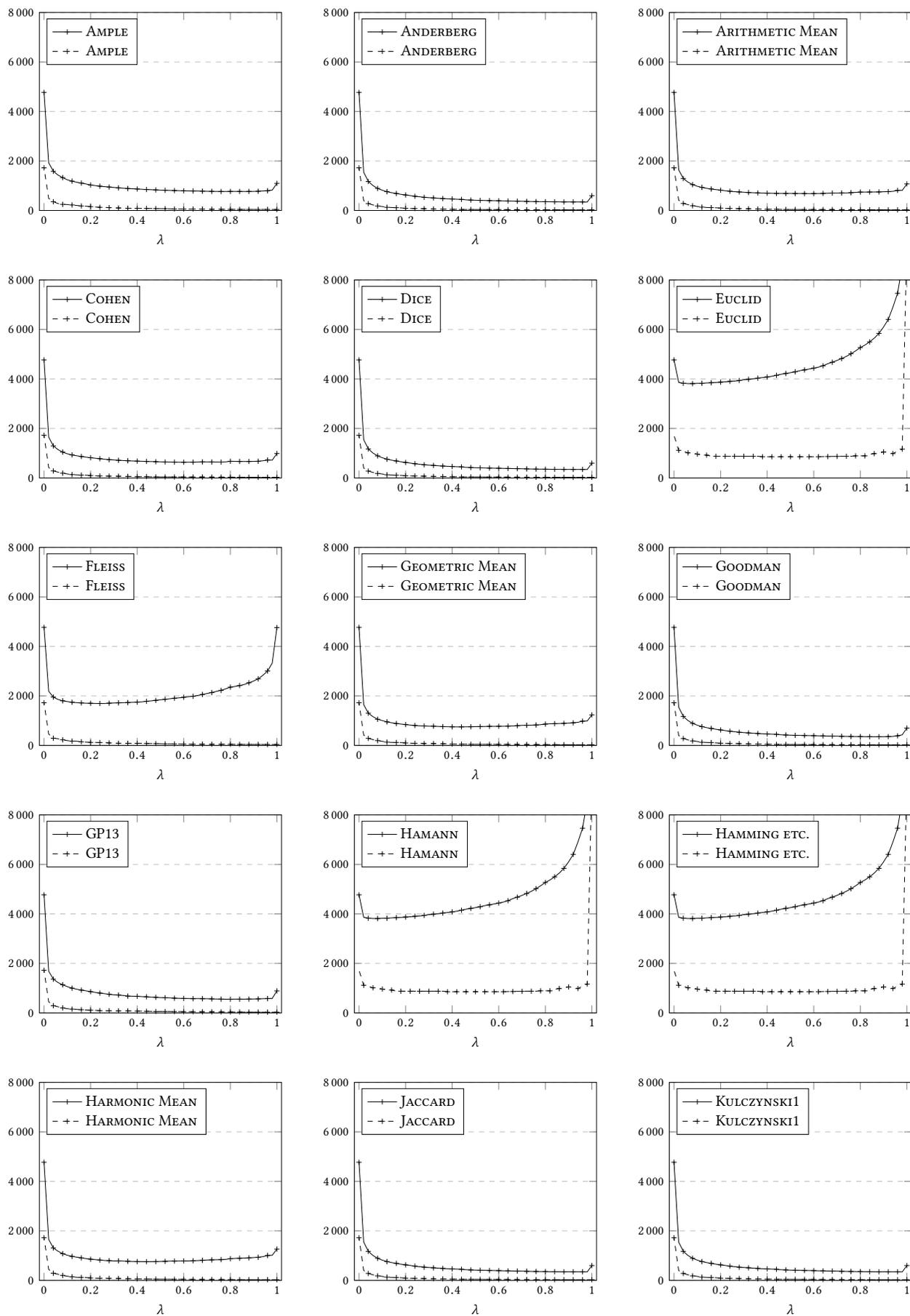


FIGURE 4: PLOTS OF $\bar{\mathcal{R}}_{\lambda}^*(\Omega)$ (SOLID) $\tilde{\mathcal{R}}_{\lambda}^*(\Omega)$ (DASHED) FOR DIFFERENT SBFL RANKING METRICS.

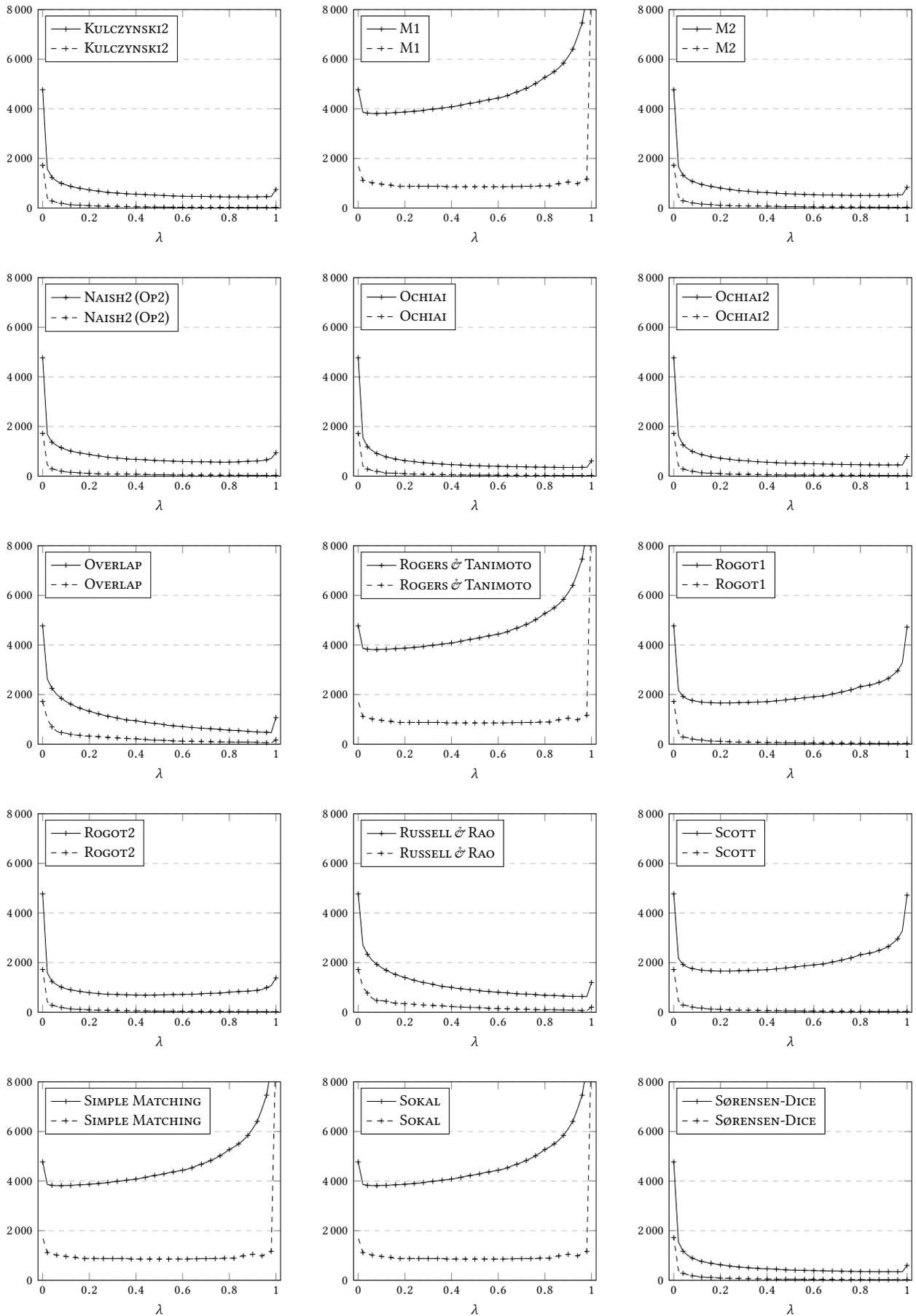


FIGURE 5: PLOTS OF $\bar{\mathcal{R}}_{\lambda}^*(\Omega)$ (SOLID) $\bar{\mathcal{R}}_{\lambda}(\Omega)$ (DASHED) FOR DIFFERENT SBFL RANKING METRICS.

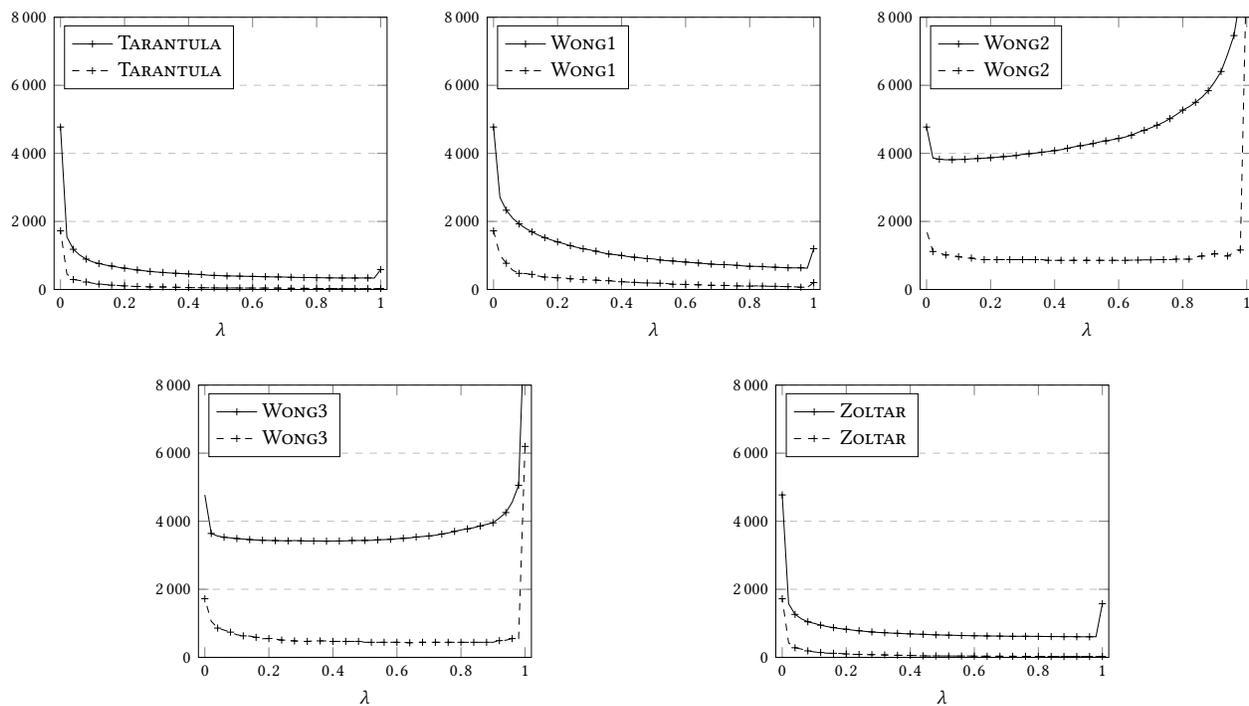


FIGURE 6: PLOTS OF $\bar{\mathcal{R}}_\lambda^*(\Omega)$ (SOLID) $\tilde{\mathcal{R}}_\lambda^*(\Omega)$ (DASHED) FOR DIFFERENT SBFL RANKING METRICS.